#### Abstract Interpretation-based Formal Software is replacing humans Verification of Complex Computer Systems - Paris métro line 12 accident<sup>1</sup>: the driver was Patrick Cousot going too fast Jerome C. Hunsaker Visiting Professor - New high-speed métro Department of Aeronautics and Astronautics line 14 (Météor): fully Massachusetts Institute of Technology automated, no operators cousot@mit.edu www.mit.edu/~cousot - Software is in all mission-École normale supérieure, Paris critical and safety-critical cousot@ens.fr www.di.ens.fr/~cousot industrial infrastructures Minta Martin Lecture, May 13<sup>th</sup>, 2005 <sup>1</sup> On August 30<sup>th</sup>, 2000, at the Notre-Dame-de-Lorette métro station in Paris, a car flipped over on its side and slid to a stop just a few feet from a train stopped on the opposite platform (24 injured). © P. Cousot 🕼 Minta Martin Lecture, MIT, May 13<sup>th</sup>, 2005 Minta Martin Lecture, MIT, May 13th, 2005 © P. Cousot — 3 — 11117 AERO Software is everywhere Why bugs in software? Minta Martin Lecture, MIT, May 13th, 2005 © P. Cousot Minta Martin Lecture, MIT, May 13<sup>th</sup>, 2005 © P. Cousot - 2 -AERQLSTRO AERQLSTRO





# Computers are finite

- Engineers use mathematics to deal with continuous, infinite structures (e.g.  $\mathbb{R}$ )
- Computers can only handle discrete, finite structures

### Putting big things into small containers

- Numbers are encoded onto a limited number of bits (binary digits)
- Some operations may overflow (e.g. integers: 32 bits × 32 bits = 64 bits)
- Using different number sizes (32, 64, ... bits) can also be the source of overflows



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#### The Ariane 5.01 maiden flight

- June 4<sup>th</sup>, 1996 was the maiden flight of Ariane 5









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### The Ariane 5.01 maiden flight failure

- June 4<sup>th</sup>, 1996 was the maiden flight of Ariane 5
- The launcher was detroyed after 40 seconds of flight because of a software overflow<sup>6</sup>



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<sup>6</sup> A 16 bit piece of code of Ariane 4 had been reused within the new 32 bit code for Ariane 5. This caused an uncaught overflow, making the launcher uncontrolable.

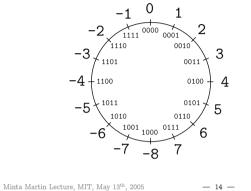
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(3) Computers go round

### Modular arithmetic...

- Todays, computers avoid integer overflows thanks to modular arithmetic
- Example: integer 2's complement encoding on 8 bits



#### ... can be contrary to common sense

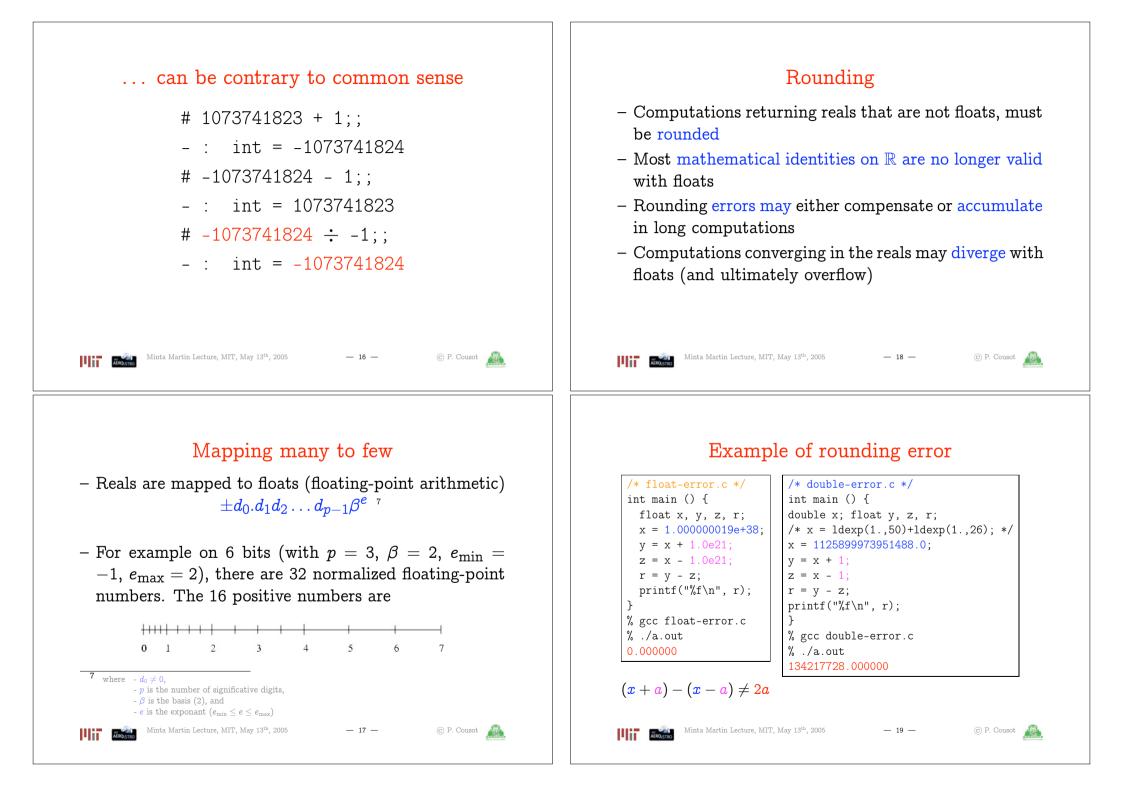
# 1073741823 + 1;; - : int = -1073741824 # -1073741824 - 1;; - : int = 1073741823 # -1073741824 ÷ -1;; - : int =

