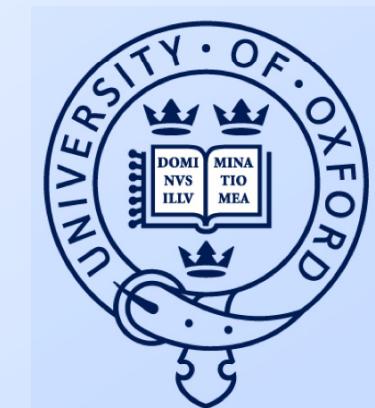
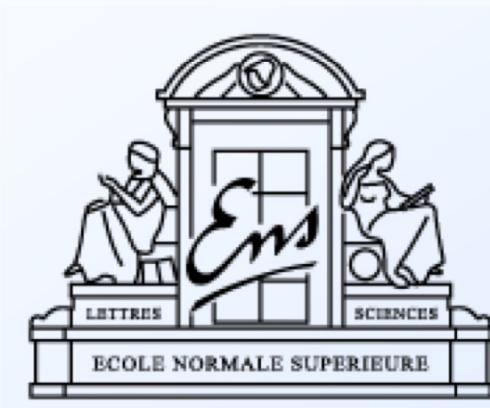
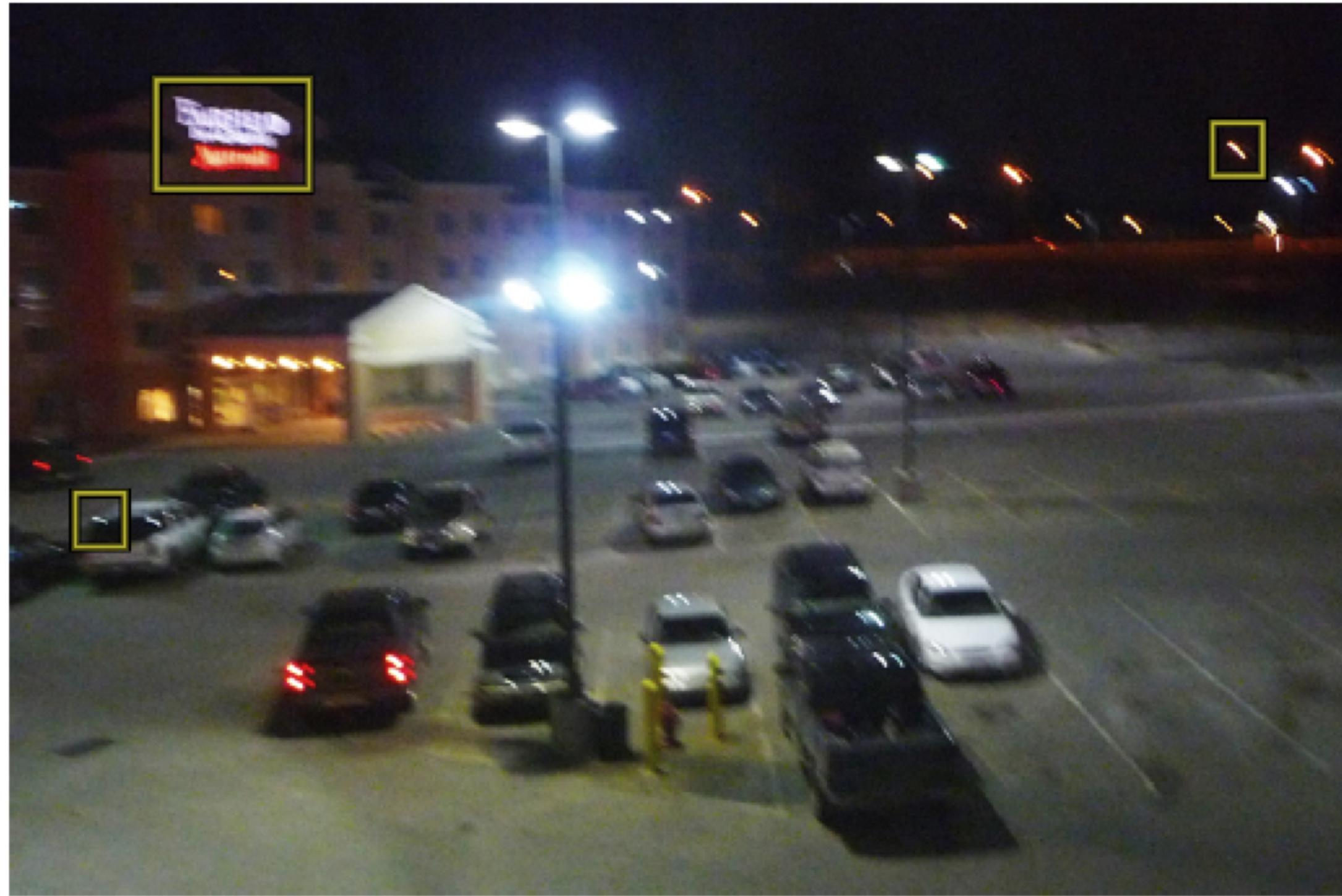


Non-uniform Deblurring for Shaken Images

Oliver Whyte Josef Sivic Andrew Zisserman Jean Ponce

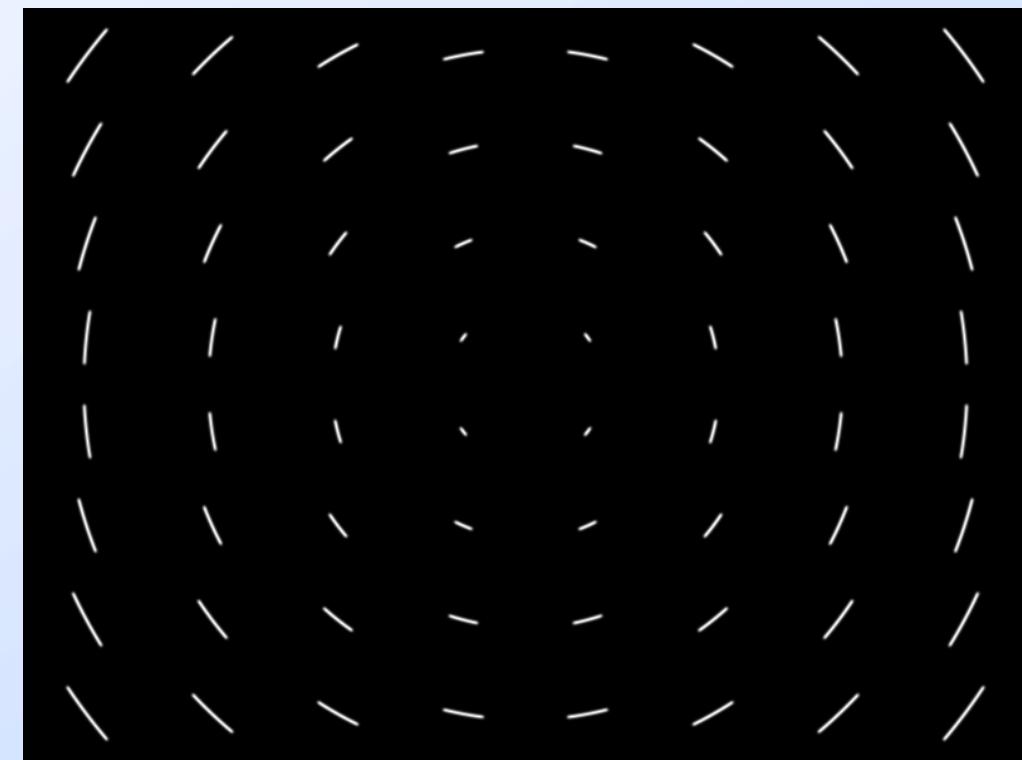
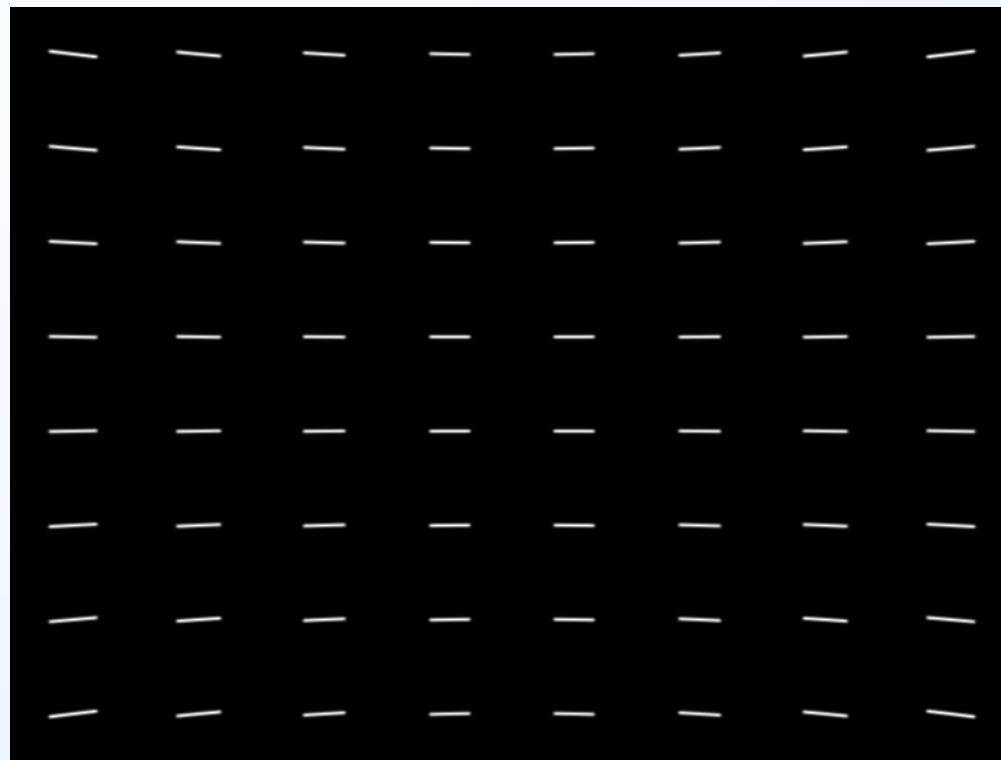


Non-uniform blur due to camera shake



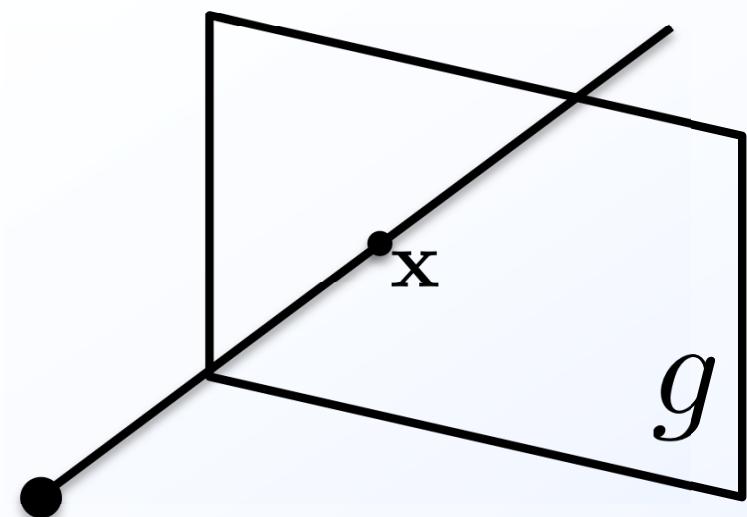
Geometric model

- Camera shake caused by 3D rotation of camera
- Camera rotations induce homographies:

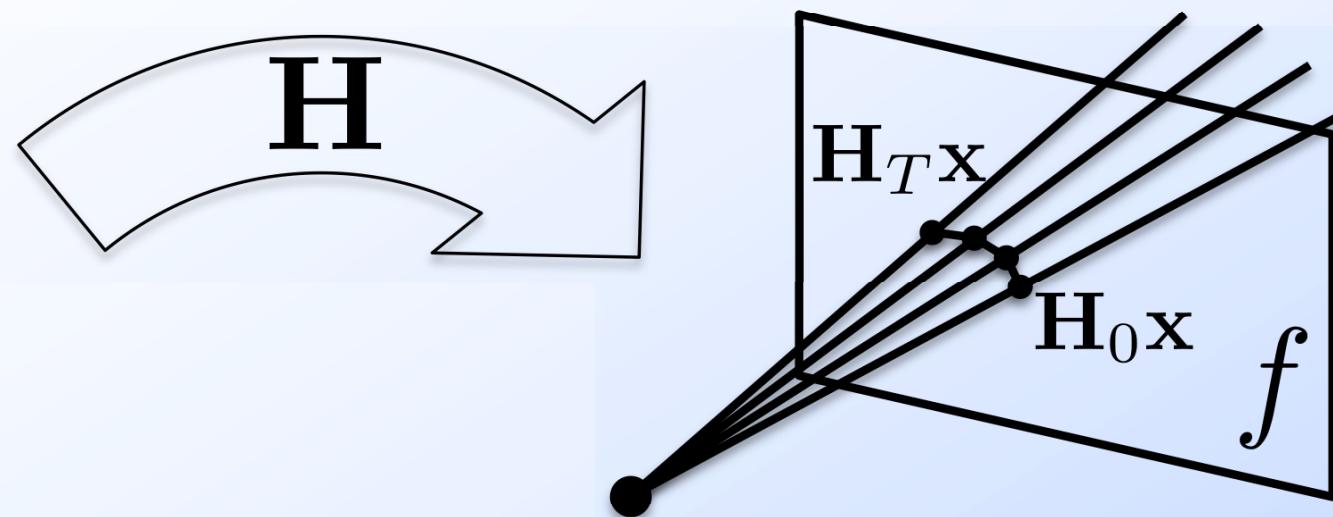


Blur model

Blurry image is a sum of many projectively-transformed versions of (latent) sharp image.



