

# Extended Criticality in Biology

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[www.di.ens.fr/users/longo](http://www.di.ens.fr/users/longo)

Bailly F., Longo G. **Mathematics and the Natural Sciences. The Physical Singularity of Life.** *Imperial College Press*, London, 2011  
(français: Hermann, 2006).

G. Longo. Emergence vs Novelty Production in Physics vs Biology. In  
*Open Historicity of Life. Theory epistemology, practice*, Paris,  
October, 2023 (to appear in the proceedings: Chollat, Montévil,  
Robert eds.)

# Criticality in Complex Systems

Self-organization and

1 - critical transitions in equilibrium dynamics

2 - critical transitions in far from equilibrium systems

3 – extended criticality in Biology

critical transitions in *least intervals* of time (scale dependent) a (weak) form of mathematical density (a weak topology of least intervals)

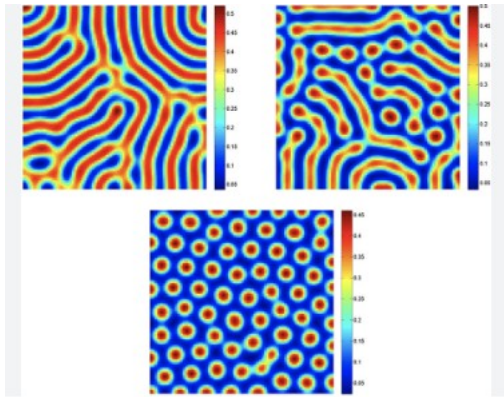
H.J. Jensen. **Self-Organized Criticality, Emergent Complex Behavior in Physical and Biological Systems.** *Cambridge lec. in Physics*, 1998

# 1 - Physical Emergence

(at equilibrium, self-organised; *a time of processes*)

Turing patterns, 1952:

a “**perturbation triggers**” a (chemical) action-reaction-diffusion



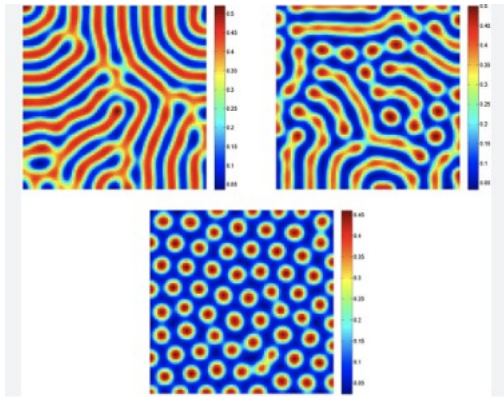
**New forms** « emerge » along the process by **critical** (“catastrophic”, says Turing) **transitions**

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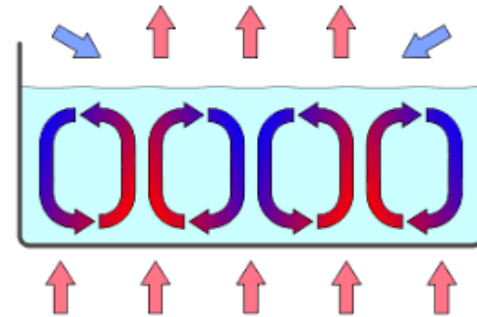
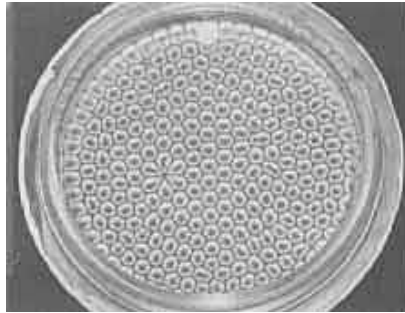
**New forms** « emerge » along the process by **critical** (“catastrophic”, says Turing) **transitions** (*Belousov–Zhabotinsky reactions, 1961*)

Every surface and path is **optimal** (a geodetic): just physical forces acting on **inert molecules**, that “follow the flow” - **Thom’s morphog.**

## 2 - Physical Emergence

(far from/at equilibrium, self-organised; a *time* of processes)