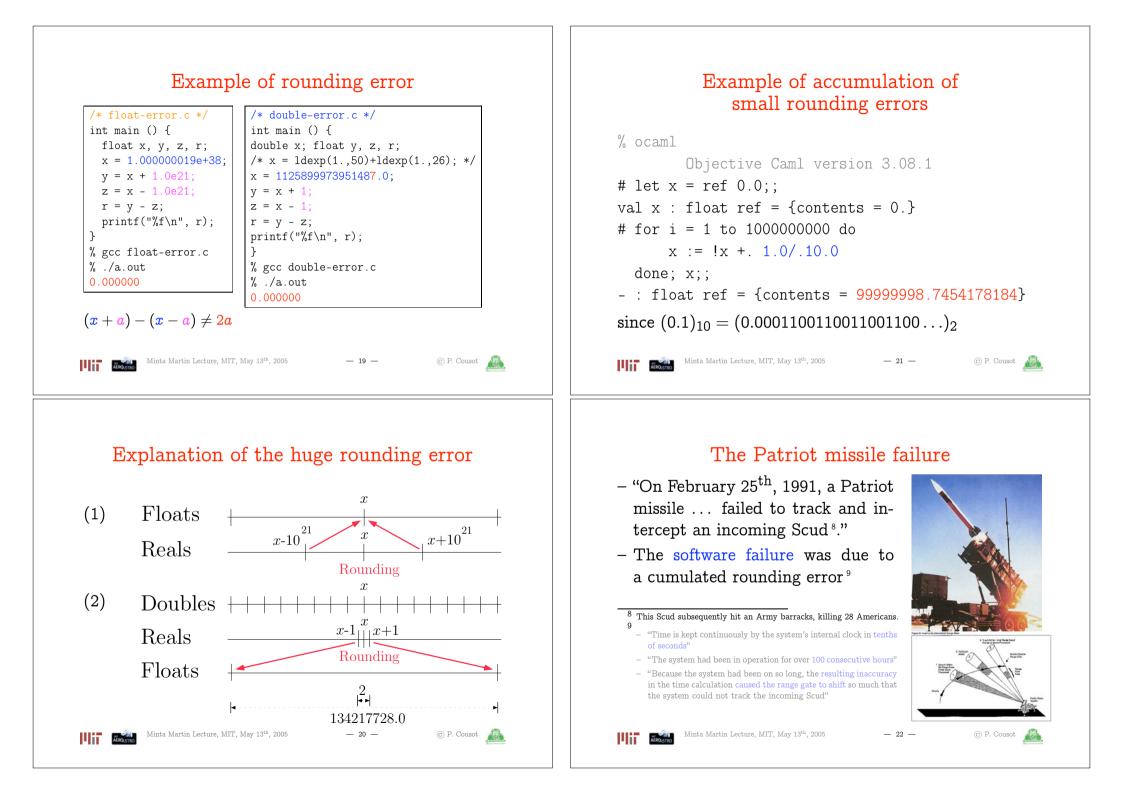




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#### Traditional software validation methods

- The law cannot enforce more than "best practice"
- Manual software validation methods (code reviews, simulations, tests, etc.) do not scale up
- The capacity of programmers/computer scientists remains essentially the same
- The size of software teams cannot grow significantly without severe efficiency losses

### Mathematics and computers can help

- Software behavior can be mathematically formalized  $\rightarrow$  semantics
- Computers can perform semantics-based program analyses to realize verification  $\rightarrow$  static analysis
  - but computers are finite so there are intrinsic limitations  $\rightarrow$  undecidability, complexity
  - which can only be handled by semantics approximations  $\rightarrow$  abstract interpretation

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# Abstract interpretation (1) very informally



