

PAKE in the UC-Framework

Adaptive Security

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Universal Composability

- ▶ **Universal Composability**
- Password-Based AKE
- UC Password-Based AKE

Provable Security

Security proofs give the guarantee that an assumption is **enough** for security:

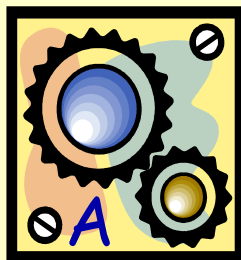
- if an adversary can break the system
- one can break the assumption

⇒ “reductionist” proof

Proof by Reduction

Reduction of a problem **P** to an attack *Atk*:

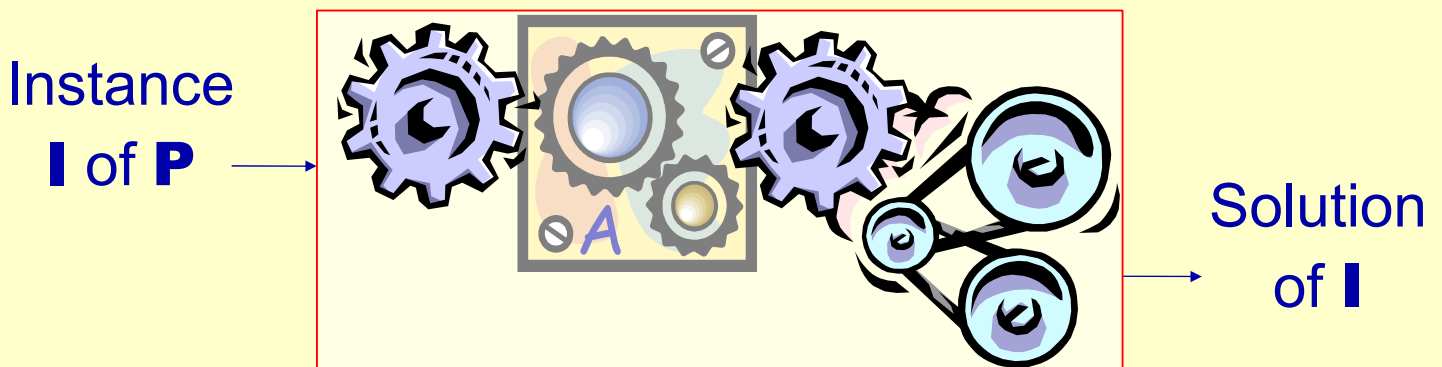
- Let *A* be an adversary that breaks the scheme
- Then *A* can be used to solve **P**



Proof by Reduction

Reduction of a problem **P** to an attack *Atk*:

- Let *A* be an adversary that breaks the scheme
- Then *A* can be used to solve **P**



P intractable \Rightarrow scheme unbreakable

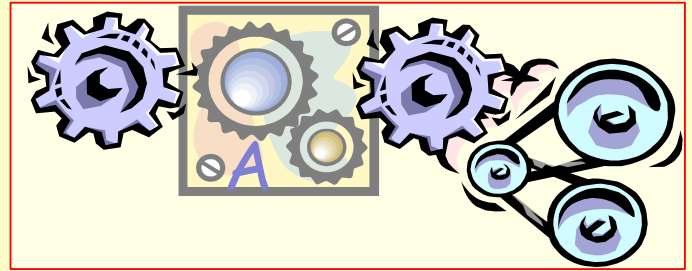
Provably Secure Scheme

To prove the security of a cryptographic scheme, one has to make precise

- the algorithmic assumptions
- the security notions to be guaranteed
- a reduction: an adversary can help to break the assumption

Simulation

In such a reduction, our simulator tries to emulate the environment, until the adversary may win the attack game