Pixel in blurry image



Sequence of pixels in sharp image

$$g(\mathbf{x}) = \int_0^T f(\mathbf{H}_t \mathbf{x}) dt + \varepsilon$$

blurry image

sharp image

homography at time instant t

noise

Blur model – continuous

- Blurry image has no temporal information
- Replace temporal integral with a weighted integral over all camera orientations

$$g(\mathbf{x}) = \int f(\mathbf{H}_\theta \mathbf{x}) w(\theta) d\theta + \varepsilon$$

homography induced at camera orientation θ

weight function (inversely proportional to rotational velocity)

integrate over camera orientations

The diagram illustrates the components of the blur model equation. It shows the equation $g(\mathbf{x}) = \int f(\mathbf{H}_\theta \mathbf{x}) w(\theta) d\theta + \varepsilon$ with three light blue rectangular boxes highlighting parts of the expression. A line points from the first box to the text 'homography induced at camera orientation θ '. Another line points from the second box to the text 'weight function (inversely proportional to rotational velocity)'. A third line points from the third box to the text 'integrate over camera orientations'.

Blur model – discrete

- Continuous:

$$g(\mathbf{x}) = \int f(\mathbf{H}_\theta \mathbf{x}) w(\theta) d\theta + \varepsilon$$

- Discrete:

$$g_i = \sum_k \left(\underbrace{\sum_j C_{ijk} f_j}_{\text{interpolation of the point } \mathbf{H}_k \mathbf{x}_i \text{ in the sharp image}} \right) w_k + \varepsilon$$

blury pixel with homogeneous coordinate vector \mathbf{x}_i

weight for the k^{th} homography

Blur model – comparison

Convolution
(uniform)

$$g_i = \sum_{u,v} f_{x_i-u, y_i-v} w_{u,v} + \varepsilon$$

Weighted sum of **translated**
copies of sharp image

Our model
(non-uniform)

$$g_i = \sum_k \left(\sum_j C_{ijk} f_j \right) w_k + \varepsilon$$

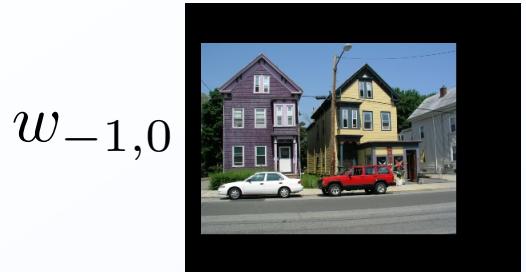
Weighted sum of **transformed**
copies of sharp image

- Both are bilinear in blur kernel and sharp image
- We can use our model with existing algorithms

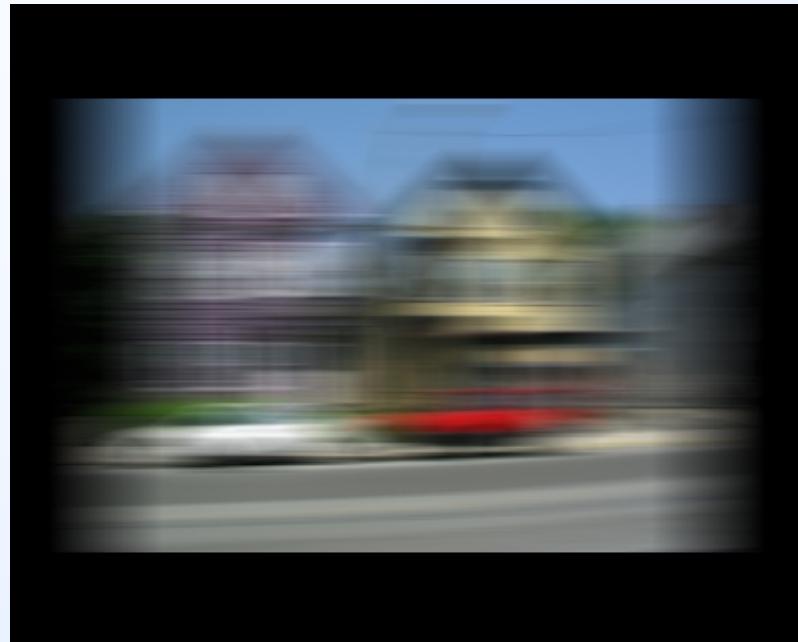
Blur model – comparison

Convolution
(uniform)

$$g_i = \sum_{u,v} f_{x_i-u, y_i-v} w_{u,v} + \varepsilon$$



$w_{-1,0}$



$+ w_{0,0}$



=



$+ w_{1,0}$

Our model
(non-uniform)

$$g_i = \sum_k \left(\sum_j C_{ijk} f_j \right) w_k + \varepsilon$$



w_0



$+ w_1$



$+ w_2$



Application I: Blind deblurring

- Estimate sharp image and kernel from a single blurry image

$$g_i = \sum_k \left(\sum_j C_{ijk} f_j \right) w_k + \varepsilon$$

\ / \ /
observed latent variables we
 want to recover

- Ill-posed problem – requires priors / regularisation on f & w
- We apply our non-uniform model in the algorithm of Fergus *et al.*, SIGGRAPH '06

Blind deblurring (Fergus *et al.*, 2006)

- Approximate posterior with a simpler factorised distribution (Miskin & MacKay, 2000)

$$p(\mathbf{f}, \mathbf{w} | \mathbf{g}) \propto p(\mathbf{g} | \mathbf{f}, \mathbf{w}) p(\mathbf{f}) p(\mathbf{w})$$

- $p(\mathbf{g} | \mathbf{f}, \mathbf{w})$: blur model + Gaussian noise model
- $p(\mathbf{f})$: sparse gradients (mixture of Gaussians)
- $p(\mathbf{w})$: sparse kernel (mixture of Laplacians)

Blind deblurring (Fergus *et al.*, 2006)

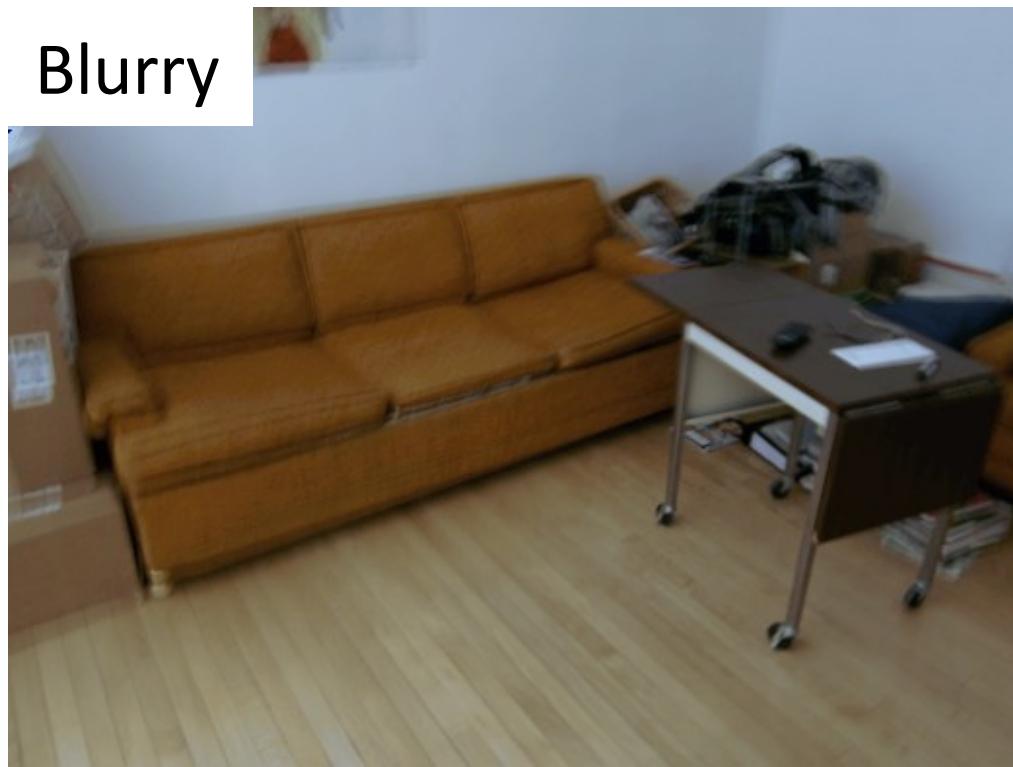
- Approximate posterior with a simpler factorised distribution (Miskin & MacKay, 2000)

$$p(\mathbf{f}, \mathbf{w} | \mathbf{g}) \approx \prod_j q(f_j) \prod_k q(w_k)$$

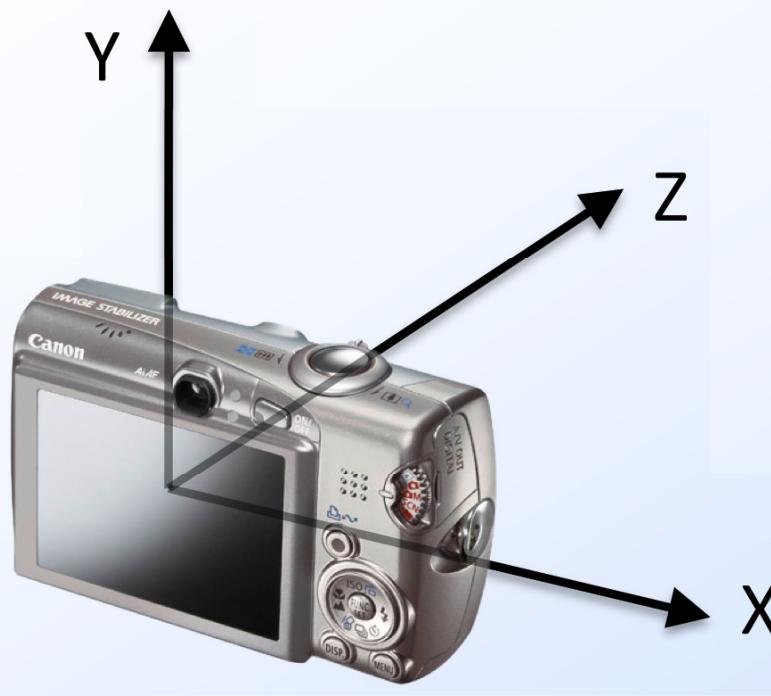
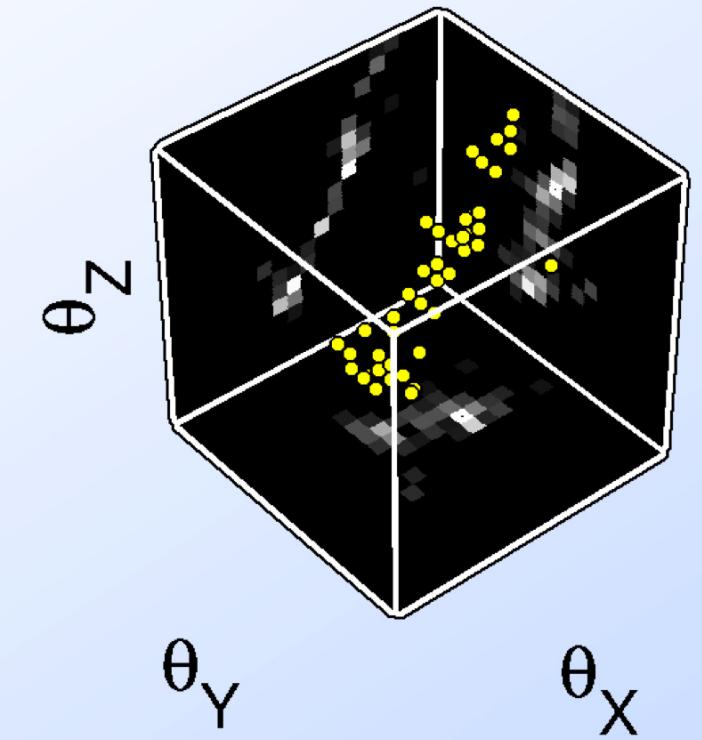
- Learn parameters of q distributions by minimising KL divergence with true posterior
- Estimate \mathbf{w} by (trivial) marginalisation
- Deblur with Richardson-Lucy algorithm