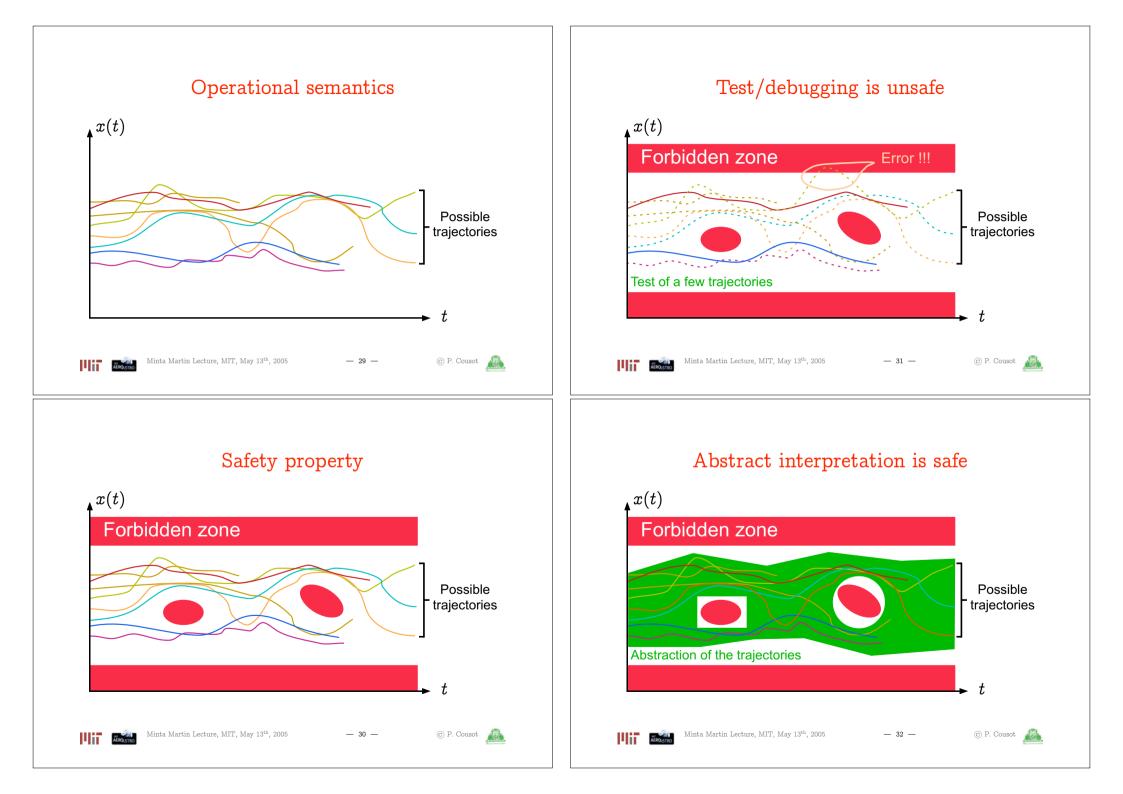
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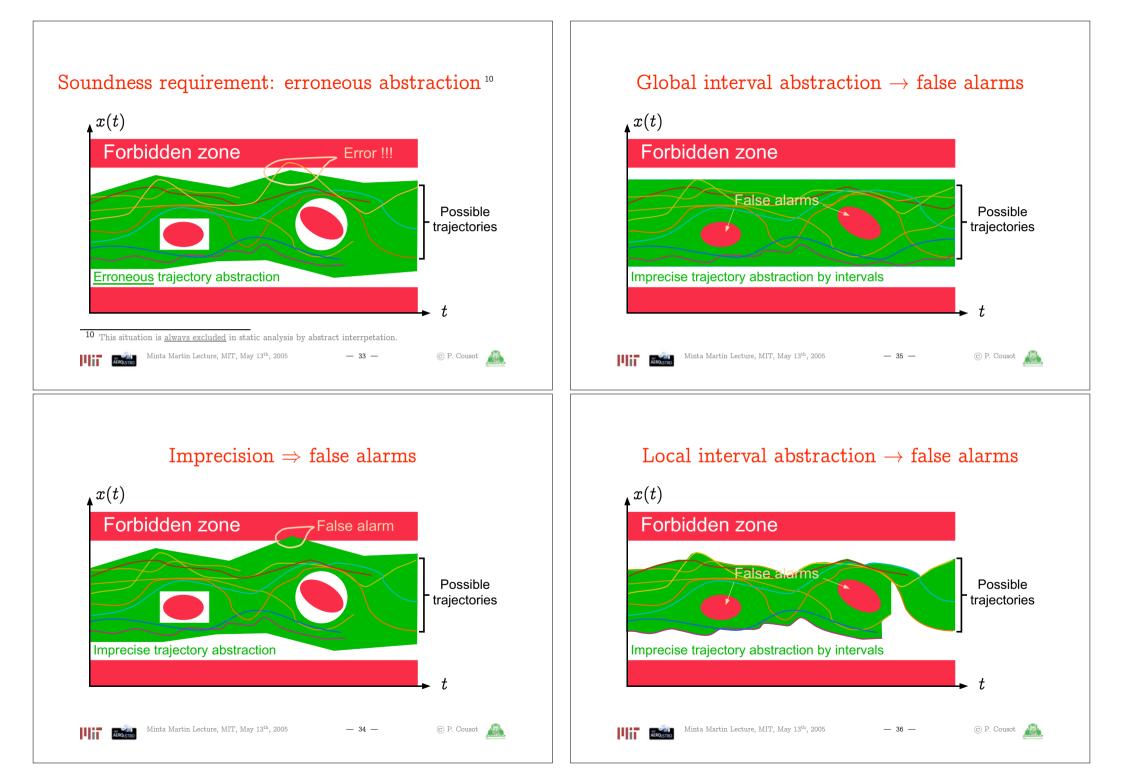
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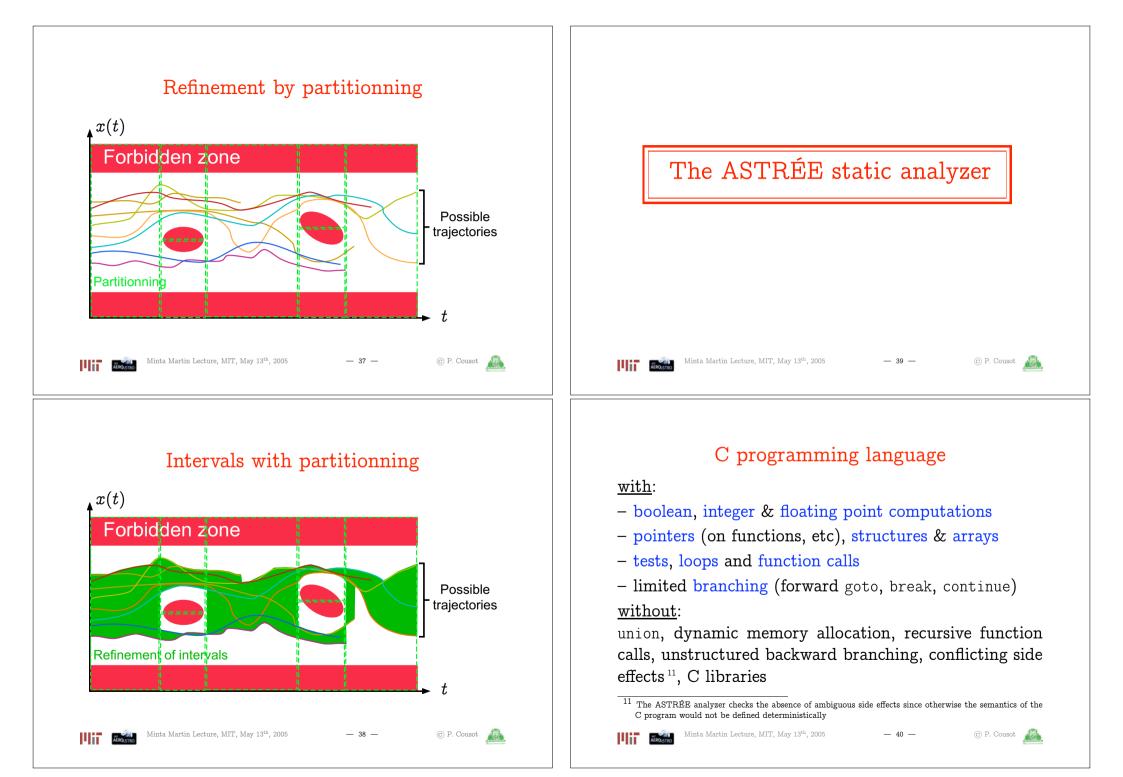