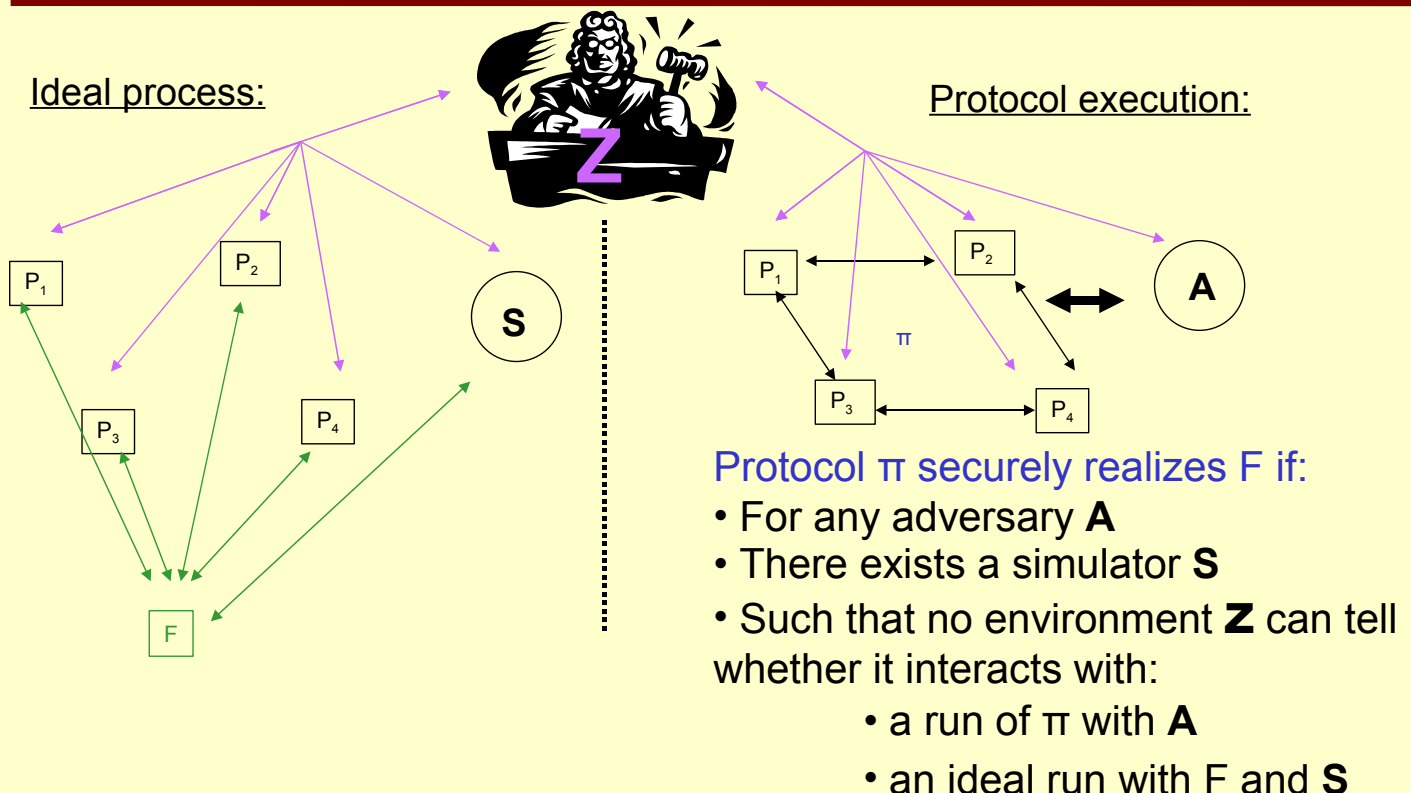


What about the composition of multiple protocols?

- the simulation fails as soon as an adversary may break one part of the global system, whereas other parts may provide a protection
 - other executing protocols may provide additional information to the adversary
- either we re-prove the global system, or we prove each component in the **UC Framework**

Universal Composability

[Canetti - FOCS '01]



Real vs. Ideal

Definition of security

Protocol π emulates the ideal process for F if

- for any adversary A
- there exists a simulator S
- such that for all Z

$$\text{IDEAL}_{S,Z}^F \sim \text{EXEC}_{\pi,A,Z}$$

\Rightarrow we say that protocol π **securely realizes** F .

$$(\forall A) (\exists S) (\forall Z) \text{IDEAL}_{S,Z}^F \sim \text{EXEC}_{\pi,A,Z}$$