Blind deblurring – results

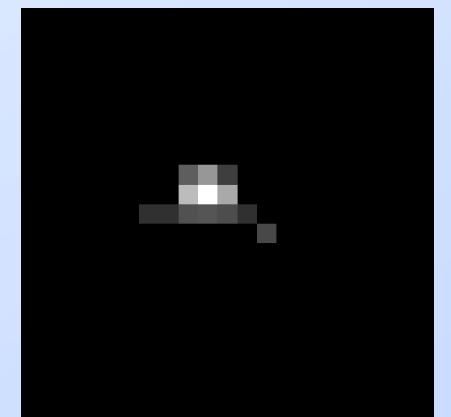
Blurry



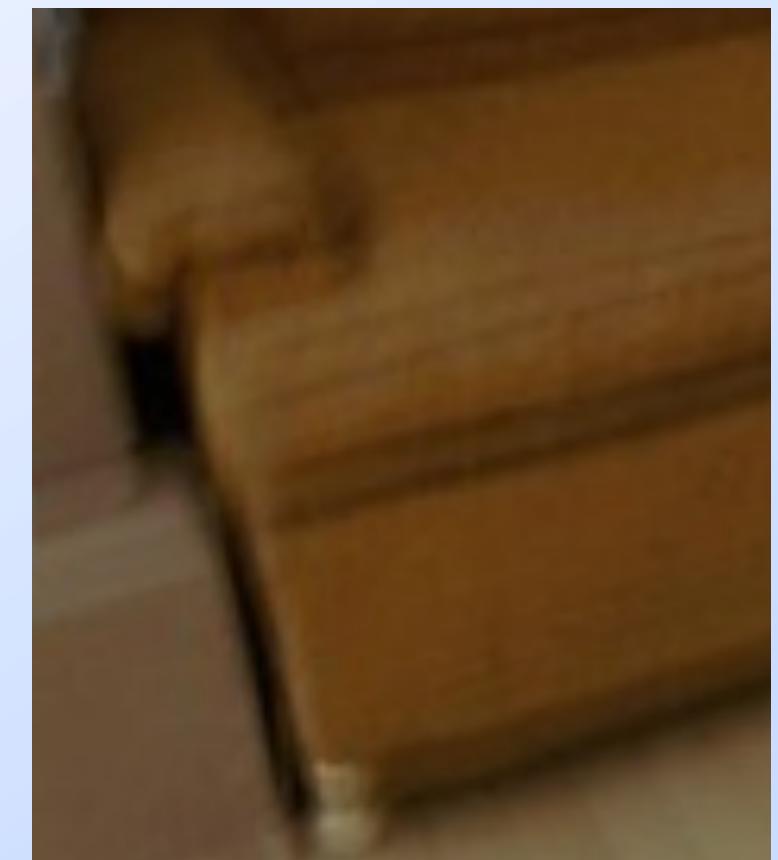
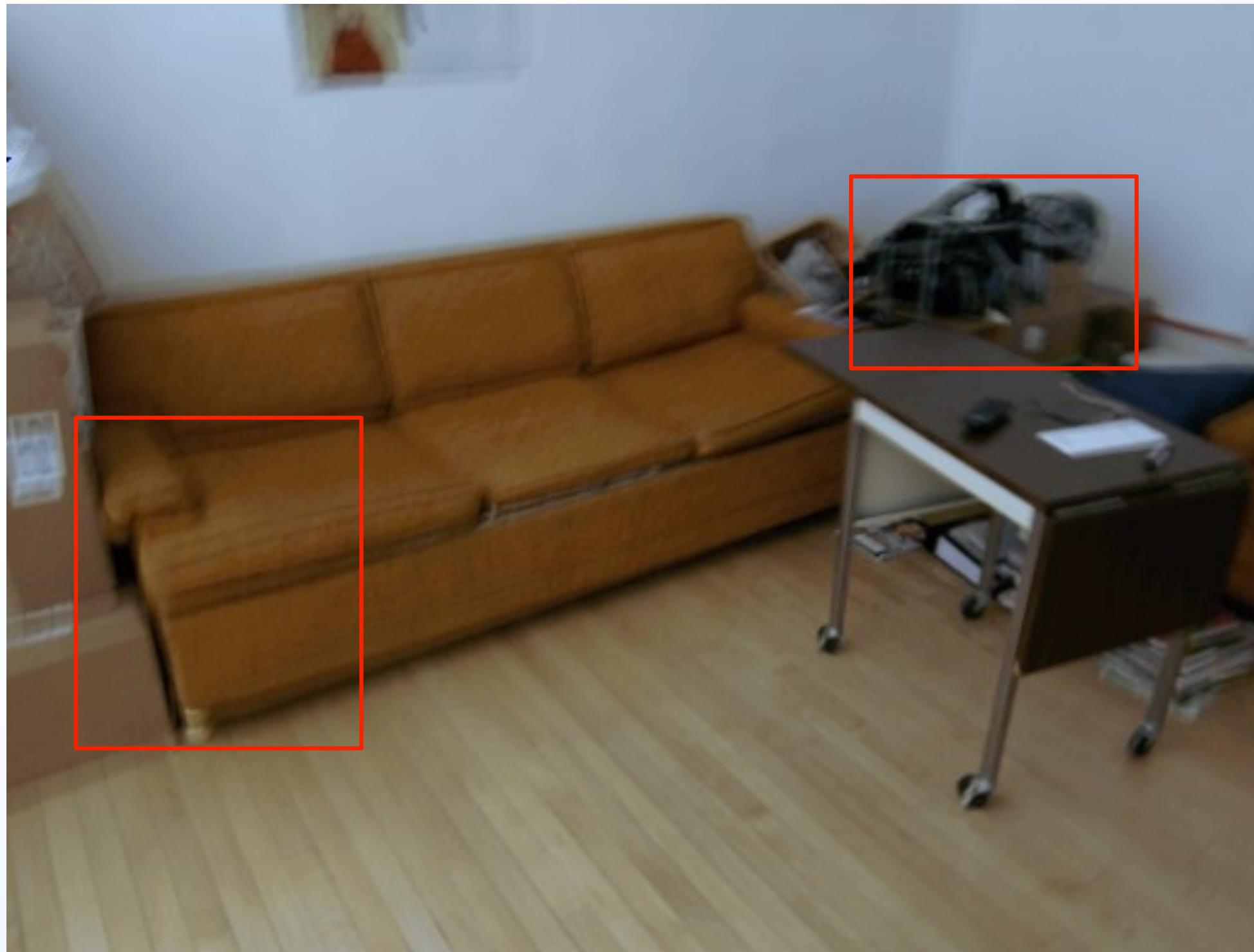
Our result



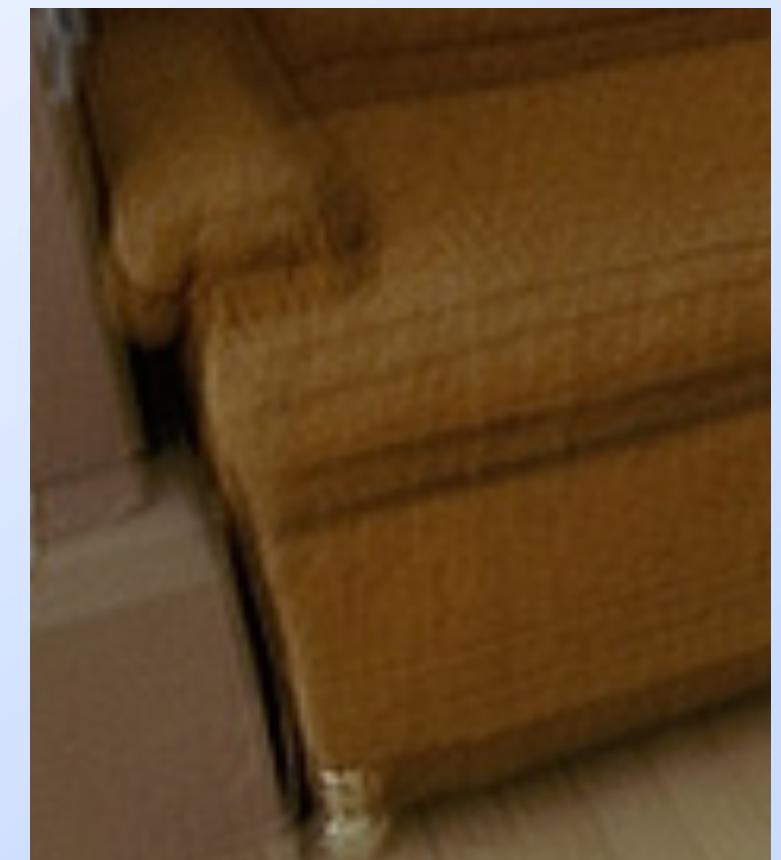
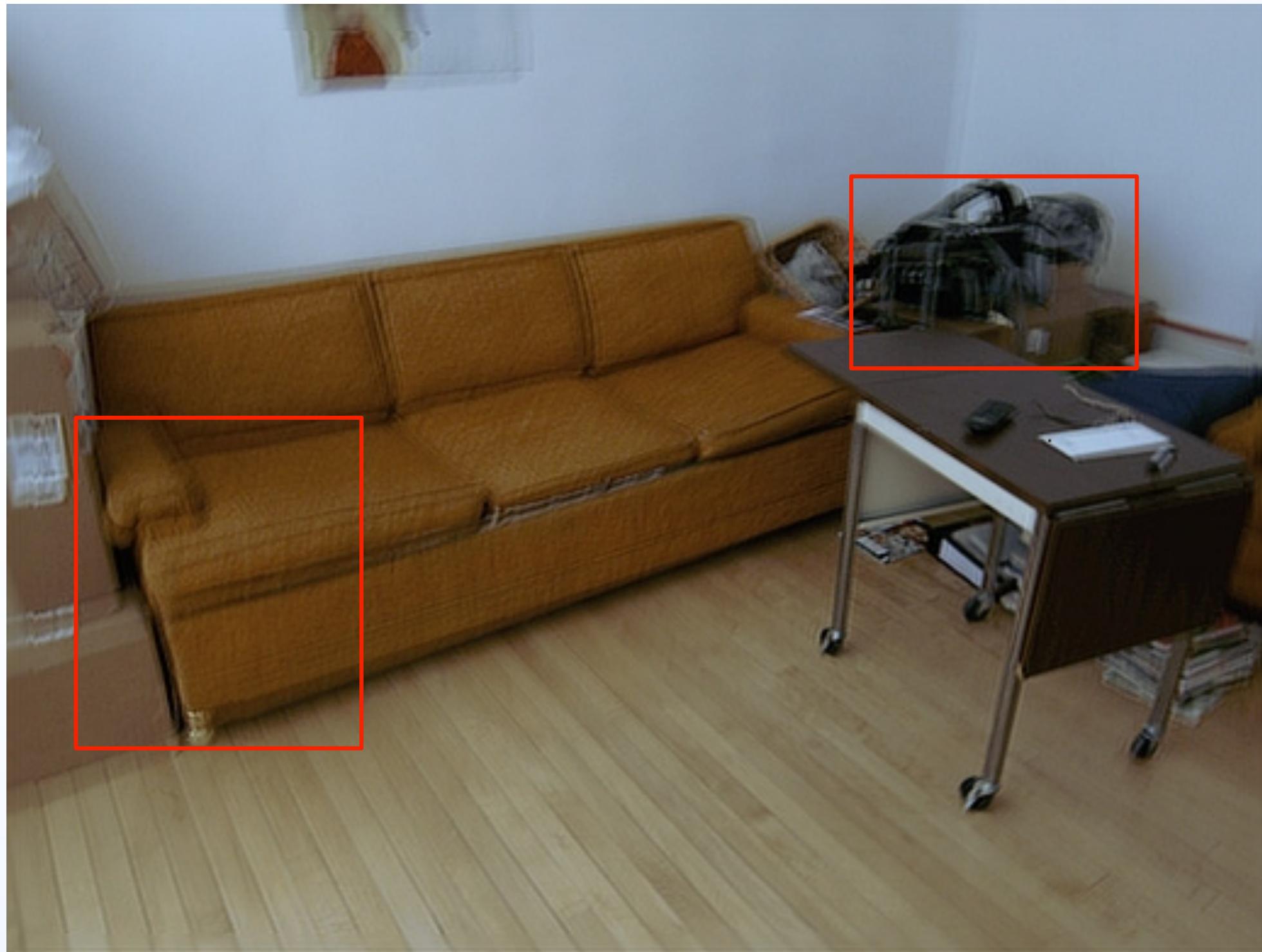
Fergus *et al.*