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### **Operational semantics**

- International norm of C (ISO/IEC 9899:1999)
- restricted by implementation-specific behaviors depending upon the machine and compiler <sup>12</sup>
- restricted by user-defined programming guidelines <sup>13</sup>
- restricted by program specific user requirements <sup>14</sup>
- restricted by a volatile environment as specified by a *trusted* configuration file.

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#### Implicit specification: absence of runtime errors

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- No violation of the norm of C  $^{\scriptscriptstyle 15}$
- No implementation-specific undefined behaviors <sup>16</sup>
- No violation of the programming guidelines <sup>17</sup>
- No violation of the programmer assertions  $^{\mbox{\tiny 18}}$
- <sup>15</sup> e.g. array index out of bounds

- $^{17}$  e.g. static variables are not be assumed to be initialized to 0
- $^{18}$  must all be statically verified



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# Application domain

- Safety critical embedded real-time synchronous software for non-linear control of very complex control/command systems<sup>19</sup>
- Strictly disciplined programming methodology
- 75% of the code is automatically generated from a high-level specification language  $^{\rm 20}$
- The external controlled system is unknown (but for the range of a few volatile variables, maximal duration,
  ... as specified in the configuration file)

<sup>19</sup> e.g. flight control software, engine control software
<sup>20</sup> e.g. S.A.O. (proprietary ), Simulink, SCADE

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## Verification of flight control software

 Primary flight control software of the Airbus A340 family and the A380 digital fly-by-wire systems





– Most critical software on board  $^{\scriptscriptstyle 21}$ 



 ASTRÉE verifies the absence of runtime errors without any false alarms!

 $^{21}$  controls automatically the airplane surface deflections and power settings, performs envelope protection,  $\ldots$  with precedence over the pilot

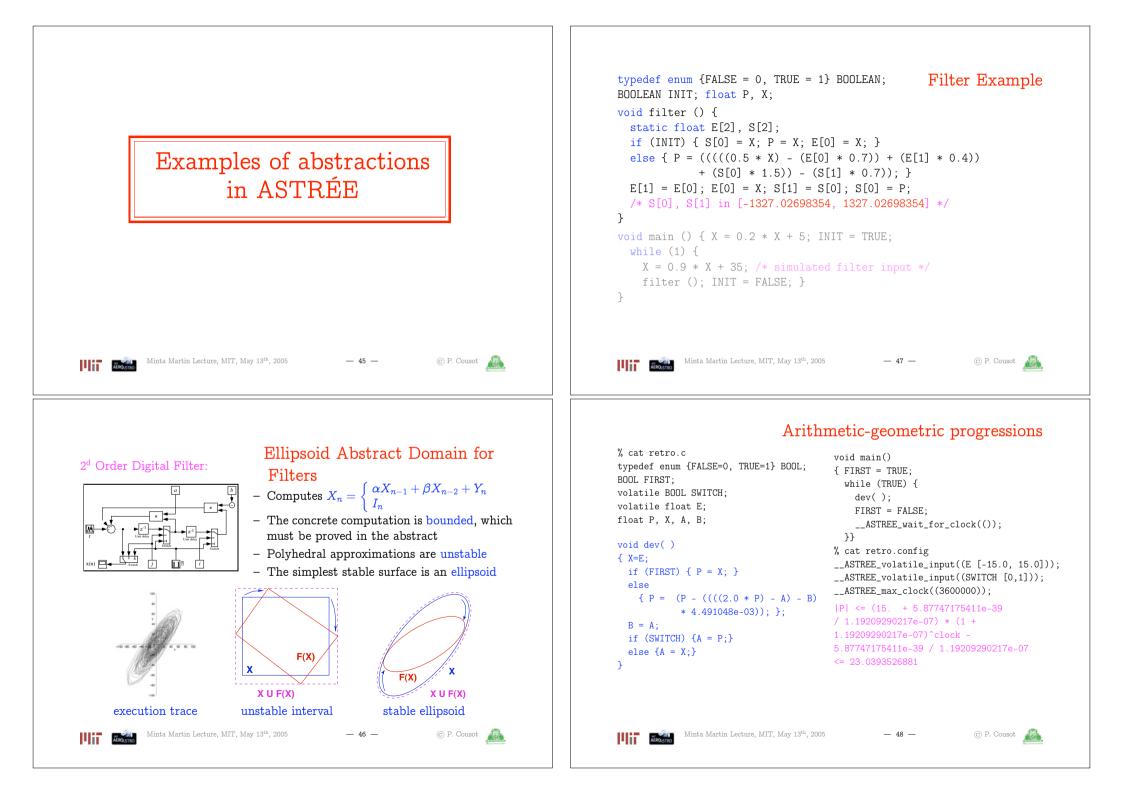
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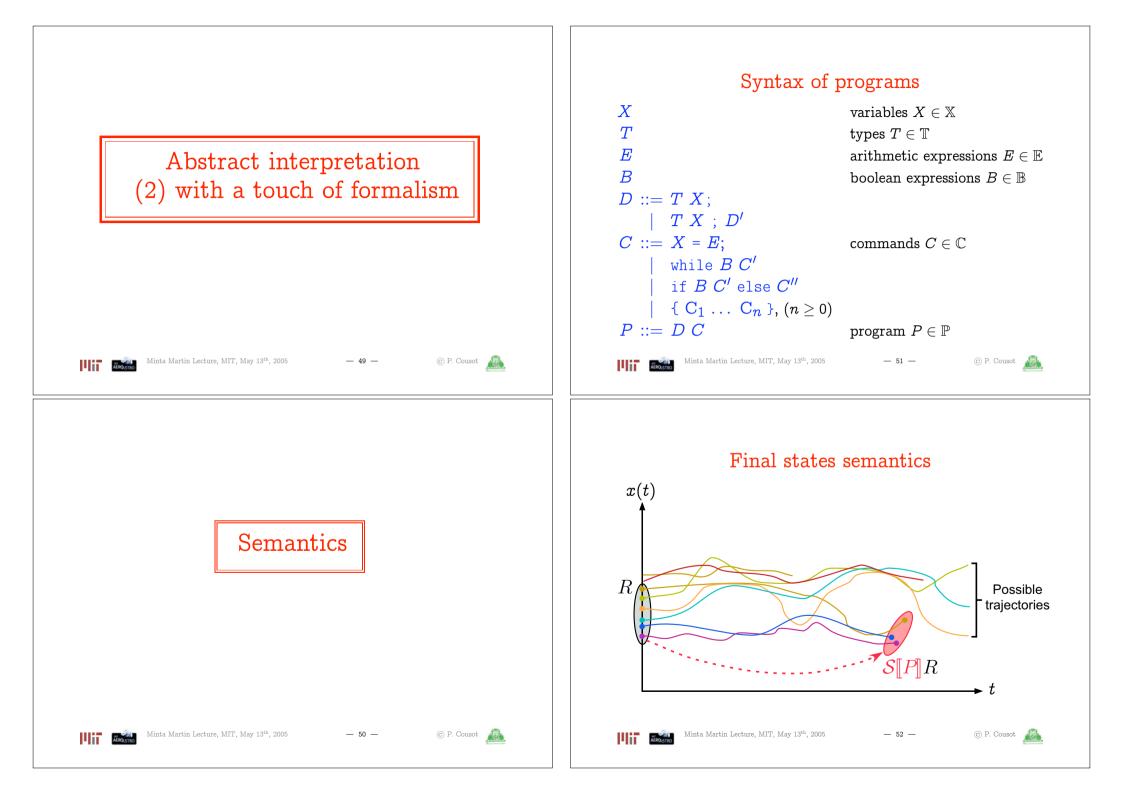


