In-Place Array Update in a Dataflow Synchronous Language

Ulysse Beaugnon, Albert Cohen, Marc Pouzet

École Normale Supérieure, INRIA
Synchronous Block Diagrams - SCADE\(^1\)

- DSL for modeling/implementing real-time control software
- Wires define streams of values
- All nodes progress at the same speed

\(^1\)http://www.esterel-technologies.com/
Dataflow Synchronous Languages - Lustre

\[
\text{node foo}(a:\ \text{int}) = (c:\ \text{int}) \{ \\
\quad c = b + 1 \quad (* \ c_t = b_t + 1 *) \\
\quad b = a + (0 \to \text{pre} \ b) \quad (* \ b_0 = a_0 *) \\
\quad (* \ b_t = a_t + b_{t-1} *) \\
\}
\]
Equation Ordering

```haskell
node foo(a: int) = (c: int) {
  c = b + 1       (* ct = bt + 1 *)
  b = a + (0 -> pre b) (* b0 = a0 *)
    (* bt = at + bt-1 *)
}
```

Implicit ordering of equations given by data dependencies

- Ordering in source code doesn’t matter

Allow feedback loops

- Every dependency loop must cross a delay
Compilation to efficient C code

```
node foo(a: int) = (c: int) {
    c = b + 1 (* c_t = b_t + 1 *)

    b = a + (0 -> pre b) (* b_0 = a_0 *)
    (* b_t = a_t + b_t-1 *)
}
```

Generated C code

```
// Computes a time step of foo
void foo_step(foo_state_t* state, int a, int* c) {
    int b = a + ((t == 0) ? 0 : state->b);
    *c = b + 1;

    state->b = b; // Update state
}
```
Functional Arrays

- Declare a new array and read from it
  
  ```
  e = d[1000]
  f = e[4]
  ```

- Define a new array from an old one
  
  ```
  g = e[3] <- 42
  ```
Functional Arrays

- Declare a new array and read from it
  \[
  e = d^{1000} \\
  f = e[4]
  \]

- Define a new array from an old one
  \[
  g = e[3] \leftarrow 42
  \]

Immutable arrays: no in-place update

```c
// Generated C code
int e[1000] = { d }; 
int f = e[4];

int g[1000];
memcpy(g, e, 1000* sizeof(int));
g[3] = 42;
```

Costly operation
Problem

How to avoid array copies ... 

... while keeping functional semantics?
Destructive Updates

Ensure no array is accessed after being updated

- Ensure arrays are updated only once
- Add dependencies from reads to writes
- Let the scheduling algorithm do the job

\[
\begin{align*}
(* & \text{ Consume a, reuse its memory for b } *) \\
b & = a[0] \leftarrow 0 \\
(* & \text{ Access a } *) \\
c & = a[0]
\end{align*}
\]

Copies are no longer needed

- Modifications of the original array cannot be observed
- Reuse the memory of the original array
Strengths of the Destructive Update Approach

Keeps pure functional semantics

Removes all implicit copies
- Reject programs that cannot be implemented without copies
- Explicit copies with the `copy` operator if needed
- No hidden performance cost

Direct mapping from source to generated code
- Only dependency analysis is more complex
- Required by certification authorities
Inter-Reaction Copies

What about \texttt{pre} ? Two solutions:

1. Insert a copy at every \texttt{pre}
2. \textbf{Handle inter-reaction aliasing}

\begin{align*}
\textbf{(} & \ast \ n_{t} \text{ consumes } a_{t} \ \textbf{*)} \\
b &= a[0] \leftarrow 0
\end{align*}

\begin{align*}
\textbf{(} & \ast \ n_{t+1} \text{ accesses } a_{t} \ \textbf{*)} \\
c &= (\texttt{pre } a)[0]
\end{align*}