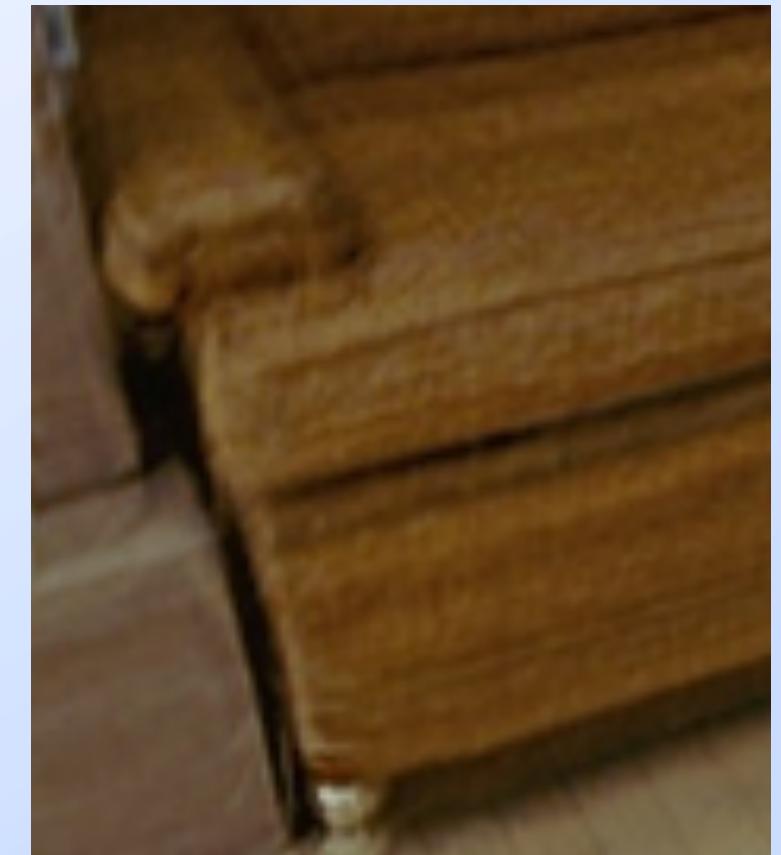
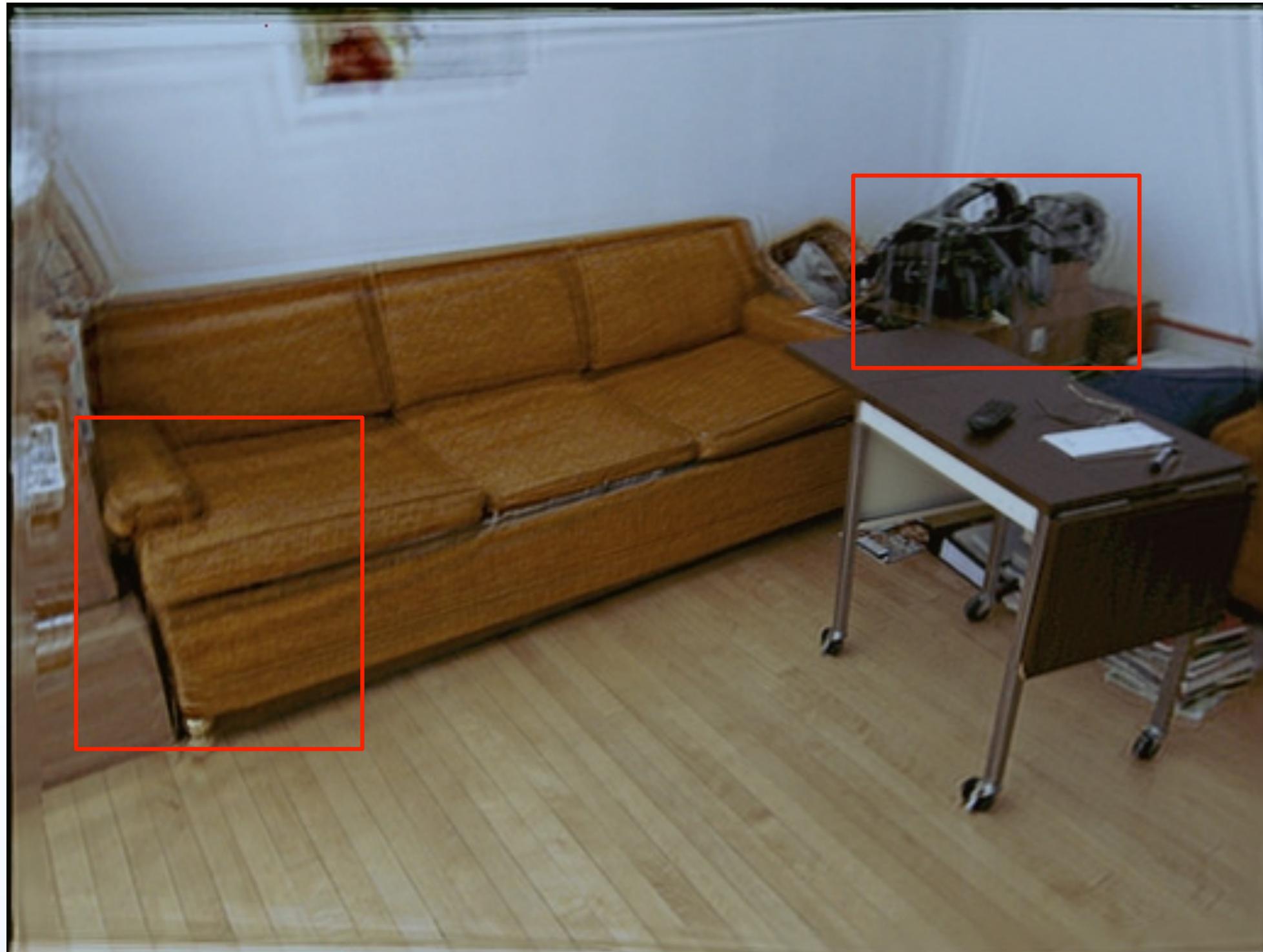
Blind deblurring – blurry image



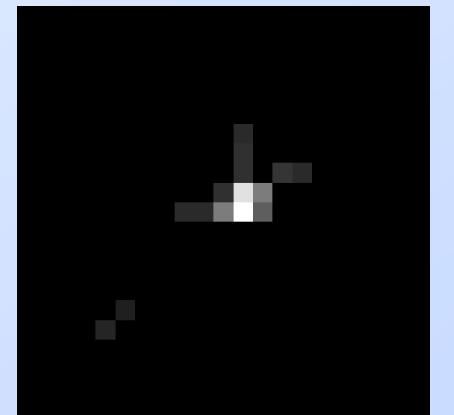
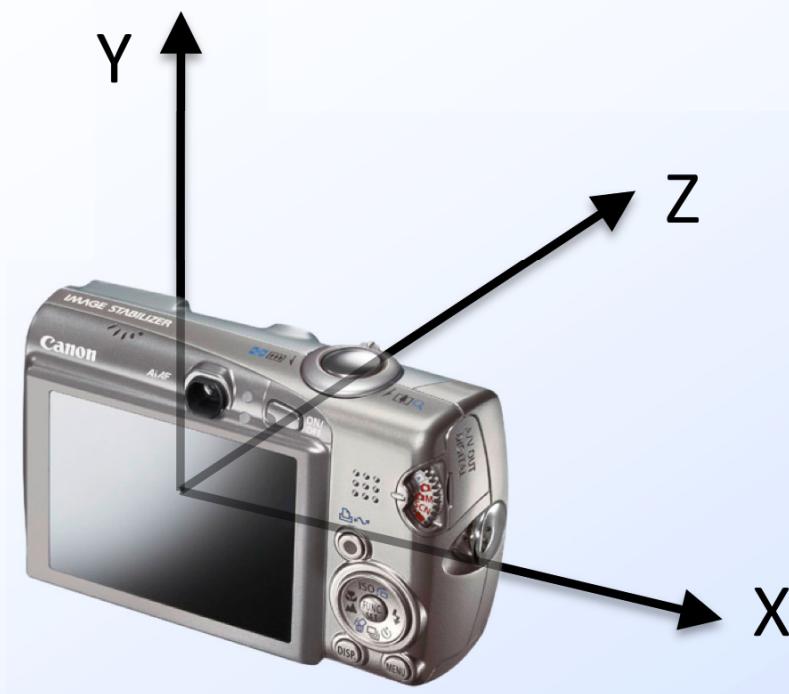
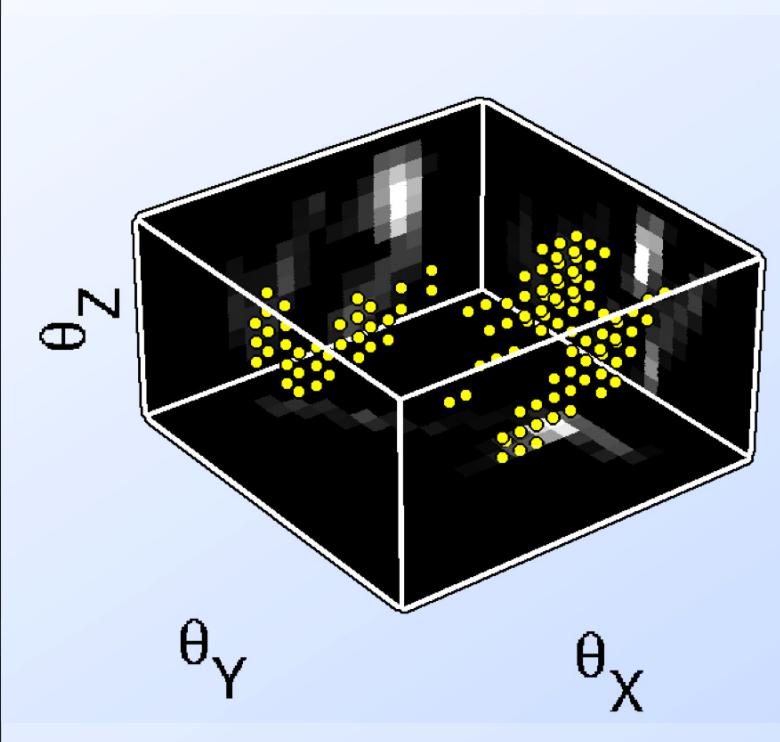
Blind deblurring – Fergus *et al.*