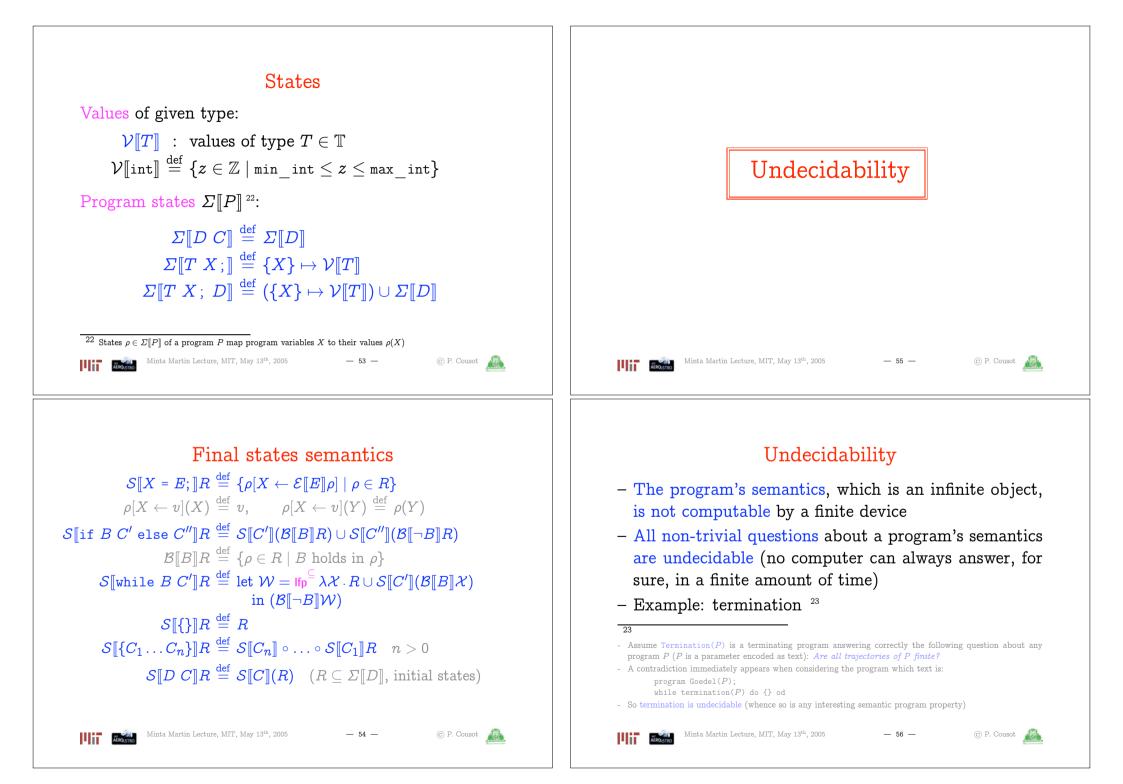
<sup>&</sup>lt;sup>12</sup> e.g. representation and size of integers, IEEE 754-1985 norm for floats and doubles