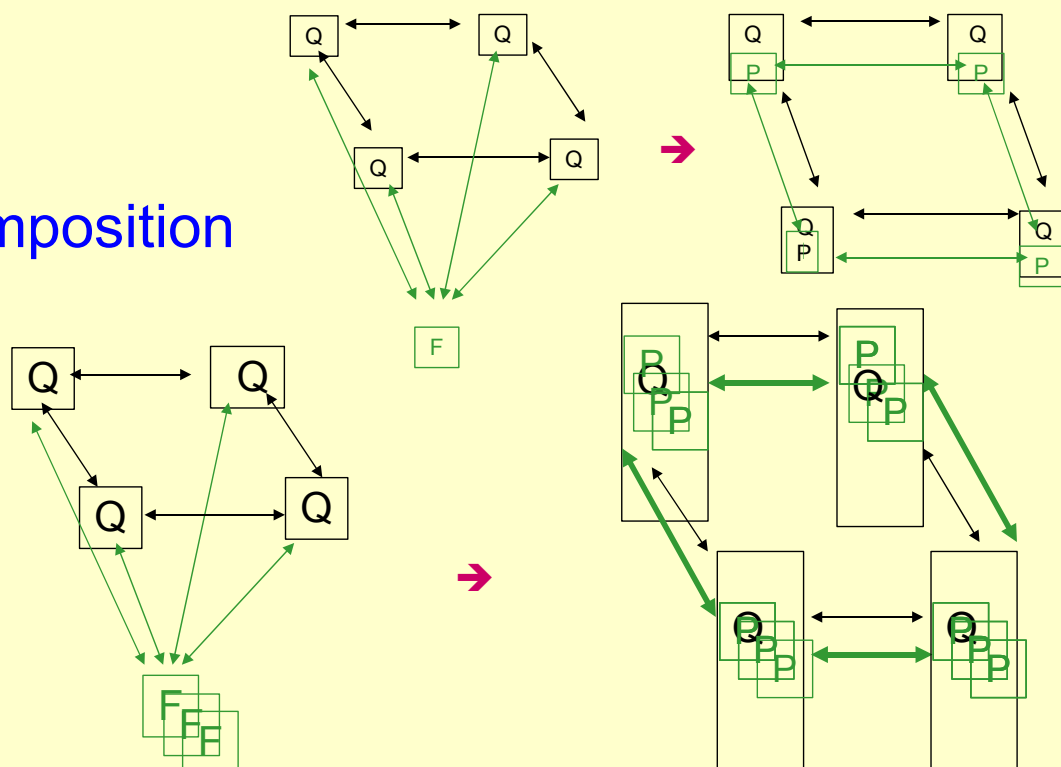
Equivalently:

$$(\exists S_d) (\forall Z) \text{IDEAL}_{S_d,Z}^F \sim \text{EXEC}_{\pi,A_d,Z}$$

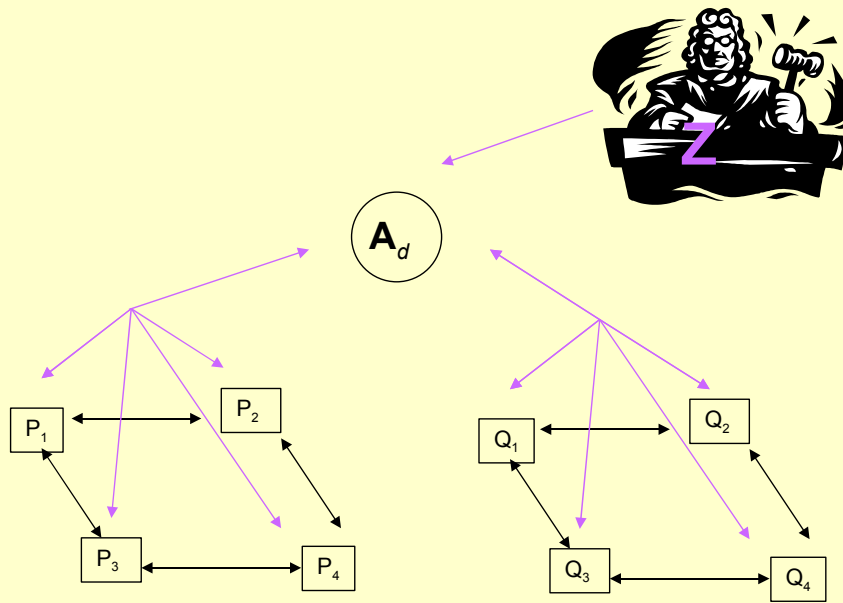
$$(\forall A) (\forall Z) (\exists S) \text{IDEAL}_{S,Z}^F \sim \text{EXEC}_{\pi,A,Z}$$

