#### PLDI'03

# A Static Analyzer for Large Safety-Critical Software

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# Automatic Program Verification by Abstract Interpretation

#### Result:

- Can produce zero or very few false alarms
   while checking non-trivial properties (absence of Run-Time Error);
- Does scale up

#### How?

- We specialize the abstract interpreter for a family of programs (which correctness proofs would be similar).
- ♦ The abstract domains are **generic** invariants automatically instantiated by the analyzer (to make these proofs).

# **Considered Programs and Semantics**

### Which Programs are Considered?

- Embedded avionic programs;
- Automatically generated from a proprietary graphical system control language (à la Simulink);
- Synchronous real-time critical programs:

```
declare volatile input, state, and output variables;
initialize state variables;
loop forever
  read volatile input variables,
  compute output and state variables,
  write to volatile output variables;
  wait for next clock tick
end loop
```

### Main Characteristics of the Programs

#### **Difficulties:**

- lacktriangle Many global variables and arrays (> 10 000);
- ♦ A huge loop (> 75 000 lines after simplification);
- Each iteration depends on the state of the previous iterations (state variables);
- Floating-point computations
   (80% of the code implements non-linear control with feed-back);
- Everything is interdependent (live variables analysis, slicing ineffective);
- Abstraction by elimination of any variable is too imprecise.

#### **Simplicities:**

- All data is statically allocated;
- ♦ Pointers are restricted to call-by-reference, **no pointer arithmetics**;
- ♦ Structured, recursion-free control flow.

#### **Semantics**

- ♦ The standard ISO C99 semantics:
  - arrays should not be accessed out of their bounds, . . .

restricted by:

- The machine semantics:
  - integer arithmetics is 2's complement,
  - floating point arithmetics is IEEE 754-1985,
  - int and float are 32-bit, short is 16-bit, ...

restricted by:

- ♦ The user's semantics:
  - integer arithmetics should not wrap-around,
  - some IEEE exceptions (invalid operation, overflow, division by zero) should not occur, . . .

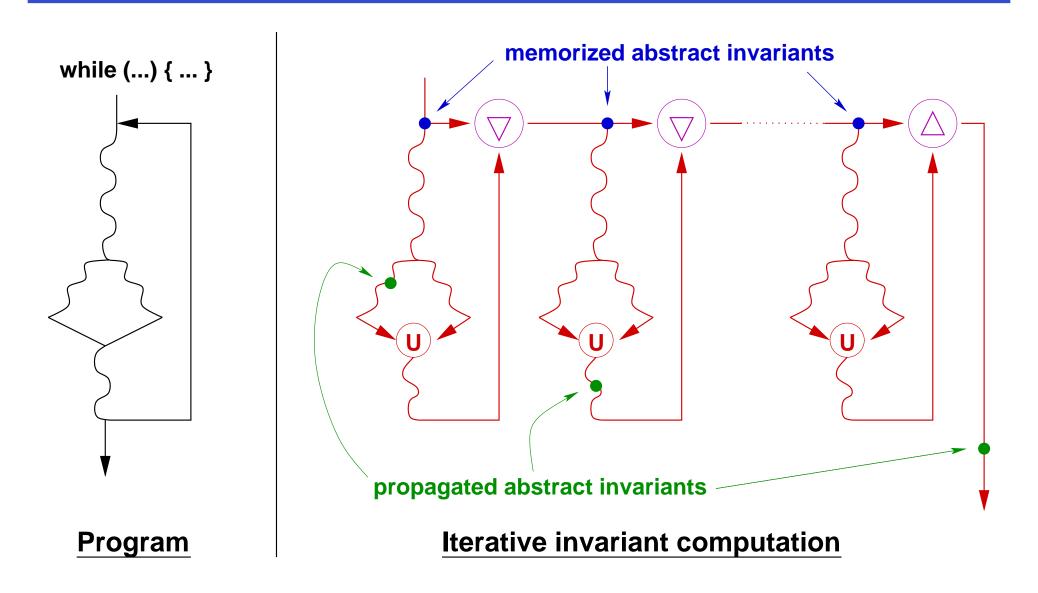
# Goal of the Program Static Analyzer

- Correctness verification
- Nothing can go wrong at execution:
  - no integer overflow or division by zero,
  - no exception, NaN, or  $\pm \infty$  generated by IEEE floating-point arithmetics,
  - no out of bounds array access,
  - no erroneous type conversion.
- ♦ The execution semantics on the machine never reaches an indetermination or an error case in the standard / machine / user semantics.

# Information about the Program Execution Automatically Inferred by the Analyzer

- ♦ The analyzer effectively computes a **finitely represented**, **compact** overapproximation of the **immense** reachable state space.
- ◆ The information is valid for any execution interacting with any possible environment (through undetermined volatiles).
- It is inferred **automatically** by abstract interpretation of the collecting semantics and convergence acceleration  $(\nabla, \Delta)$ .