c_{t+1} \text{ must be executed before } b_{t}

\textbf{Must } \texttt{retime} \textbf{ equations}

1. Compute \( c_{t} \text{ at time } t - 1 \)
Problems to Solve

Inter-Reaction Alias Analysis
- Avoid unnecessary explicit copies

Array Memory Management
- Arrays outlive a single time step

Modular Compilation
- Compile a node independently of its calling context
- Unknown aliasing between arguments
- Retiming imposed by feedback loops
- The alternative is inlining: exponential code size
Modular Compilation - Unknown Aliasing

```c
node f (A, B: int [8])
    = (c: int) {
        D = B[0] <- 0
    }

(* Without aliasing *)
x = f (A’, B’)

(* With aliasing *)
y = f (A’, A’)
```

Is there a dependency from Read A to Write B?
node f(A, B: int[8])
    = (c: int) {
      D = B[0] <- 0
    }

(* Without aliasing *)
x = f(A', B')

(* With aliasing *)
y = f(A', A')

Expose reads and writes to the calling context
**Modular Compilation - Unknown Aliasing**

```plaintext
node f(A, B: int[8])
    = (c: int) {
        D = B[0] <- 0
    }

(* Without aliasing *)

x = f(A', B')

(* With aliasing *)

y = f(A', A')
```

The context adds feedback loops if needed.
Dependencies are of the form:

$$\forall t \in \mathbb{N} : a_t \text{ depends on } b_{t-w} \quad \text{with } w \in \mathbb{Z} \text{ constant.}$$

Dependencies represented by a weighted graph:

```plaintext
node foo(a, b: int) = (c: int) {
  (* c_t = a_t + b_{t-1} *)
  c = 0 -> a + pre b
}
```
How can we schedule this node?
\{a_{t-1}, b_t\} \text{ before } \{d_t, e_t\}
Modular Compilation - Feedback Loops

\{d_t, e_t\} before \{a_{t-1}, b_t\}
Modular Compilation - Feedback Loops

- $a_{t-1}$ and $b_t$ can be executed atomically
- $c_t$ can be executed atomically
- $d_t$ and $e_t$ can be executed atomically
Grayboxing: Partitioning into atomic subnodes

- Subnodes are compiled independently
- The calling context orders subnodes
- Avoid a full inlining
Grayboxing Definition

A grayboxing is given by:

- A partitioning $X^0, \ldots, X^{k-1}$ of equations in atomic sub-nodes
- A retiming function for each sub-node $r_i : X_i \rightarrow \mathbb{Z}$
  - $a_t$ is computed at the reaction $t + r(a)$
- A dependency relation $X \xrightarrow{w} Y$ on sub-nodes
  - $X \xrightarrow{w} Y \implies Y_t \text{ depends on } X_{t-w}$

A Grayboxing must:

- Respect dependencies between equations
- Not reject any calling context

Extension of [Pouzet and Raymond 2009] for retiming
Finding a Minimal Grayboxing

**Goal:** Minimize the Number of Partitions

**Optimal Solution:** NP-Complete
- Encode the problem for an SMT solver

**Heuristic:** Find a Good-Enough Partitioning
- Optimal on inputs and outputs
- Based on an existing heuristic that doesn’t handle retiming

See the paper for more information
Conclusion

In-place updates in a synchronous dataflow language

- Avoid copy operations
- Keeps pure functional semantics
- No hidden performance cost
- No expressivity loss

Relies on scheduling constraints

- Ensure no array is accessed after being written to
- Leverages the existing scheduling algorithms
Destructive Updates for Synchronous Dataflow Languages

With copying \texttt{pre}

\begin{itemize}
  \item Minimal alteration of the compilation process
  \item Arrays copied at the end of iterations
\end{itemize}

With inter-iteration aliasing

\begin{itemize}
  \item \texttt{pre} creates aliasing instead of copying
  \item Need for retiming created by iter-iteration aliasing
  \item Context-aware scheduling and retiming for more genericity
  \item Modular compilation enabled by the grayboxing technique
\end{itemize}