UC Theorem: Composition

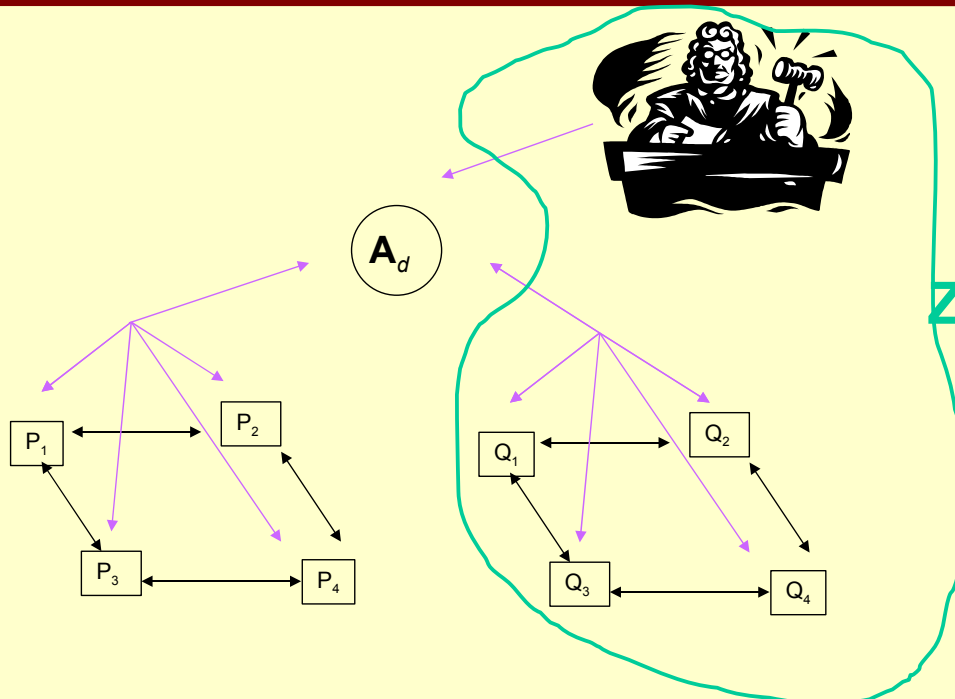
Modular composition



UC Theorem: Idea

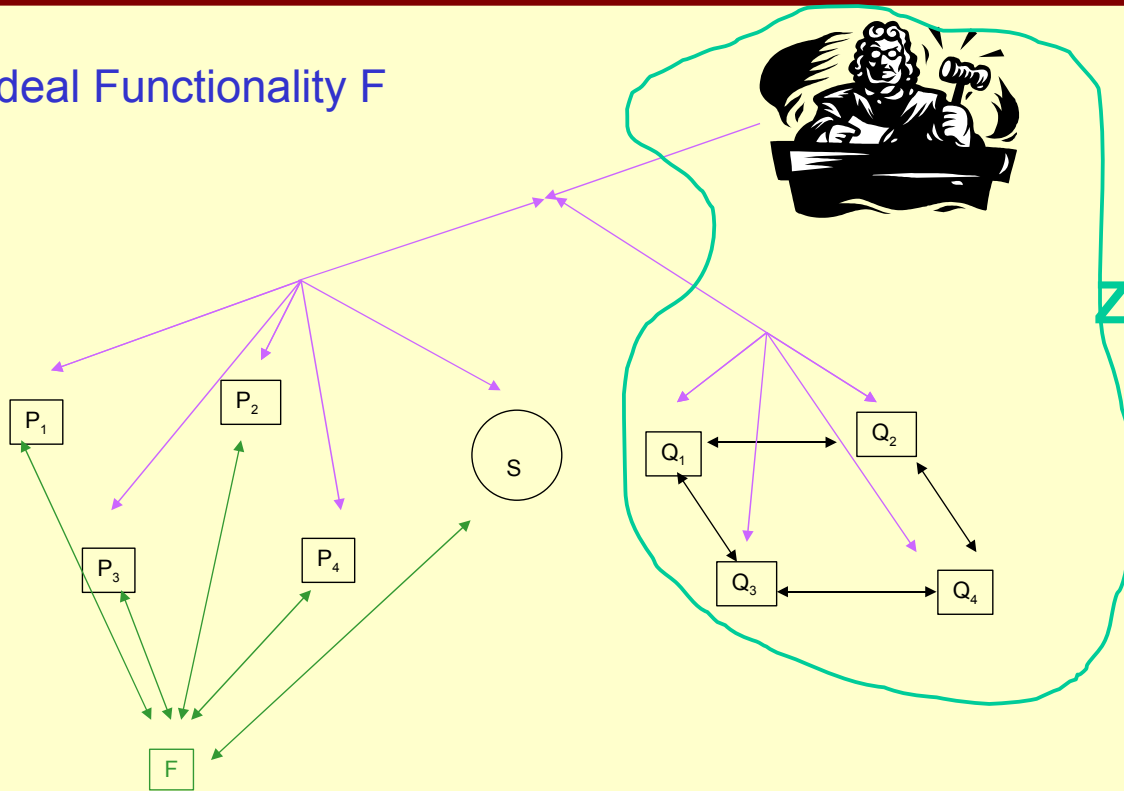


UC Theorem: Idea



UC Theorem: Idea

Ideal Functionality F



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Implications of UC

Can design and analyze protocols in a modular way:

- Partition a given task T to simpler sub-tasks $T_1 \dots T_k$
- Construct protocols for realizing $T_1 \dots T_k$.
- Construct a protocol for T assuming ideal access to $T_1 \dots T_k$.
- Use the composition theorem to obtain a protocol for T from scratch.

(Now can be done concurrently and in parallel.)

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Password-Based AKE

Key Exchange

Key Exchange: a two-party protocol to generate a common random key that is “secret” for external adversaries.

- Assuming authenticated communication (Diffie-Hellman model)
- Unauthenticated communication (AKE)
- Different ways to authenticate the exchange:
 - Long-term public keys for signature or encryption plus “public-key infrastructure”.
 - Long-term pre-shared keys
 - Trusted third parties (The Kerberos model)
 - Passwords

Analysis of AKE

AKE has been studied extensively:

- Protocols were proposed, and later broken

First complexity-based notion: [Bellare-Rogaway - Crypto '93]

- Based on a “distinguishing game” for the adversary (FtG)
- Explicitly handles multiple concurrent sessions

Treatments that argue usability for secure sessions:

- Bellare-Canetti-Krawczyk - STOC '98
 - simulation based (but has problems)
- Canetti-Krawczyk – EC '01: based on BR93
 - with a different system model, defines and obtains “secure sessions”.
- Canetti-Krawczyk – EC '02: A UC treatment of AKE

Ideal Functionality: KE

Functionality \mathcal{F}_{KE}

\mathcal{F}_{KE} is parameterized by a security parameter k . It interacts with an adversary S and a set of (dummy) parties via the following queries:

Upon receiving a query $(\text{NewSession}, sid, P_i, P_j, \text{role})$ **from party** P_i :

Send $(\text{NewSession}, sid, P_i, P_j, \text{role})$ to S . In addition, if this is the first NewSession query, or if this is the second NewSession query and there is a record (P_j, P_i) , then record (P_i, P_j) .