# Iterations to Over-Approximate the Reachable States



# **Abstract Domains**

#### Choice of the Abstract Domains

#### **Abstract Domain:**

- Computer representation of a class of program properties;
- Transformers for propagation through expressions and commands;
- lacktriangle Primitives for convergence acceleration:  $\nabla$ ,  $\Delta$ .

#### **Composition of Abstract Domains:**

♦ Essentially approximate reduced product (conjunction with simplification).

#### **Design of Abstract Domains:**

- Know-how;
- Experimentation.

#### **Interval Abstract Domain**

- Classical domain [Cousot Cousot 76];
- Minimum information needed to check the correctness conditions;
- Not precise enough to express a useful inductive invariant (thousands of false alarms);
- ♦ ⇒ must be refined by:
  - combining with existing domains through reduced product,
  - designing new domains, until all false alarms are eliminated.

#### **Clock Abstract Domain**

#### **Code Sample:**

```
R = 0;
while (1) {
   if (I)
      { R = R+1; }
   else
      { R = 0; }
   T = (R>=n);
   wait_for_clock ();
}
```

- Output T is true iff the volatile input I has been true for the last n clock ticks.
- The clock ticks every s seconds for at most h hours, thus R is bounded.
- To prove that R cannot overflow, we must prove that R cannot exceed the elapsed clock ticks (impossible using only intervals).

#### **Solution:**

- We add a phantom variable clock in the concrete user semantics to track elapsed clock ticks.
- ◆ For each variable X, we abstract three intervals: X, X+clock, and X-clock.
- ♦ If X+clock or X-clock is bounded, so is X.

### Octagon Abstract Domain

#### **Code Sample:**

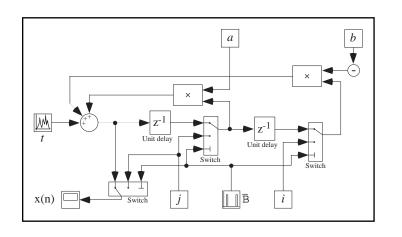
- At ★, the interval domain gives
   L ≤ max(max A, (max Z)+(max V)).
- In fact, we have  $L \leq A$ .
- To discover this, we must know at ★ that
   R = A-Z and R > V.

Solution: we need a numerical relational abstract domain.

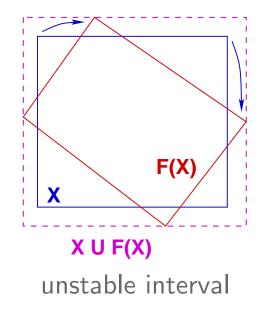
- ♦ The **octagon** abstract domain [Miné 03] is a good cost / precision trade-off.
- Invariants of the form  $\pm x \pm y \le c$ , with  $\mathcal{O}(\mathbb{N}^2)$  memory and  $\mathcal{O}(\mathbb{N}^3)$  time cost.
- Here, R = A-Z cannot be discovered, but we get  $L-Z \leq max R$  which is sufficient.
- We use many octagons on small packs of variables instead of a large one using all variables to cut costs.

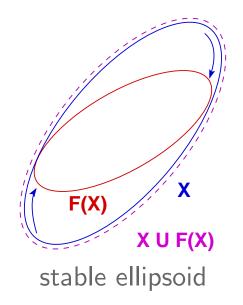
## Ellipsoid Abstract Domain

#### 2<sup>d</sup> Order Filter Sample:



- Computes  $X_n = \left\{ \begin{array}{l} \alpha X_{n-1} + \beta X_{n-2} + Y_n \\ I_n \end{array} \right.$
- The concrete computation is **bounded**, which must be proved in the abstract.
- There is no stable interval or octagon.
- The simplest stable surface is an **ellipsoid**.



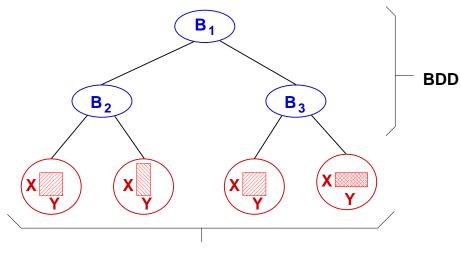


#### **Decision Tree Abstract Domain**

Synchronous reactive programs encode control flow in boolean variables.

#### **Code Sample:**

#### **Decision Tree:**



**Numerical abstract domains** 

There are too many booleans  $(4\ 000)$  to build one big tree so we:

- ♦ limit the BDD height to 3 (analysis parameter);
- use a syntactic criterion to select variables in the BDD and the numerical parts.

## Relational Domains on Floating-Point

#### **Problems:**

- ♦ Relational numerical abstract domains rely on a **perfect mathematical concrete semantics** (in  $\mathbb{R}$  or  $\mathbb{Q}$ ).
- lacktriangle Perfect arithmetics in  $\mathbb{R}$  or  $\mathbb{Q}$  is costly.
- ♦ IEEE 754-1985 floating-point concrete semantics incurs rounding.