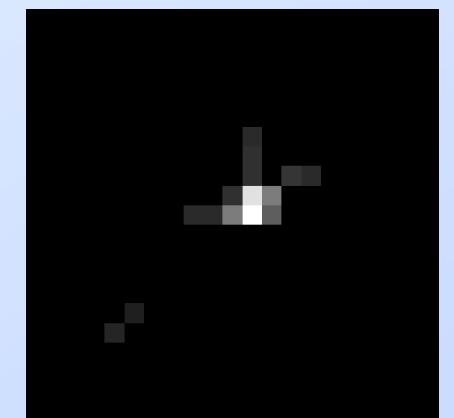
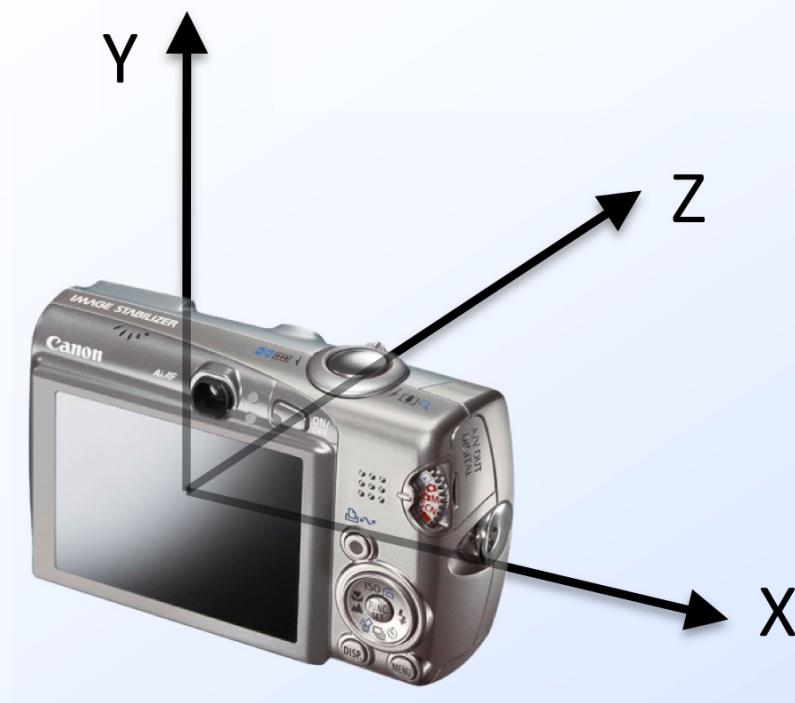
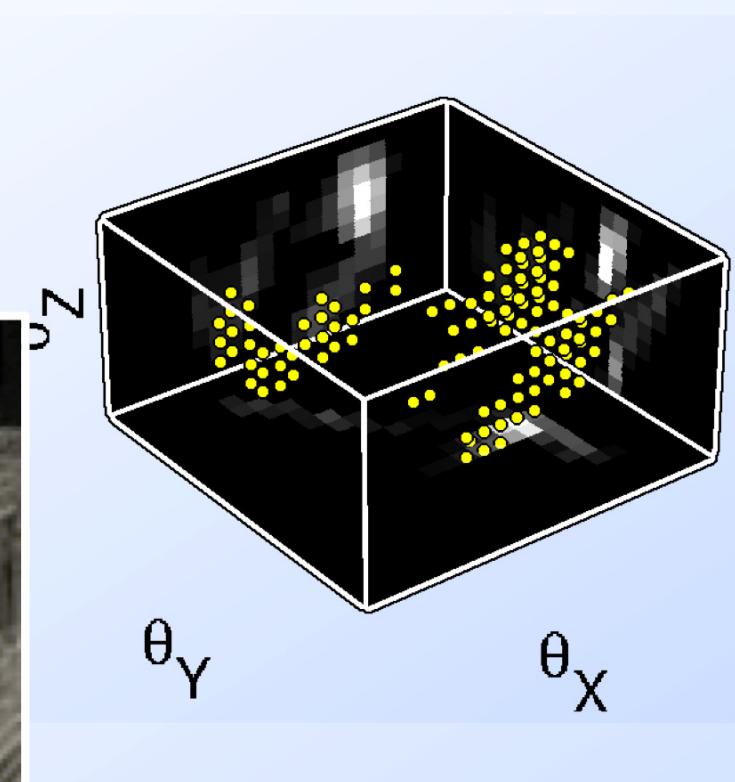
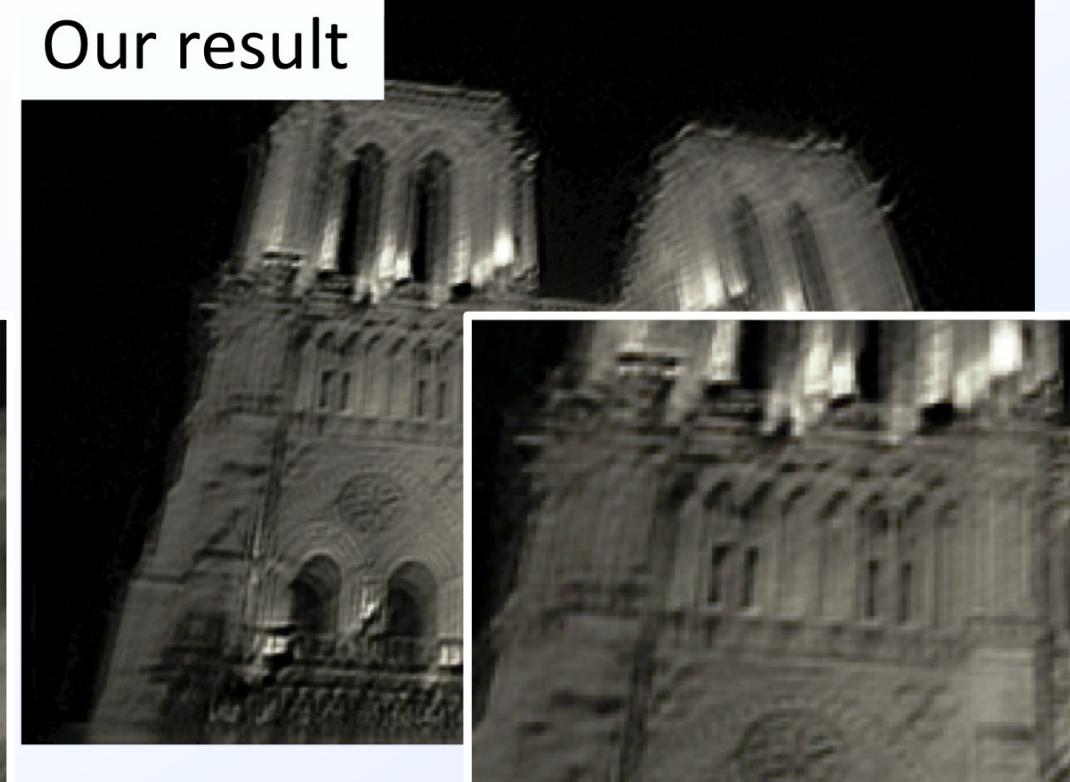
Blind deblurring – our result



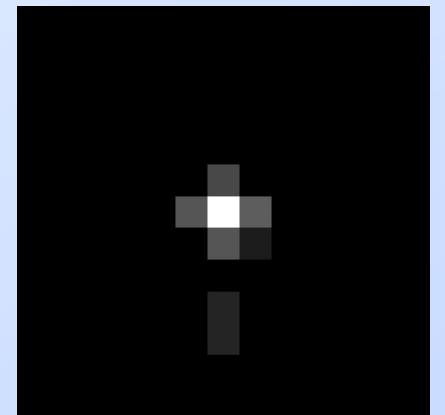
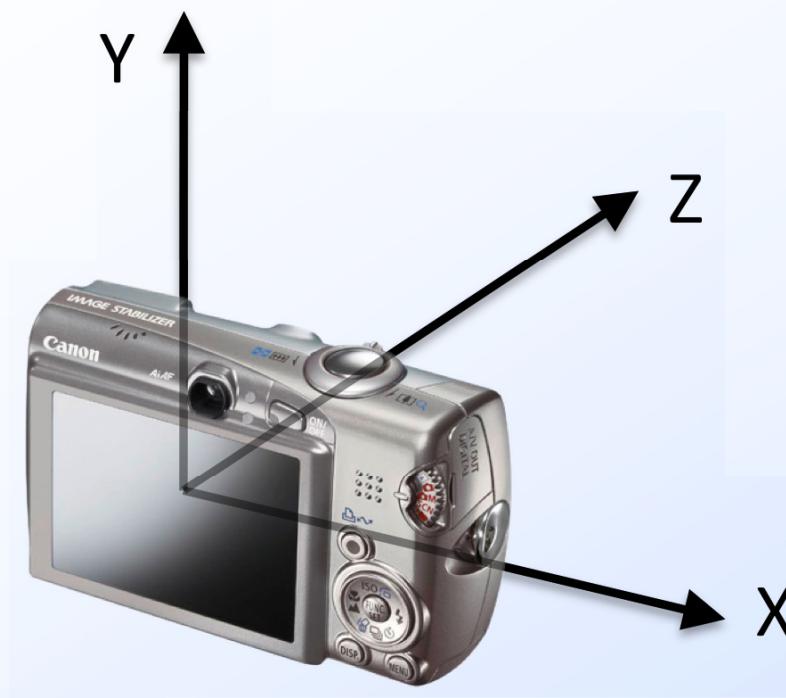
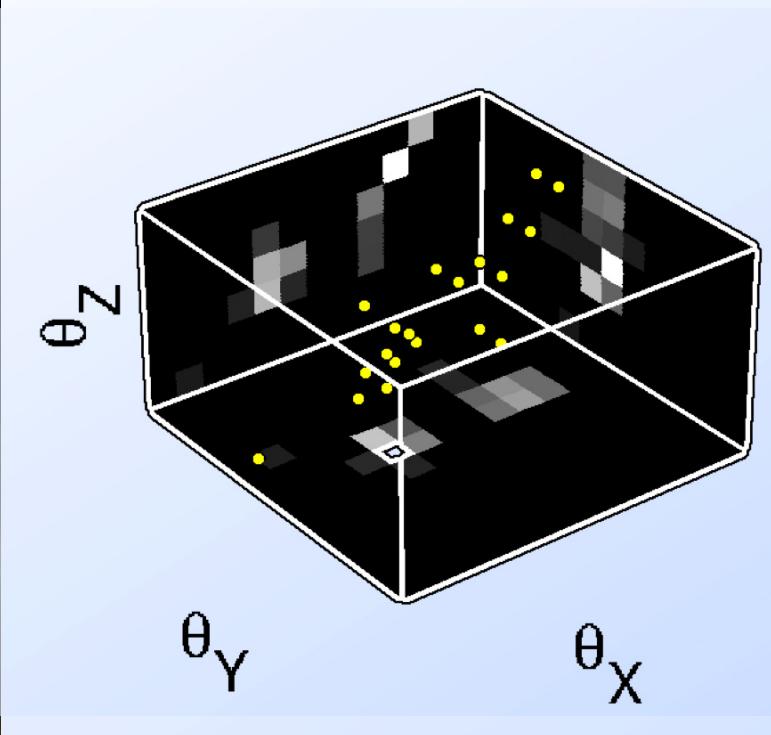
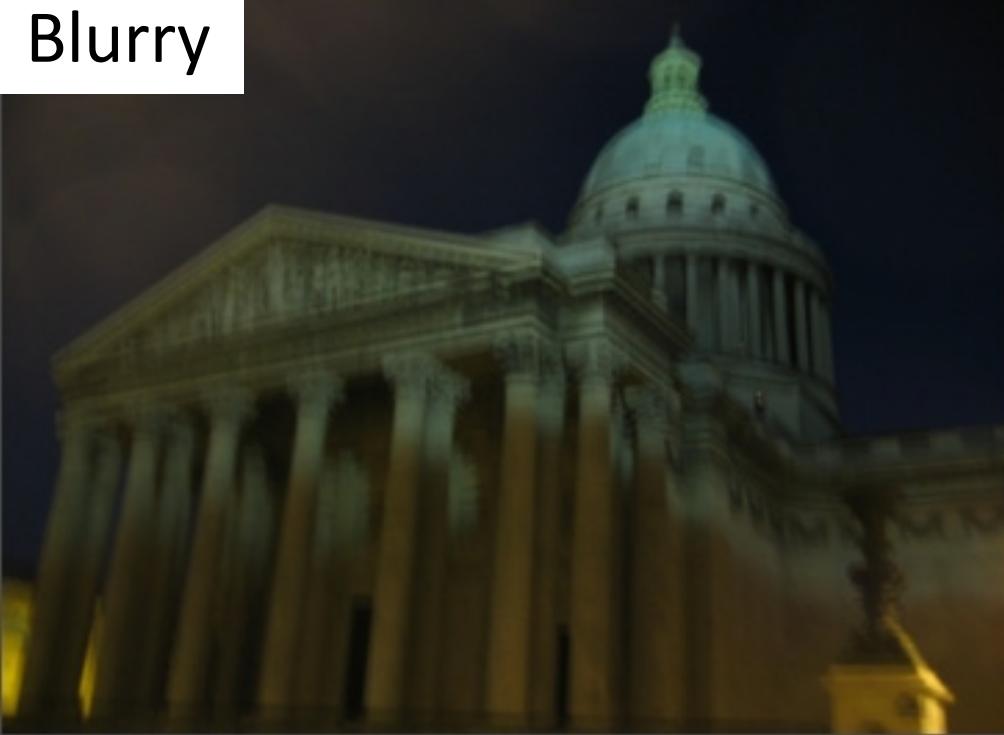
Blind deblurring – results