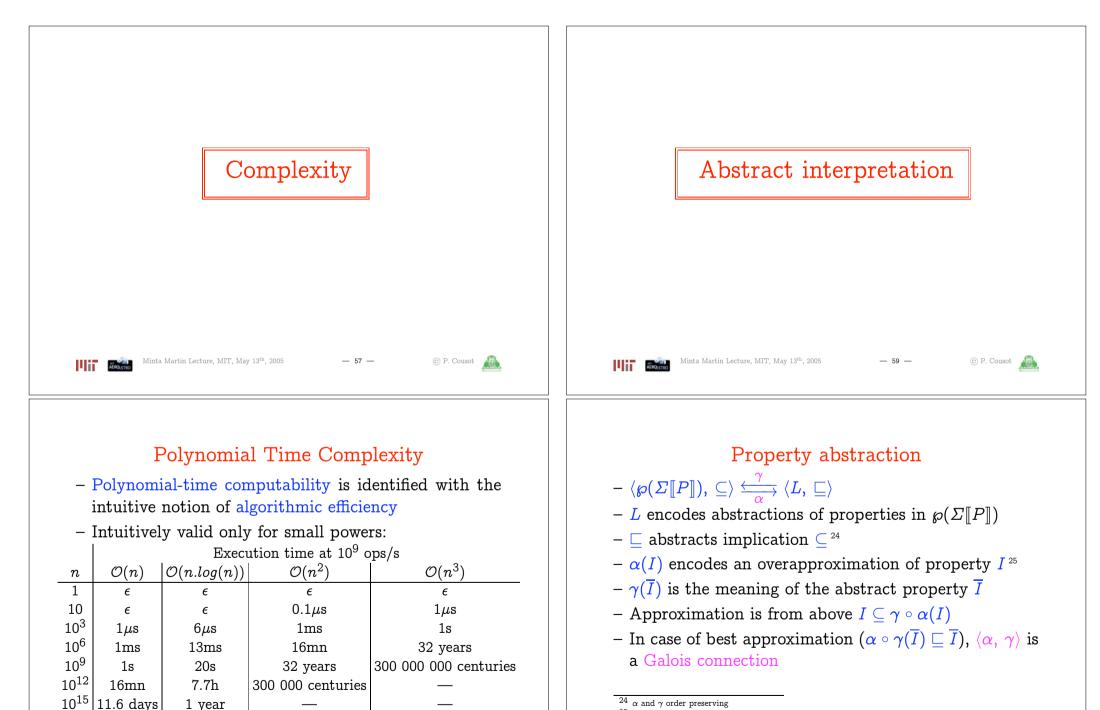
 $<sup>^{13}\,</sup>$  e.g. no modular arithmetic for signed integers, even though this might be the hardware choice  $^{14}\,$  e.g. assert

<sup>&</sup>lt;sup>16</sup> e.g. maximum short integer is 32767, no float overflow









11.6 davs

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1 year

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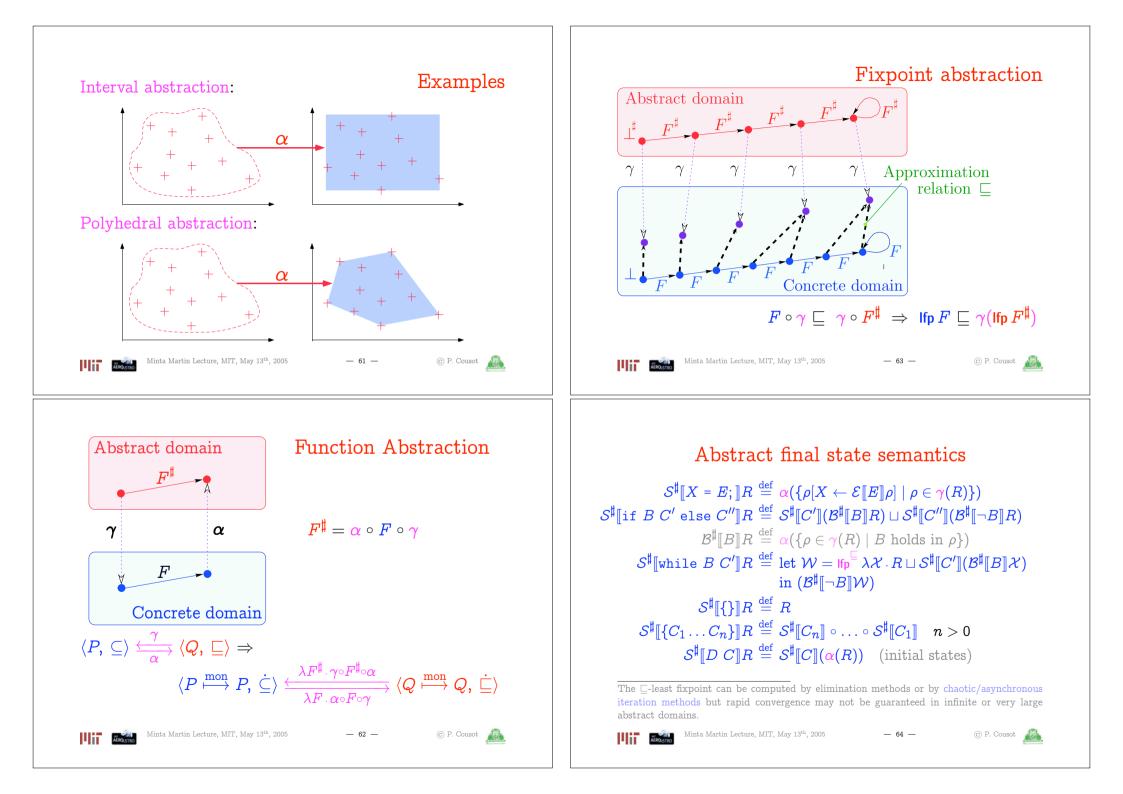
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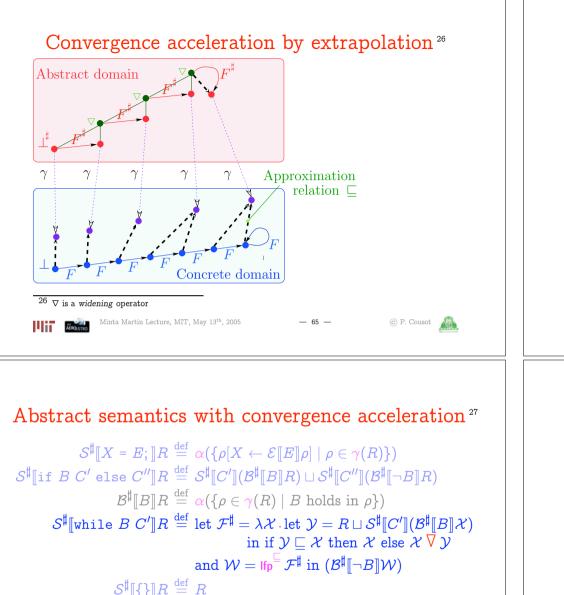
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 $^{24} \alpha$  and  $\gamma$  order preserving