#### **Solution:**

- lacktriangle Build an abstract mathematical semantics in  $\mathbb R$  that over-approximates the concrete floating-point semantics, including rounding.
- Implement the abstract domains on  $\mathbb{R}$  using floating-point numbers rounded in a sound way.

# Iteration Strategies for Fixpoint Approximation

# **Iteration Refinement: Loop Unrolling**

#### **Principle:**

♦ Semantically equivalent to:

```
while (B) { \mathbb{C} } \Longrightarrow if (B) { \mathbb{C} }; while (B) { \mathbb{C} }
```

- More precise in the abstract:
  - less concrete execution paths are merged in the abstract.

#### **Application:**

♦ Isolate the initialization phase in a loop (e.g. first iteration).

### **Iteration Refinement: Trace Partitioning**

#### **Principle:**

♦ Semantically equivalent to:

```
if (B) { C1 } else { C2 }; C3

↓
if (B) { C1; C3 } else { C2; C3 };
```

- More precise in the abstract:
  - concrete execution paths are merged later.

#### **Application:**

```
if (B)
    { X=0; Y=1; }
else
    { X=1; Y=0; }
R = 1 / (X-Y);
/ cannot result in a division by zero
```

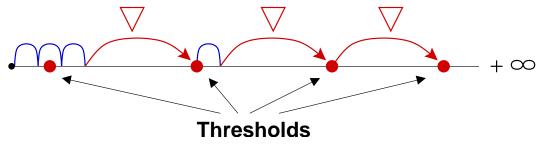
# Convergence Accelerator: Widening

#### **Principle:**

Brute-force widening:



Widening with thresholds:



#### **Examples:**

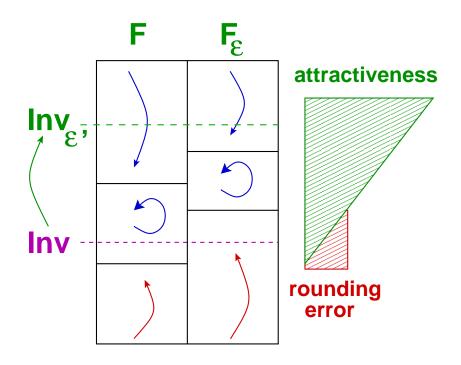
- ◆ 1., 10., 100., 1000., etc. for floating-point variables;
- maximal values of data types;
- syntactic program constants, etc.

# Fixpoint Stabilization for Floating-point

#### **Problem:**

- Mathematically, we look for an abstract invariant inv such that  $F(inv) \subseteq inv$ .
- ♦ Unfortunately, abstract computation uses floating-point and incurs rounding: maybe  $F_{\varepsilon}(inv) \nsubseteq inv!$

#### **Solution:**



- Widen inv to inv<sub> $\varepsilon'$ </sub> with the hope to jump into a stable zone of  $F_{\varepsilon}$ .
- Works if F has some attractiveness property that fights against rounding errors (otherwise iteration goes on).
- $\varepsilon'$  is an analysis parameter.

# Results

### **Example of Analysis Session**

```
Visualizator
      clocks
           trees octagons
                    filters
                           help
Search string: TRUC[0]
                            Next
                                 Previous
                                                 Goto line:
demo.c
  else
       @P = coef1 * X + TRUC[0].e * coef2 + TRUC[1].e * coeal
            TRUC[0].s * coef4 + TRUC[1].s * coef5;0
  *TRUC[1].e = TRUC[0].e;
  @TRUC[0].e = X:
  @TRUC[1].s = TRUC[0].s;
  atruc[0].s = P;a
} @
<u>void coffee machine explosion()</u>
info
/* Analyzer launched at 2003/ 6/ 2 11:45:43
     -103.23142654533073426 <= X-P <= 166.32563104533073783
  -67.325631045330709412 <= X+P <= 202.23142654533074847 }
 <clock in {0}, <MACHIN in {0}>;
  clock in {0},
  <TRUC[0].e in {15.5}, TRUC[0].s in [-20.7485, 20.7485], 2</pre>
TRUC[1].e in {15.5},
   TRUC[1].s in [-20.7485, 20.7485], X in \{15.5\}, P in [-2.7]
coffee machine explosion 55:3 (ellipse)
L43 C21 c894
```

#### Results

#### **♦** Efficient:

- tested on two **75 000** lines programs,
- 120 min and 37 min computation time on a 2.8GHz PC,
- 200 Mb memory usage.

#### Precise:

• 11 and 3 lines containing a warning.

#### **Exhaustive:**

full control and data coverage (unlike checking, testing, simulation).

#### **Conclusion**

#### Success story:

 we succeed where a commercial abstract interpretation-based static analysis tool failed

(because of prohibitive time and memory consumption and very large number of false alarms);

- ♦ **Usable** in practice for verification:
  - directly applicable to other similar programs by changing some analyzer parameters,
  - approach generalizable to other program families
     by including new abstract domains and specializing the iteration strategy.

(Work in progress: power-on self-test for a family of embedded systems.)