Blind deblurring – results

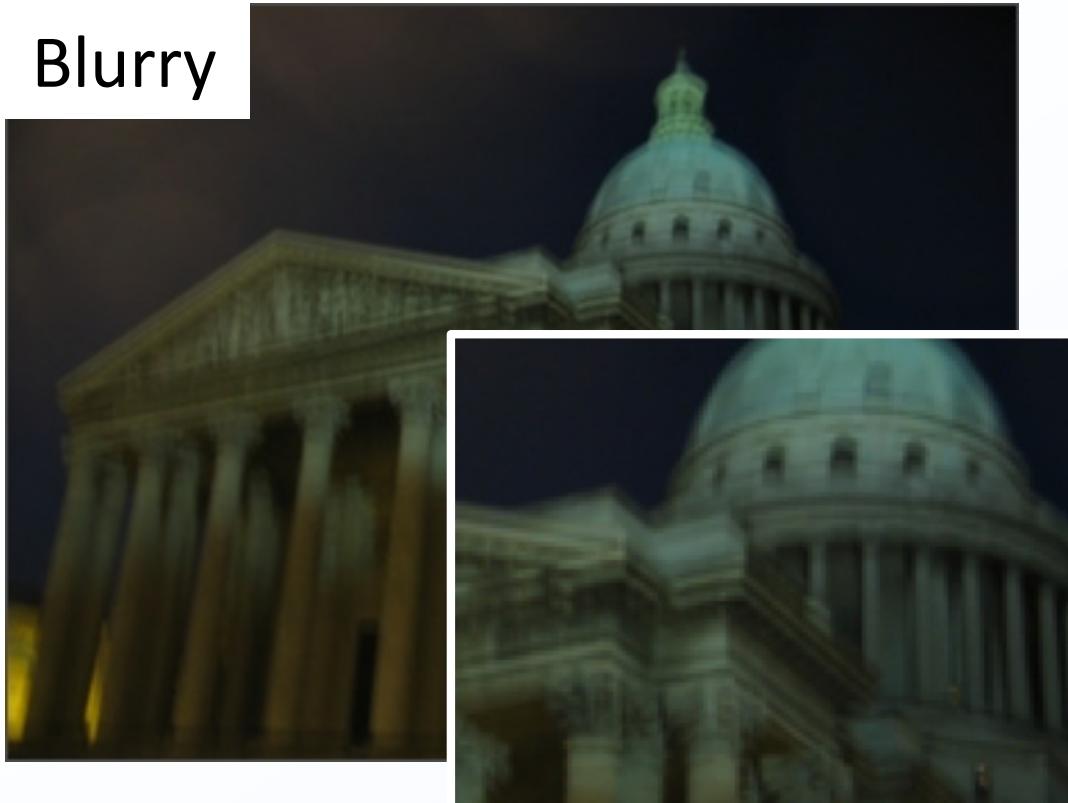


Blind deblurring – results

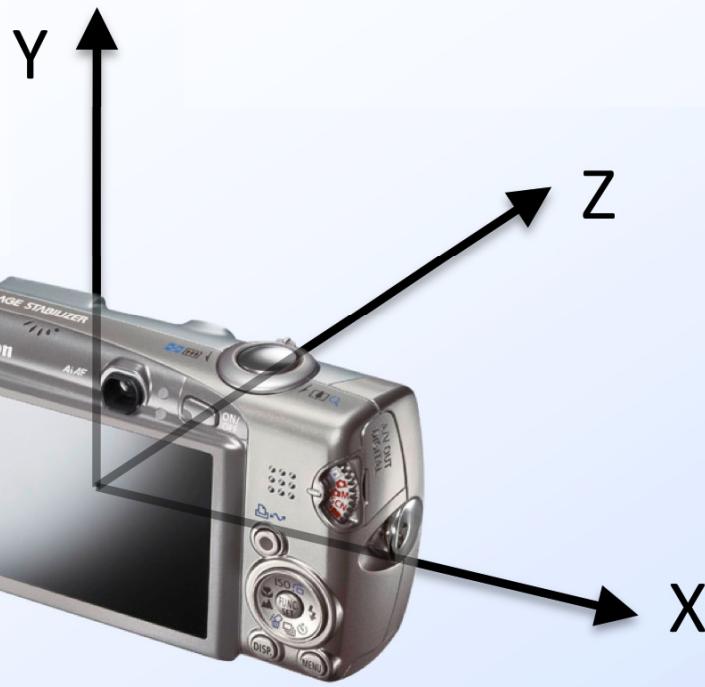
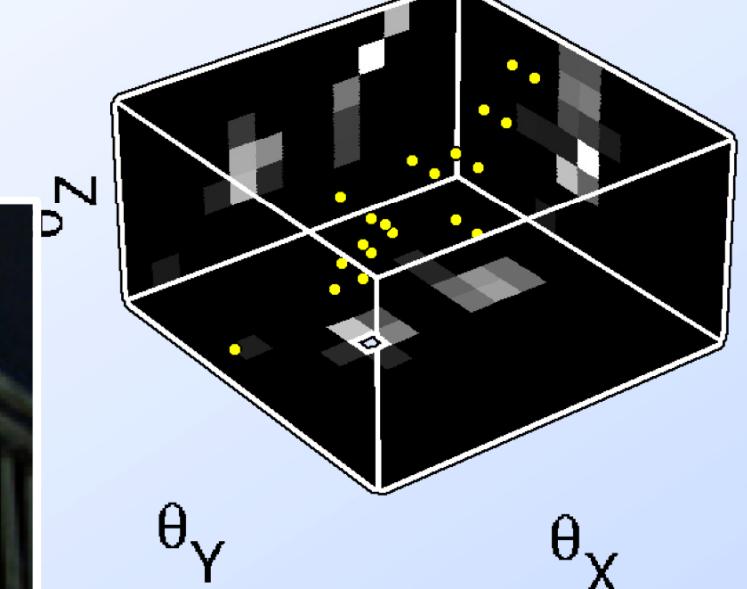
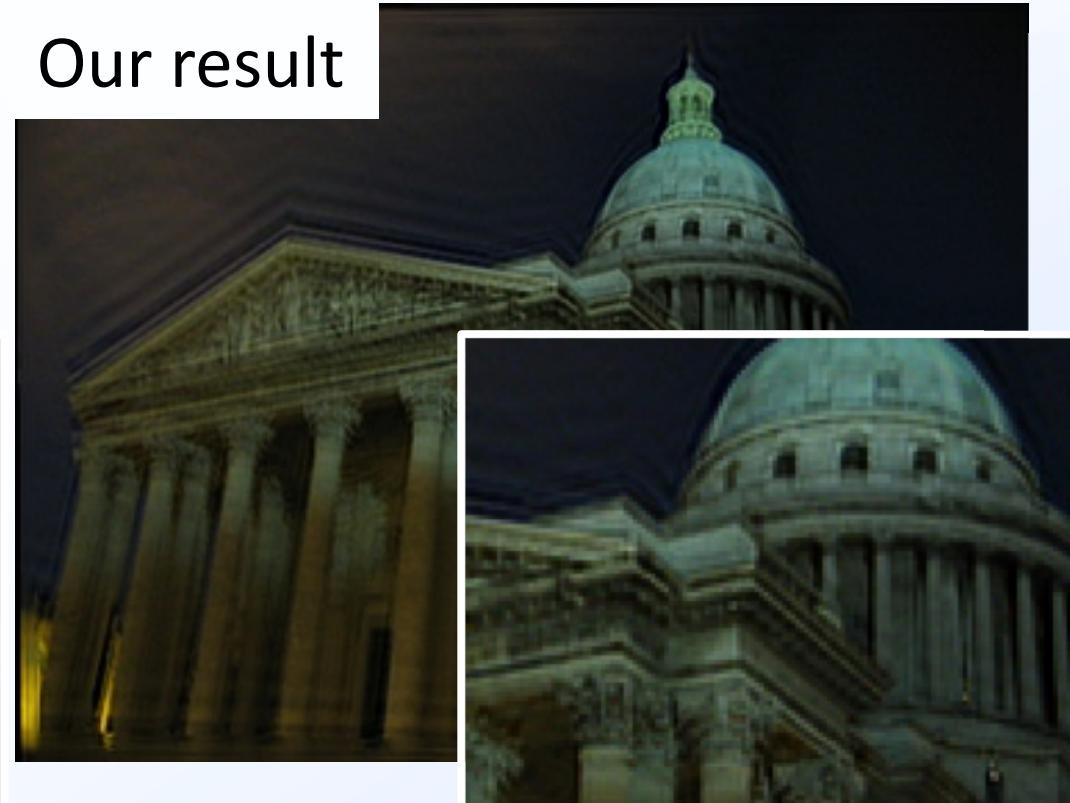


Blind deblurring – results

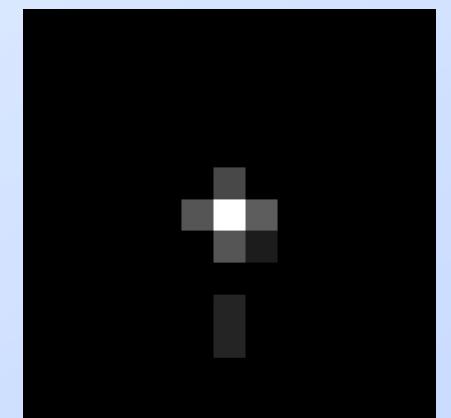
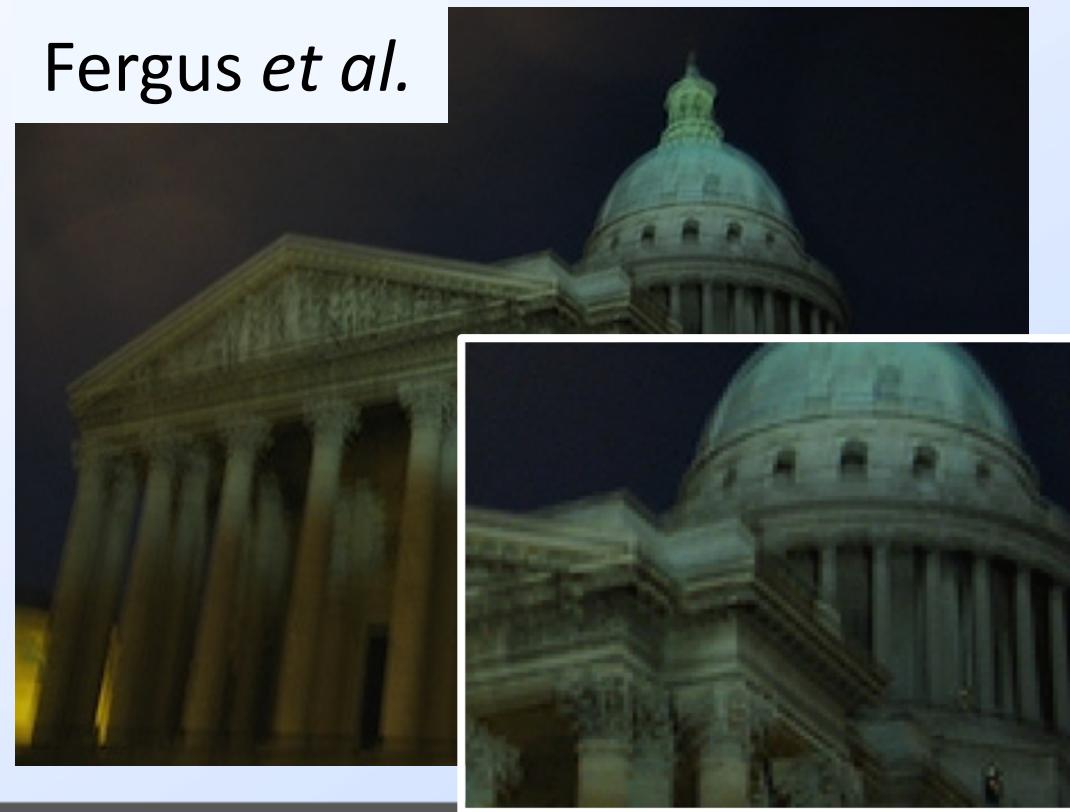
Blurry



Our result



Fergus *et al.*



Blind deblurring – synthetic

Sharp image



Blurry image



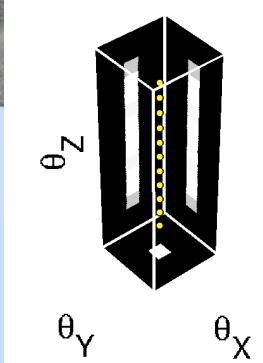
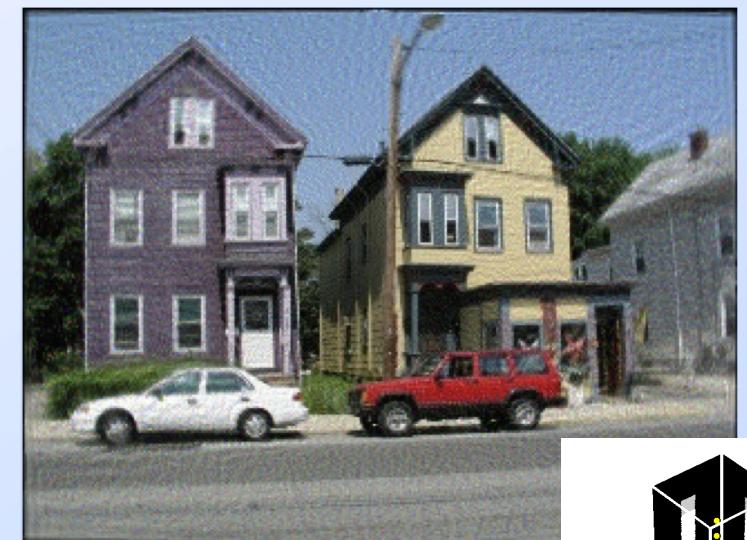
Fergus *et al.*