 $^{25}$  e.g.  $\alpha$ (set of points) = polyhedron and  $\gamma$ (polyhedron) = set of interior points

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#### Applications of Abstract Interpretation

Abstract interpretation formalizes sound approximations as found everywhere in computer science:

- Syntax Analysis [TCS 290(1) 2002]
- Hierarchies of Semantics (including Proofs) [POPL'92], [TCS 277(1-2) 2002]
- Program Transformation [POPL '02]
- Typing & Type Inference [POPL '97]
- (Abstract) Model Checking [POPL '00]



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 $S^{\sharp}[\{C_1 \dots C_n\}] R \stackrel{\text{def}}{=} S^{\sharp}[[C_n]] \circ \dots \circ S^{\sharp}[[C_1]] \quad n > 0$ 

 $S^{\sharp} \llbracket D \ C \rrbracket R \stackrel{\text{def}}{=} S^{\sharp} \llbracket C \rrbracket (\alpha(R))$  (initial states)

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- Bisimulations [RT-ESOP '04]
- Software Watermarking [POPL '04]
- Code obfuscation [DPG-ICALP '05]
- Static Program Analysis [POPL '77], [POPL '78], [POPL '79] including
  - Dataflow Analysis [POPL '79], [POPL '00],
  - Set-based Analysis [FPCA '95],
  - Predicate Abstraction [Manna's festschrift '03], ...

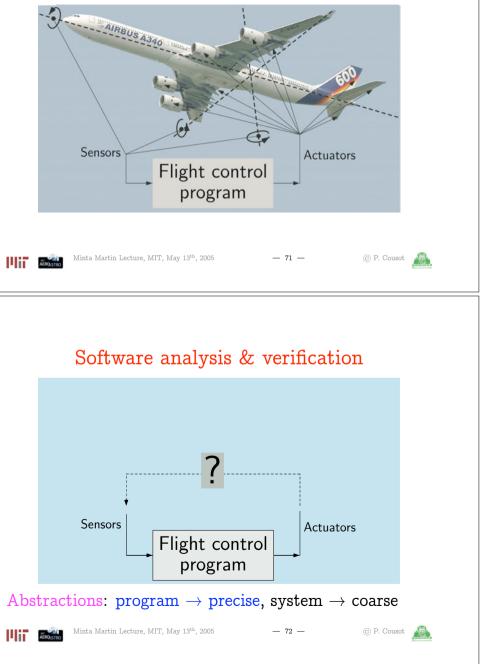
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- **WCET** [EMSOFT '01], ...

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Project while visiting MIT







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#### Grand challenge System analysis & verification Software verification - is the grand challenge for computer scientists and engineers in the next 15 years - will not be convincing without global system verification Sensors Actuators Flight control program Abstractions: program $\rightarrow$ precise, system $\rightarrow$ precise © P. Cousot Minta Martin Lecture, MIT, May 13<sup>th</sup>, 2005 — 73 — Minta Martin Lecture, MIT, May 13<sup>th</sup>, 2005 — 75 — © P. Cousot A AERQLSTRO AEROLSTRO Conclusion THE END My MIT web site is www.mit.edu/~cousot, where these slides are available My ENS web site is www.di.ens.fr/~cousot For more technical details, see the MIT course 16.399 on Abstract interpretation web.mit.edu/16.399/ © P. Cousot Minta Martin Lecture, MIT, May 13<sup>th</sup>, 2005 — 74 — © P. Cousot 👔 Minta Martin Lecture, MIT, May 13<sup>th</sup>, 2005 — 76 — AEROLSTRO AERQLSTRO

#### References

- [1] www.astree.ens.fr [3, 4, 5, 6, 7, 8, 9, 10]
- [2] P. Cousot. Méthodes itératives de construction et d'approximation de points fixes d'opérateurs monotones sur un treillis, analyse sémantique de programmes. Thèse d'État ès sciences mathématiques, Université scientifique et médicale de Grenoble, Grenoble, France, 21 March 1978.
- [3] B. Blanchet, P. Cousot, R. Cousot, J. Feret, L. Mauborgne, A. Miné, D. Monniaux, and X. Rival. Design and implementation of a special-purpose static program analyzer for safety-critical real-time embedded software. The Essence of Computation: Complexity, Analysis, Transformation. Essays Dedicated to Neil D. Jones, LNCS 2566, pp. 85-108. Springer, 2002.
- [4] B. Blanchet, P. Cousot, R. Cousot, J. Feret, L. Mauborgne, A. Miné, D. Monniaux, and X. Rival. A static analyzer for large safety-critical software. PLDI'03, San Diego, pp. 196-207, ACM Press, 2003.
- [POPL'77] P. Cousot and R. Cousot. Abstract interpretation: a unified lattice model for static analysis of programs by construction or approximation of fixpoints. In Conference Record of the Fourth Annual ACM SIGPLAN-SIGACT Symposium on Principles of Programming Languages, pages 238-252, Los Angeles, California, 1977. ACM Press, New York, NY, USA.
- [PACJM'79] P. Cousot and R. Cousot. Constructive versions of Tarski's fixed point theorems. Pacific Journal of Mathematics 82(1):43-57 (1979).
- [POPL'78] P. Cousot and N. Halbwachs. Automatic discovery of linear restraints among variables of a program. In Conference Record of the Fifth Annual ACM SIGPLAN-SIGACT Symposium on Principles of Programming Languages, pages 84–97, Tucson, Arizona, 1978. ACM Press, New York, NY, U.S.A.