Upon receiving a query $(\text{NewKey}, sid, P_i, sk)$ **from** S , where $|sk| = k$:

If there is a record (P_i, P_j) , and this is the first NewKey query for P_i , then:

- If either P_i or P_j is corrupted, then output (sid, sk) to player P_i .
- If there is also a record (P_j, P_i) , and a key sk' was sent to P_j , output (sid, sk') to P_i .
- In any other case, pick a new random key sk' of length k and send (sid, sk') to P_i .

Figure 1: The authenticated key-exchange functionality \mathcal{F}_{KE}

Password-Based Authentication

- **Asymmetric:** (sk_A, pk_A) and possibly (sk_B, pk_B)
 - they authenticate to each other using the knowledge of the private key associated to the certified public key
- **Symmetric:** common (long – high-entropy) secret
 - they use the long term secret to derive a secure and authenticated ephemeral key sk
- **Password:** common (short - low-entropy) secret
 - let us assume a **20-bit** password
 - ⇒ it is possible to win with non-negligible advantage

Ideal Functionality: pwKE

[Canetti-Halevi-Katz-Lindell-MacKenzie – EC '05]

Functionality $\mathcal{F}_{\text{pwKE}}$

The functionality $\mathcal{F}_{\text{pwKE}}$ is parameterized by a security parameter k . It interacts with an adversary S and a set of parties via the following queries:

Upon receiving a query $(\text{NewSession}, sid, P_i, P_j, pw, \text{role})$ from party P_i :

Send $(\text{NewSession}, sid, P_i, P_j, \text{role})$ to S . In addition, if this is the first NewSession query of this form, mark the record (P_i, P_j, pw) as fresh. If this is not the first NewSession query of this form, mark the record as interrupted.

Upon receiving a query $(\text{TestPwd}, sid, P_i, pw')$ from the adversary S :

If there is a record of the form (P_i, P_j, pw) which is fresh, then do: If $pw = pw'$, mark the record compromised and reply to S with "correct guess". If $pw \neq pw'$, mark the record interrupted and reply with "wrong guess".

Upon receiving a query $(\text{NewKey}, sid, P_i, sk)$ from S , where $|sk| = k$:

If there is a record of the form (P_i, P_j, pw) , and this is the first NewKey query for P_i , then:

- If this record is compromised, or either P_i or P_j is corrupted, then output (sid, sk) to player P_i .
- If this record is fresh, and there is a record (P_j, P_i, pw') with $pw' = pw$, and a key sk' was sent to P_j , and (P_j, P_i, pw) was fresh at the time, then output (sid, sk') to P_i .
- In any other case, pick a new random key sk' of length k and send (sid, sk') to P_i .

Either way, mark the record (P_i, P_j, pw) as completed.

Figure 2: The password-based key-exchange functionality $\mathcal{F}_{\text{pwKE}}$

Concurrent Executions

In this ideal functionality:

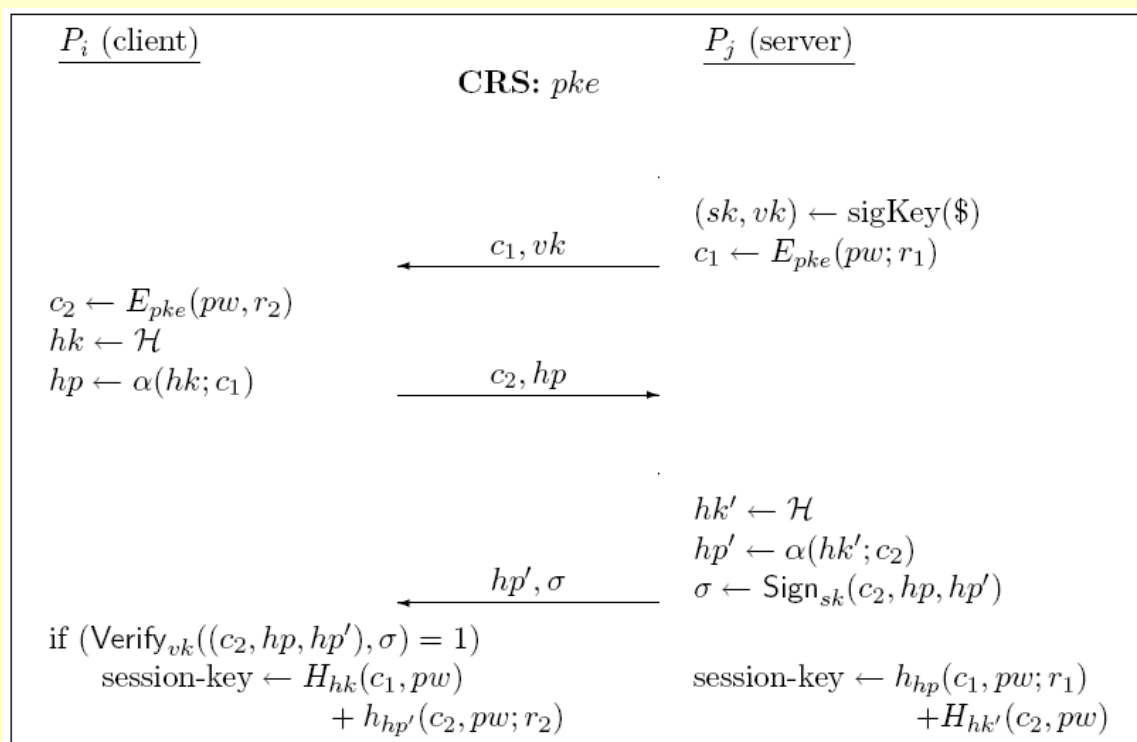
- **TestPwd** query, which gives the authorization to the adversary to test **one** password per session
- In case of correct password guess, the adversary can choose the key

Passwords:

- The environment chooses the passwords
- Can thus make players run with different passwords, or related passwords

⇒ passwords are not in an internal state of the functionality: no need of joint-state UC

KOY/GL Protocol



KOY/GL: Security Analysis

- Commitment:

- $c = \text{Commit}(pw, r) = \text{Encrypt}(pke, pw, r)$
- IND-CCA \Rightarrow NM for multiple commitments

- Smooth Projective Hash Functions:

$$H(c, pw) = \text{Hash}(hk; c, pw) = \text{ProjHash}(hp; c, pw; r)$$

- No information about $H(c, pw)$ if $pw \neq \text{Decrypt}(ske, c)$
- Hard to compute $H(c, pw')$ without either the hash-key hk or the witness r

- Session Key:

$$c_1 = \text{Encrypt}(pke, pw, r_1) \quad c_2 = \text{Encrypt}(pke, pw, r_2)$$

$$\begin{aligned} sk &= \text{Hash}(hk_2; c_1, pw) + \text{ProjHash}(hp_1; c_2, pw; r_2) \\ &= \text{ProjHash}(hp_2; c_1, pw; r_1) + \text{Hash}(hk_1; c_2, pw) \end{aligned}$$

KOY/GL: Security Analysis

- Passive Adversary:

- Pseudo-randomness without the witness
 \Rightarrow indistinguishability of the session key

- Active Adversary:

- NM for multiple commitments
 \Rightarrow no new valid commitment (except chance with pw)
- Invalid commitment
 \Rightarrow indistinguishability of sk (statistic)
- Replay of commitment: does not know the witness
 \Rightarrow indistinguishability of sk (computational)

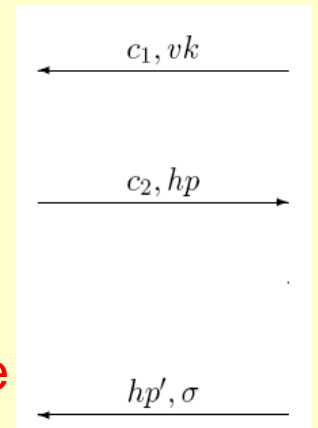
KOY/GL: Security Analysis

Proof: with an extractable commitment

- Adversary sends c_1 : we can extract the password, and check whether it is correct or not
- Simulator sends c_1 : with a random/dummy pw
 - adversary sends c_2 : extract and check
 - wrong \Rightarrow random key
 - correct \Rightarrow we get stuck