Our result



Ground-truth



Blind deblurring – synthetic

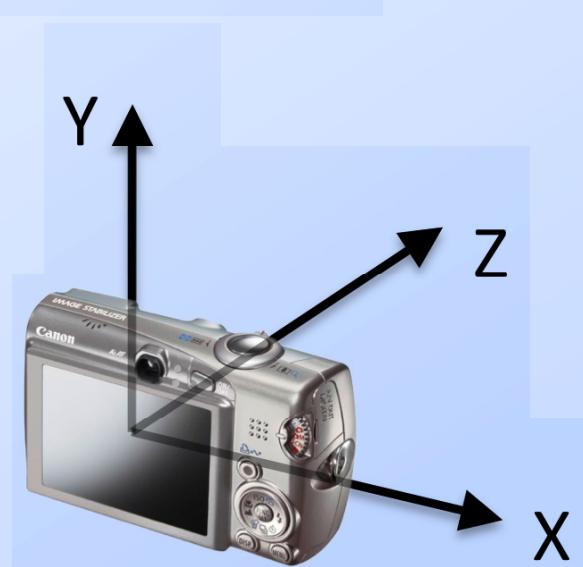
	10px		20px		30px	
<i>Y</i> -axis	R	U	R	U	R	U
$\sigma = 0$	23.1 (1.4)	23.2 (1.4)	27.2 (1.1)	58.1 (2.4)	32.2 (1.1)	129.3 (4.4)
$\sigma = 5$	24.9 (1.3)	25.8 (1.3)	29.0 (1.1)	56.8 (2.2)	33.4 (1.1)	62.9 (2.1)
$\sigma = 10$	27.0 (1.2)	30.1 (1.3)	30.7 (1.1)	48.7 (1.8)	41.9 (1.3)	57.8 (1.8)
<i>Z</i> -axis	R	U	R	U	R	U
$\sigma = 0$	14.4 (1.3)	21.8 (2.0)	18.1 (1.0)	26.1 (1.6)	25.4 (1.2)	57.6 (2.7)
$\sigma = 5$	17.4 (1.2)	24.8 (1.7)	23.2 (1.2)	54.5 (2.8)	30.6 (1.3)	58.6 (2.5)
$\sigma = 10$	22.0 (1.1)	50.9 (2.7)	26.5 (1.1)	55.8 (2.4)	30.0 (1.2)	57.5 (2.2)

RMS errors for deblurred results

(R) our rotational model, compared to (U) Fergus *et al.*

In parentheses, the ratio to the RMS error achieved using the ground-truth kernel.

Our model gives lower errors, particularly as the blur's non-uniformity increases



Blind deblurring – uniform blur

Sharp image

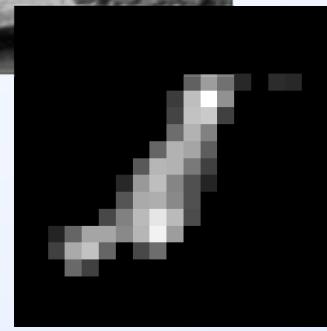


Blurry image

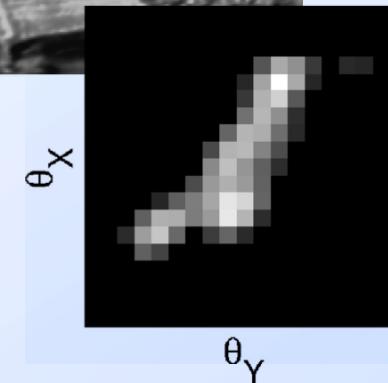


From Levin *et al.*
CVPR '09

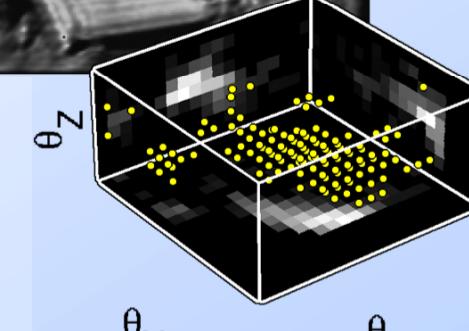
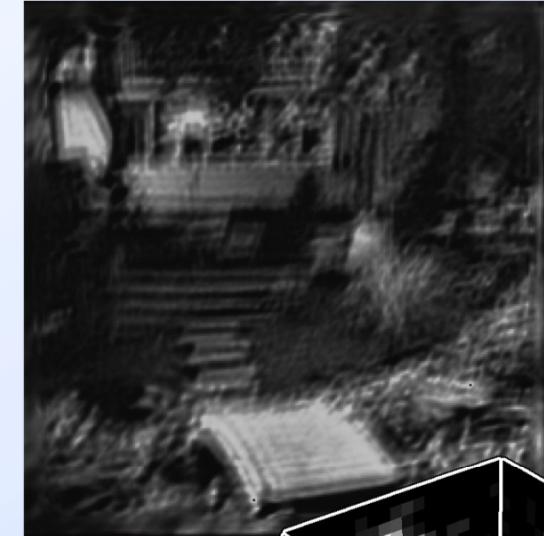
Fergus *et al.*



Ours $\theta_z = 0$



Ours

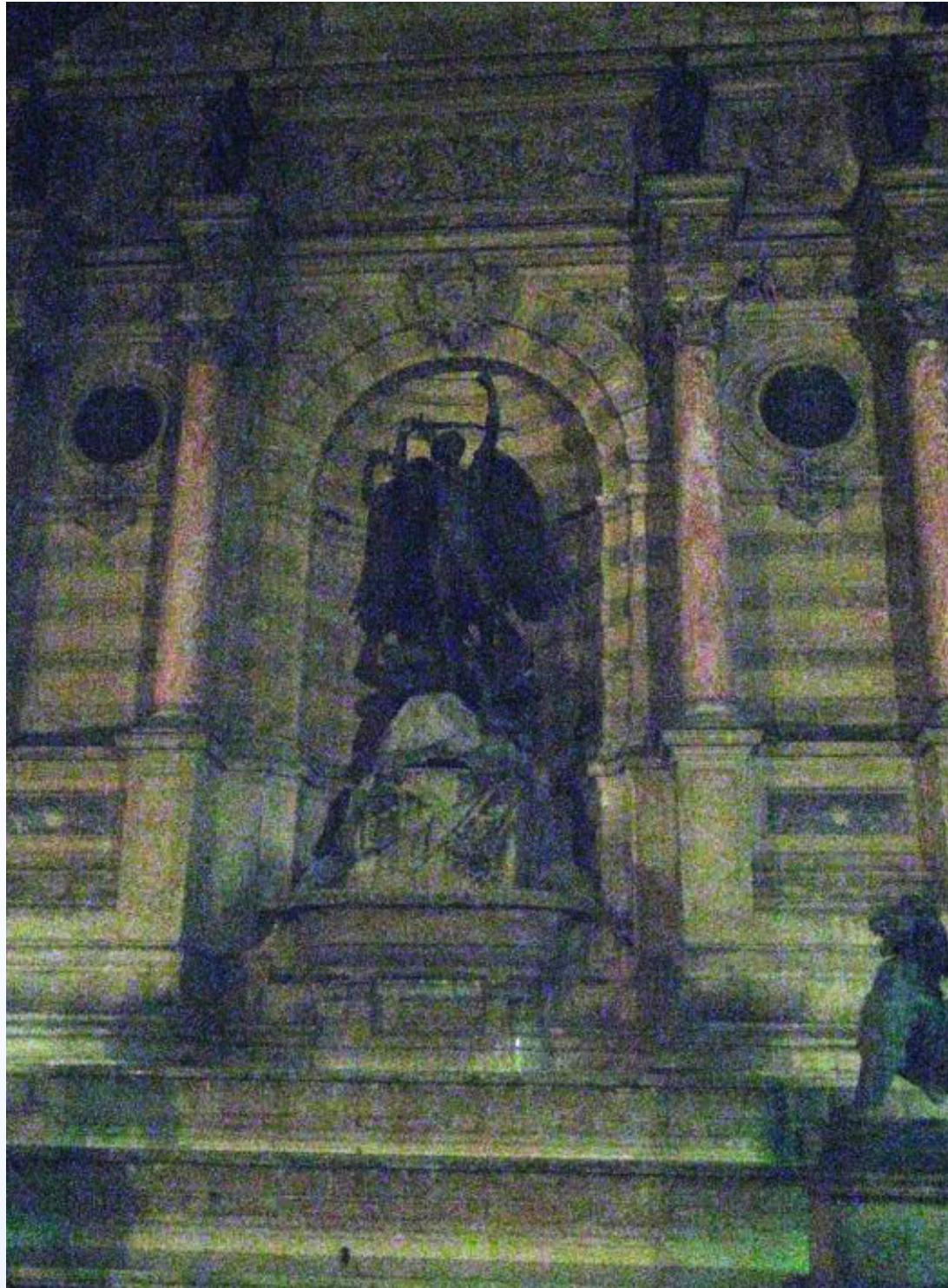


Ground-truth

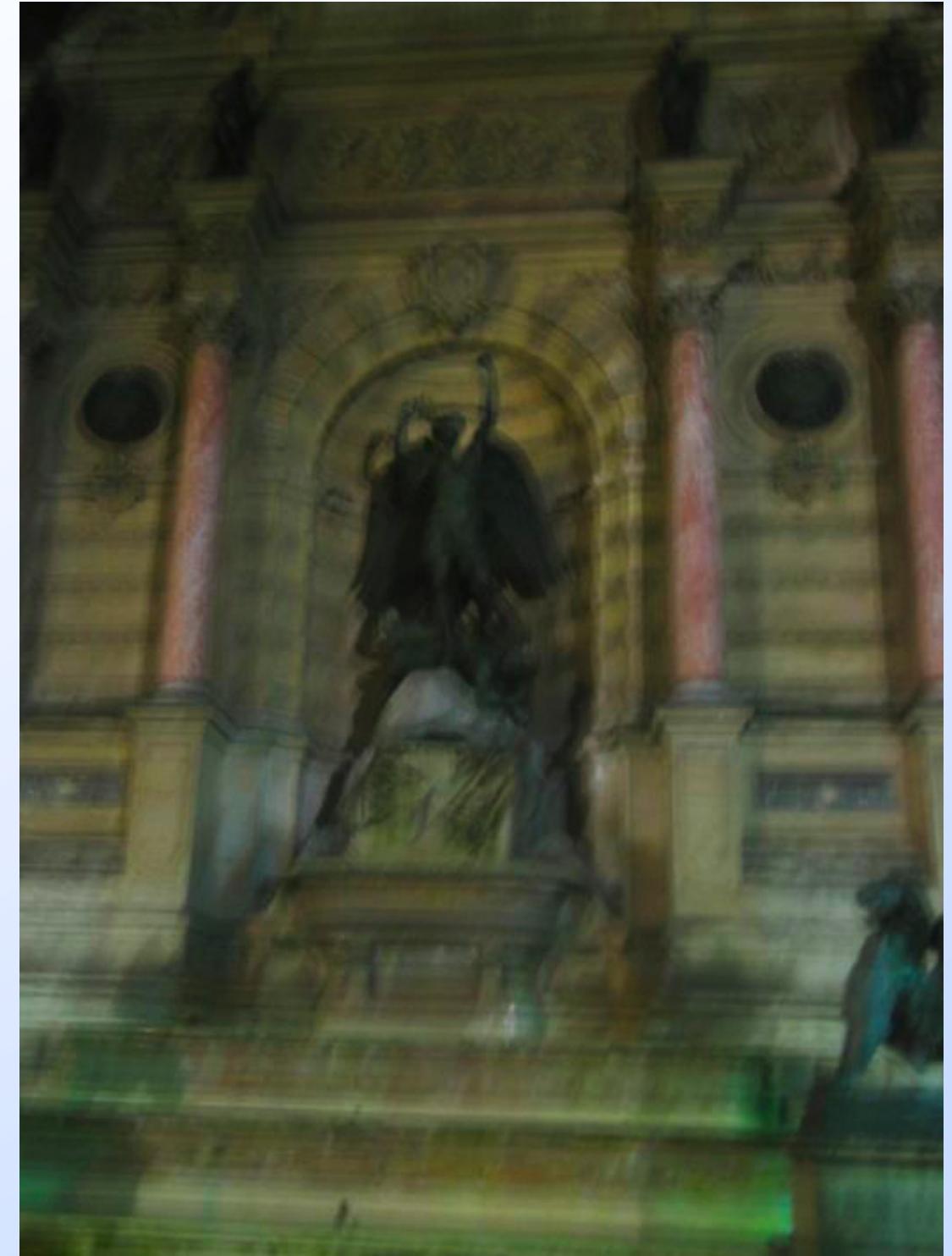


Application II: Noisy / blurry images

Noisy



Blurry



Noisy / blurry image pairs (Yuan *et al.*, 2007)

- Use a noisy image as a proxy for the sharp image, estimate kernel using least squares:

$$\min_{\mathbf{w}} \|\mathbf{g} - \hat{\mathbf{g}}(\mathbf{f}_N, \mathbf{w})\|_2^2 \quad \text{s.t.} \quad \|\mathbf{w}\|_1 = 1$$
$$w_k \geq 0 \quad \forall k$$