Minta Martin Lecture, MIT, May 13<sup>th</sup>, 2005

— 77 —

- [POPL'79] P. Cousot and R. Cousot. Systematic design of program analysis frameworks. In Conference Record of the Sixth Annual ACM SIGPLAN-SIGACT Symposium on Principles of Programming Languages, pages 269-282, San Antonio, Texas, 1979. ACM Press, New York, NY, U.S.A.
- [POPL'92] P. Cousot and R. Cousot. Inductive Definitions, Semantics and Abstract Interpretation. In Conference Record of the 19<sup>th</sup> ACM SIGACT-SIGMOD-SIGART Symposium on Principles of Programming Languages, pages 83-94, Albuquerque, New Mexico, 1992. ACM Press, New York, U.S.A.
- [FPCA'95] P. Cousot and R. Cousot. Formal Language, Grammar and Set-Constraint-Based Program Analysis by Abstract Interpretation. In SIGPLAN/SIGARCH/WG2.8 7<sup>th</sup> Conference on Functional Programming and Computer Architecture, FPCA'95. La Jolla, California, U.S.A., pages 170–181. ACM Press, New York, U.S.A., 25-28 June 1995.
- [POPL'97] P. Cousot. Types as Abstract Interpretations. In Conference Record of the 24<sup>th</sup> ACM SIGACT-SIGMOD-SIGART Symposium on Principles of Programming Languages, pages 316–331, Paris, France, 1997. ACM Press, New York, U.S.A.
- [POPL'00] P. Cousot and R. Cousot. Temporal abstract interpretation. In Conference Record of the Twentyseventh Annual ACM SIGPLAN-SIGACT Symposium on Principles of Programming Languages, pages 12-25, Boston, Mass., January 2000. ACM Press, New York, NY.
- [POPL'02] P. Cousot and R. Cousot. Systematic Design of Program Transformation Frameworks by Abstract Interpretation. In Conference Record of the Twentyninth Annual ACM SIGPLAN-SIGACT Symposium on Principles of Programming Languages, pages 178–190, Portland, Oregon, January 2002. ACM Press, New York, NY.
- [TCS 277(1-2) 2002] P. Cousot. Constructive Design of a Hierarchy of Semantics of a Transition System by Abstract Interpretation. Theoretical Computer Science 277(1-2):47-103, 2002.



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- [TCS 290(1) 2002] P. Cousot and R. Cousot. Parsing as abstract interpretation of grammar semantics. Theoret. Comput. Sci., 290:531-544, 2003.
- [Manna's festschrift '03] P. Cousot. Verification by Abstract Interpretation. Proc. Int. Symp. on Verification Theory & Practice – Honoring Zohar Manna's 64th Birthday, N. Dershowitz (Ed.), Taormina, Italy, June 29 – July 4, 2003. Lecture Notes in Computer Science, vol. 2772, pp. 243–268. © Springer-Verlag, Berlin, Germany, 2003.
- [5] P. Cousot, R. Cousot, J. Feret, L. Mauborgne, A. Miné, D. Monniaux, and X. Rival. The ASTRÉE analyser. ESOP 2005, Edinburgh, LNCS 3444, pp. 21–30, Springer, 2005.
- [6] J. Feret. Static analysis of digital filters. ESOP'04, Barcelona, LNCS 2986, pp. 33-48, Springer, 2004.
- [7] J. Feret. The arithmetic-geometric progression abstract domain. In VMCAI'05, Paris, LNCS 3385, pp. 42-58, Springer, 2005.
- [8] Laurent Mauborgne & Xavier Rival. Trace Partitioning in Abstract Interpretation Based Static Analyzers. ESOP'05, Edinburgh, LNCS 3444, pp. 5-20, Springer, 2005.
- [9] A. Miné. A New Numerical Abstract Domain Based on Difference-Bound Matrices. PADO'2001, LNCS 2053, Springer, 2001, pp. 155–172.
- [10] A. Miné. Relational abstract domains for the detection of floating-point run-time errors. ESOP'04, Barcelona, LNCS 2986, pp. 3—17, Springer, 2004.
- [POPL'04] P. Cousot and R. Cousot. An Abstract Interpretation-Based Framework for Software Watermarking. In Conference Record of the Thirtyfirst Annual ACM SIGPLAN-SIGACT Symposium on Principles of Programming Languages, pages 173-185, Venice, Italy, January 14-16, 2004. ACM Press, New York, NY.



- [DPG-ICALP'05] M. Dalla Preda and R. Giacobazzi. Semantic-based Code Obfuscation by Abstract Interpretation. In Proc. 32nd Int. Colloquium on Automata, Languages and Programming (ICALP'05 - Track B). LNCS, 2005 Springer-Verlag. July 11-15, 2005, Lisboa, Portugal. To appear.
- [EMSOFT'01] C. Ferdinand, R. Heckmann, M. Langenbach, F. Martin, M. Schmidt, H. Theiling, S. Thesing, and R. Wilhelm. Reliable and precise WCET determination for a real-life processor. ESOP (2001), LNCS 2211, 469-485.
- [RT-ESOP '04] F. Ranzato and F. Tapparo. Strong Preservation as Completeness in Abstract Interpretation. ESOP 2004, Barcelona, Spain, March 29 - April 2, 2004, D.A. Schmidt (Ed), LNCS 2986, Springer, 2004, pp. 18-32.



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