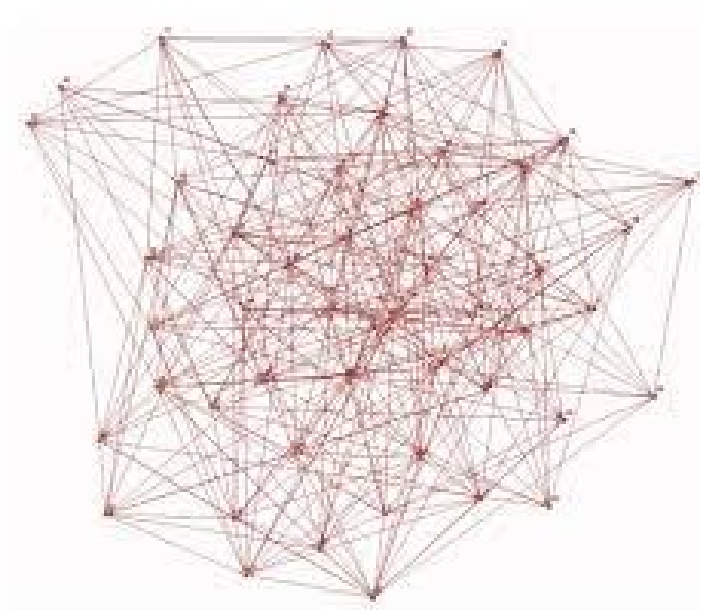
- Benard Cells:



- Parisi's Networks  
(Spin Glasses  
and its mathematics)

Mathematically:

- all *point-wise* transitions
- a new “structure of coherence”
- symmetry changes



# Towards Biology

## Darwin:

*first principle*: “descent with modification”

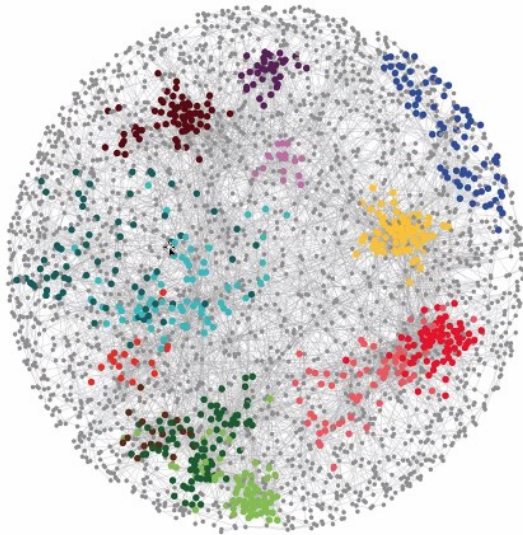
(At each reproduction: variation)

“even not breeders ...”

*second principle*: “selection”

(the exclusion of the incompatible *stabilizes*  
species/populations... organisms)

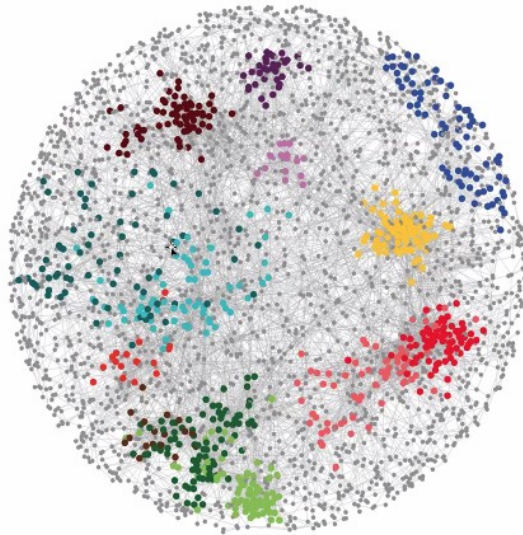
# Biology, molecular level: Gene interaction *networks*



Raamesh Deshpande,  
**Interaction network** of genes in *S. cerevisiae*

M. Nykter, N.D. Price, M. Aldana, S.A. Ramsey, S.A. Kauffman, L.E. Hood, O. Yli-Harja, and I. Shmulevich. **Gene expression dynamics in the macrophage exhibit criticality.** *PNAS*, 105(6):1897, 2008.