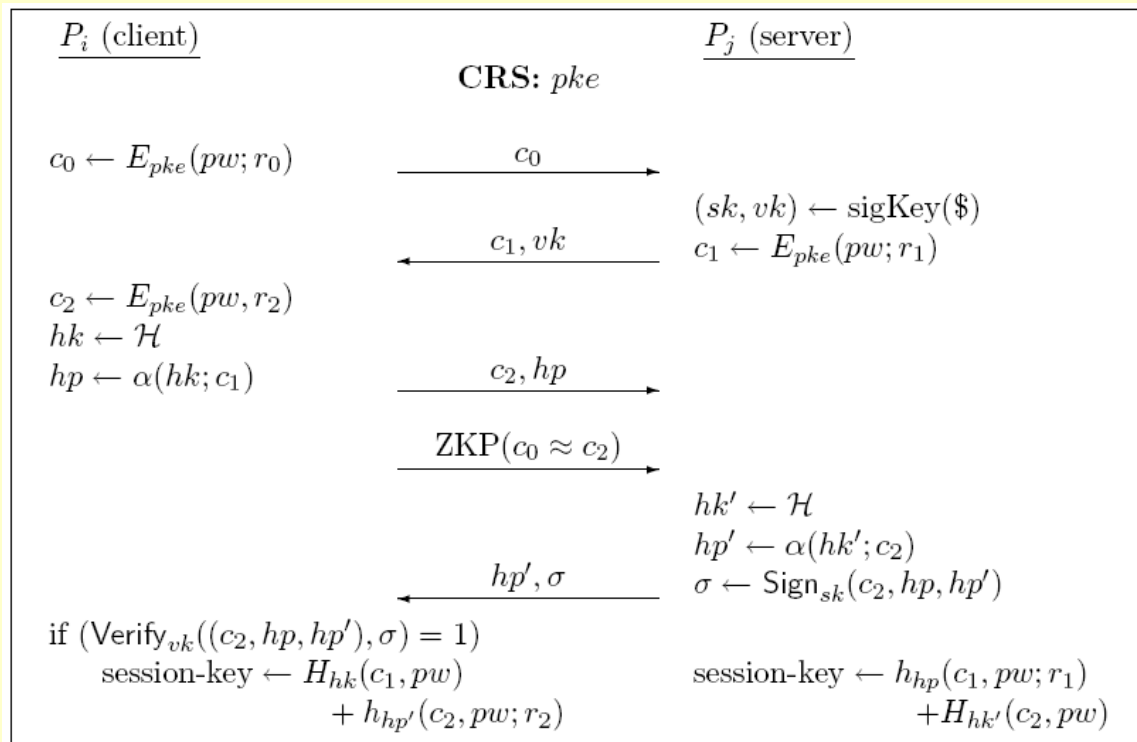
Wrong simulation if adversary has guessed pw

Not negligible and thus not UC secure



UC PAKE

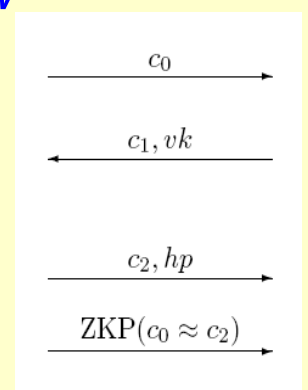
[Canetti-Halevi-Katz-Lindell-MacKenzie – EC '05]



CHKLMK: Idea

UC Proof: with an extractable commitment

- Adversary sends c_0 : we can extract the password, and check whether it is correct or not
- Simulator sends c_0 : with a random/dummy pw
 - adversary sends c_1 : extract and check pw
 - wrong \Rightarrow random key
 - correct \Rightarrow we commit the correct password in c_2 and simulate a fake ZKP



Adaptive Adversary

An adaptive adversary can corrupt players at any time and receive the internal state

- in KOY/GL-like scheme: not secure
 - in the simulation, use of “dummy password” for c_0
 - if corruption right after that: how to simulate r_0 ?
 - in EKE-like scheme: secure
 - granted the Programmability of the Ideal-Cipher and the Random Oracle
- ⇒ Adaptive adversaries and strong corruption
[Abdalla-Catalano-Chevalier-Pointcheval – CT-RSA '08]

EKE Scheme