“reconstruction” of blurry image using \mathbf{f}_N & \mathbf{w}

noisy image

- Linear least squares thanks to bilinear model:
$$\hat{\mathbf{g}}(\mathbf{f}_N, \mathbf{w}) = \mathbf{B}_N \mathbf{w}$$
- Deblur with modified Richardson-Lucy algorithm

Noisy / blurry image pairs – results

Uniform result



Our result

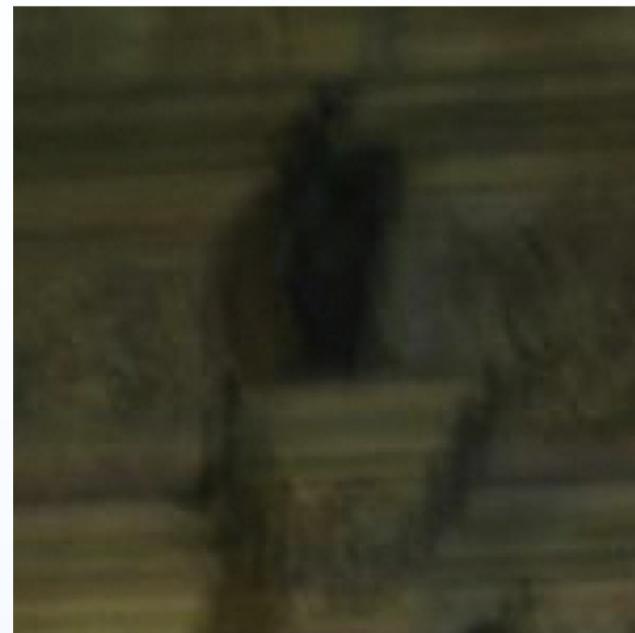


Noisy / blurry image pairs – detail

Noisy



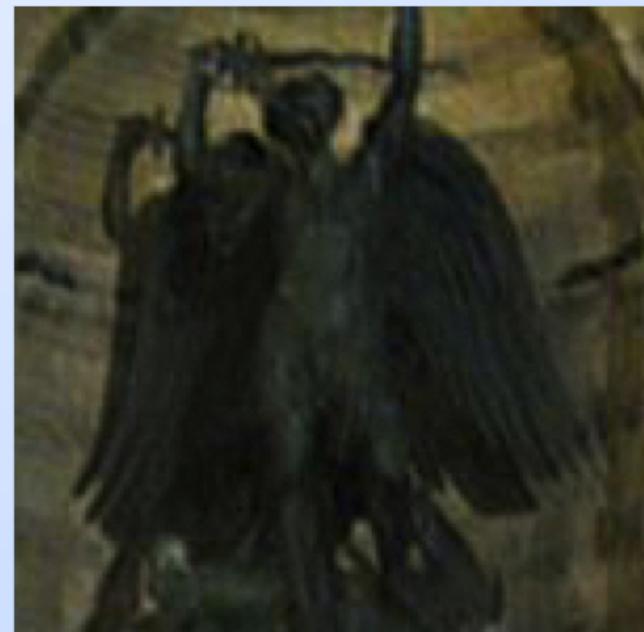
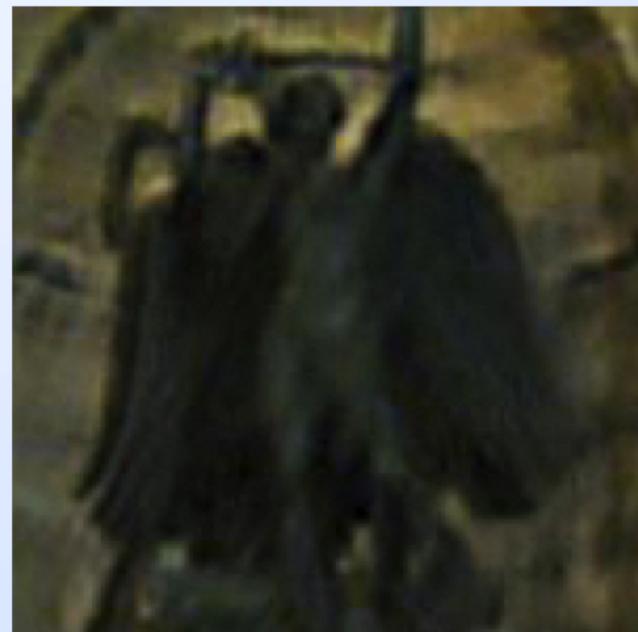
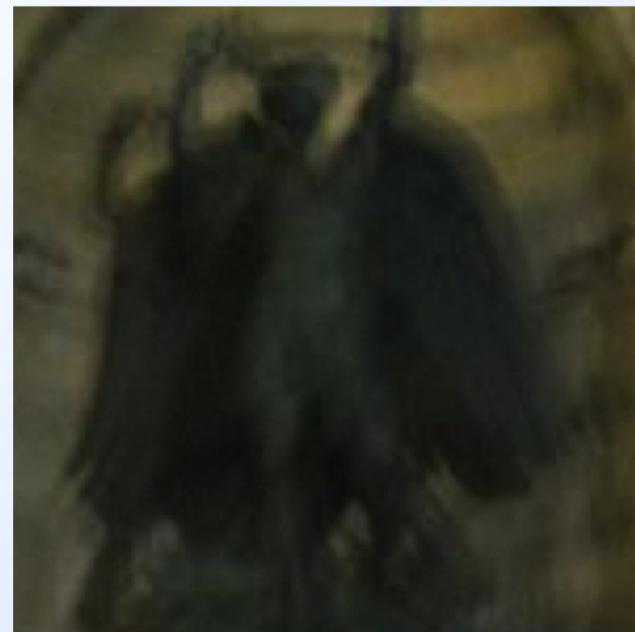
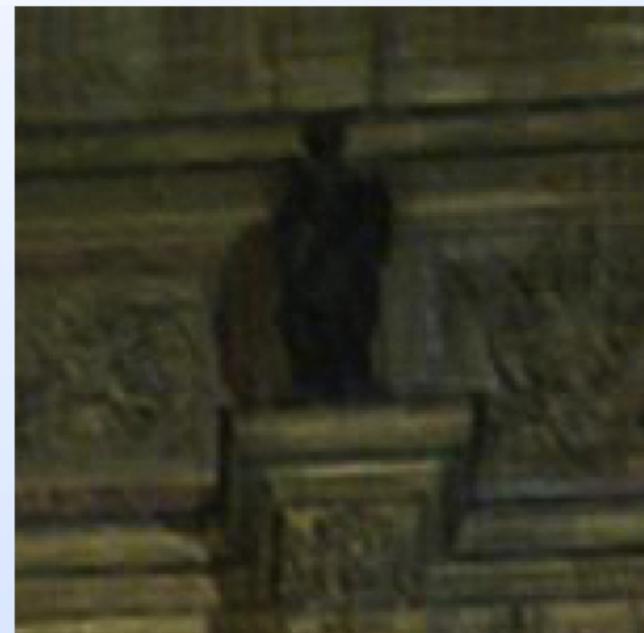
Blurry



Uniform result



Our result

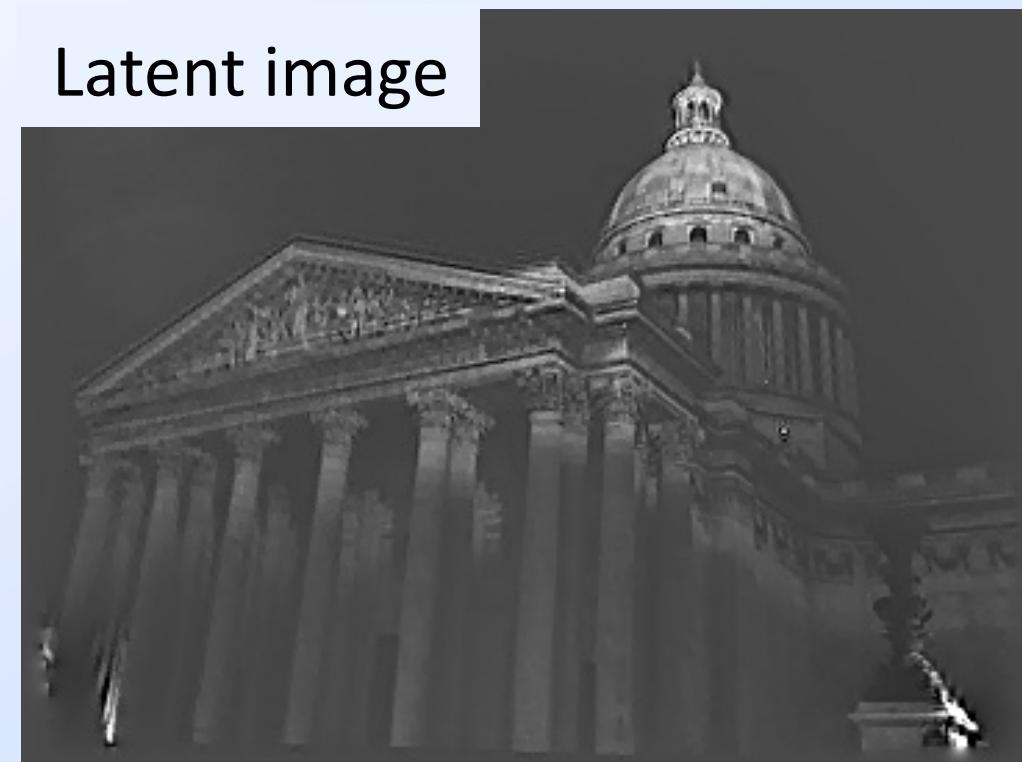
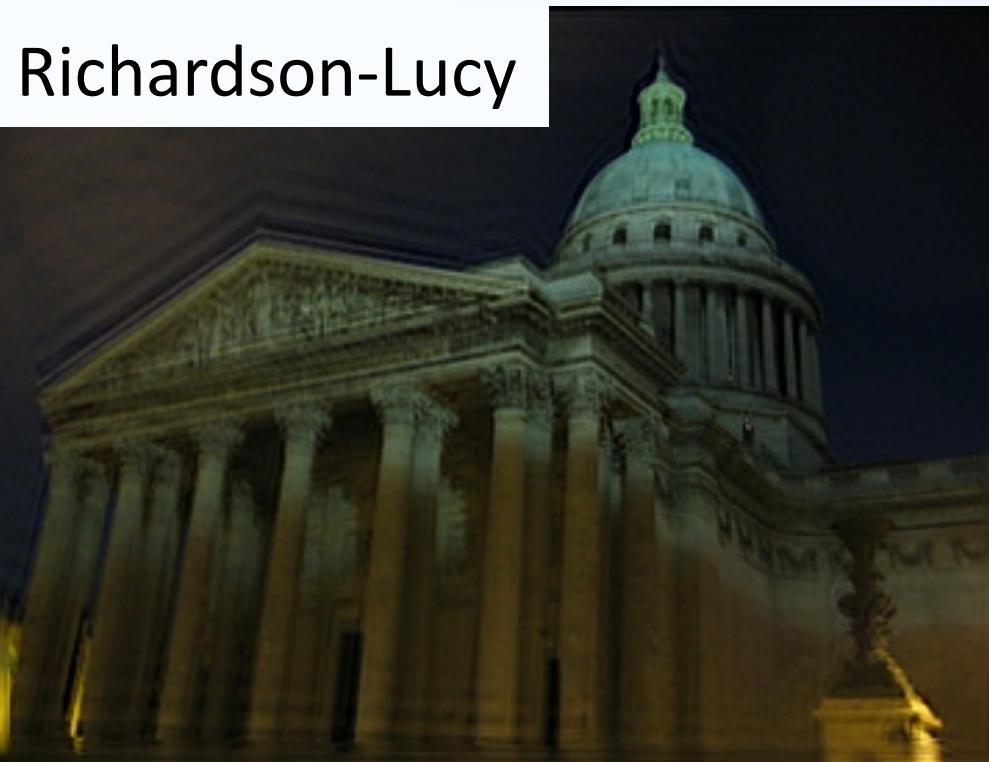


Conclusions

- A geometrically derived model for non-uniform blur due to camera-shake
- Bilinear computational form generalises typical convolution blur model
- Can plug our model into existing deblurring algorithms

Future directions

- Problem of “ringing” in deblurred images, due to Richardson-Lucy algorithm
 - Possibility of using latent image directly from variational algorithm



Future directions

- Problem of “ringing” in deblurred images, due to Richardson-Lucy algorithm
- Better algorithms for estimating and removing the blur
- Computational cost

Non-uniform Deblurring for Shaken Images

Oliver Whyte Josef Sivic Andrew Zisserman Jean Ponce