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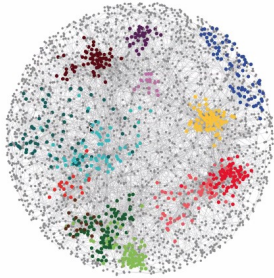
- Key aspects of “critical” emergence: the formation of
- extended **correlation** lengths and
  - **coherence** structures,
  - the **divergence** of some observables w.r. to the control parameter(s) (the **global** affects the local, renormalization, critical exponents), etc....

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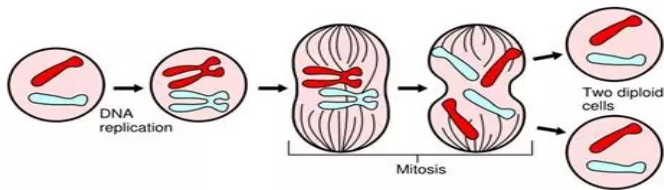
## Gene interaction *networks* in an *organism*



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In an organism, **each cell reproduction is *also* a critical transition:**  
a bifurcation, a re-organization of the coherence structure: tissue matrix, collagen's tensegrity structure, the cells' molecular exchanges

### Major Events in Mitosis

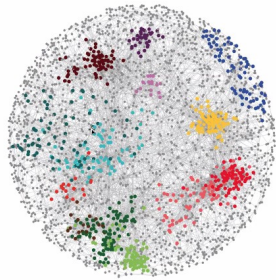


### Biological Time:

always given in **intervals**, by rhythms  
(metabolic, cardiac, respiration...)

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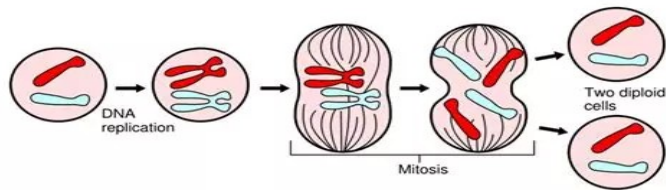
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### Major Events in Mitosis



**Biological Time:**  
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Biological **stability** (at transitions) is given by **constraints**, in the **nesting** and **interaction** of different levels of organization:  
molecular networks, cells, tissue, organism, ecosystem  
*no preferred causal level*

# Brain Networks

E. Lovecchio, P. Allegrini, E. Geneston, B. West, P. Grigolini, From self-organized to extended criticality, *Frontiers in Phys.* Vol 3, 2012

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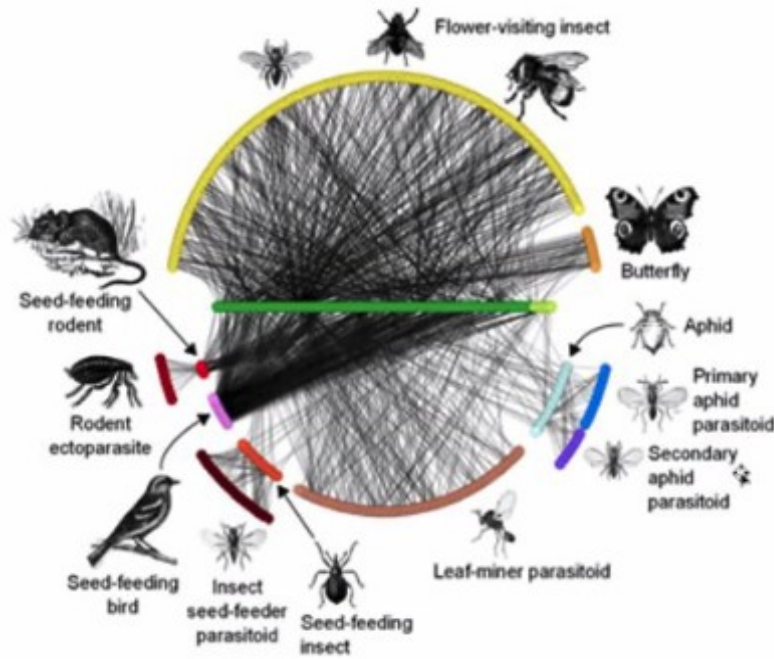
## Cooperatively firing neurons:

- (i) infinitely large time period, **temporal complexity** corresponds to Mittag-Leffler complexity;
- (ii) For large values of the **interaction coupling** the periodic nature of the process becomes predominant while maintaining to some extent, in the intermediate time asymptotic region, the signature of complexity;
- (iii) Focusing our attention on firing neuron **avalanches**

« extended criticality advocated by Bailly and Longo, 2006 »

# **Ecosystemic interaction *networks* (of organisms)**

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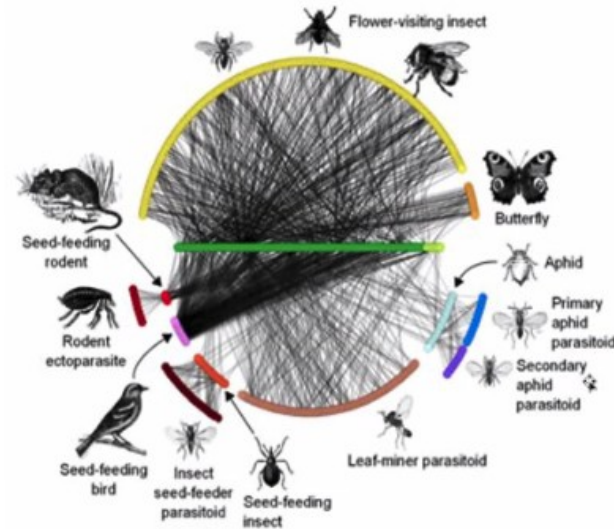
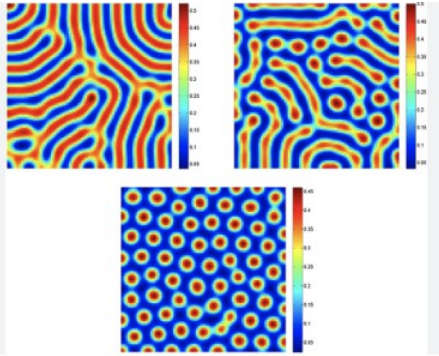
Our networks comprised **1501 quantified unique interactions between a total of 560 taxa**, comprising plants and 11 groups of animals...

Pocock et al. 2012. The robustness and restoration of a network of ecological network. *Science* 335: 973-977.

Courtesy of  
A. Hilbeck

A fine-tuning of **rhythms** (metabolic, circadian... *global* and *individual*)  
All different individuals, they are **specific**, the *result of a history*  
*of* the **generic** (identical) elements of a physical network

# Criticality and Emergence in physical vs biological interaction networks



Species' **interaction**  
networks at Norwood  
Farm (125 ha),  
Somerset, UK



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Changes in **individual** organisms  
(phylogenetic paths) are *causes* and  
*consequences* of network deformations

**Generic** components/elements  
Emergence and transitions: in  
the network, pointwise

Rhythms give least **intervals of time**,  
many “transitions” in each interval

# Summary: Physical vs Biological networks (“*emergence*”)

## Physics:

- Emerging collective behavior, many possible equilibria
- Necessary (qualitatively predictable, in probabilities)
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- “Emerging” *collective* and *individual* (phylogenetic trajectories)
- Coordinating or disrupting *bio-rhythms* (and physical frequencies)
- Rhythms produce *least intervals*, that contain **numerous critical transitions** (at least: gene and molecular networks, reproductions)

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**Extended Critical Transitions (dense in a time of viability)**

## Some readings in Biology

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M. Nykter, N.D. Price, M. Aldana, S.A. Ramsey, S.A. Kauffman, L.E. Hood, O. Yli-Harja, and I. Shmulevich. Gene expression dynamics in the macrophage exhibit criticality. *PNAS*, 105(6):1897, 2008.

G. Longo and M. Montévil. From physics to biology by extending criticality and symmetry breakings. *Progress in Biophysics and Molecular Biology, Systems Biology and Cancer*, 106(2):340 – 347, 2011 (more papers on this are in <https://www.di.ens.fr/users/longo/download.html> )

E. Lovecchio, P. Allegrini, E. Geneston, B. West, P. Grigolini, From self-organized to extended criticality *Frontiers in Phys.* Vol 3, 2012