

The Biological Consequences of the Computational World: Mathematical Reflections on Cancer Biology¹

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Abstract The role of continua has been clear since antiquity in the mathematical approaches to physics, while discrete manifolds were brought to the limelight mostly by Quantum and Information Theories, in the XX century. We first stress how theorizing and measuring radically change in physics when using discrete vs. continuous mathematical manifolds. It will follow that the reference to discrete structures and digital information is far from neutral in knowledge construction. In biology, in particular, we claim that the introduction of information as a new observable on discrete data types has been promoting a dramatic reorganization of the tools for knowledge. We briefly analyze the origin and the nature and then highlight some consequences of the bias thus induced in life sciences. We show how strong consequences have been derived from vague, common sense hypotheses and stress their role in cancer biology. We finally summarize new theoretical frames that propose different directions as for the organizing principles for biological thinking and experimenting, including in cancer research. Cancer is then viewed as an organismal, tissue based issue, according to the perspective proposed in (Sonnenschein, Soto, 1999; Baker, 2015).

Keywords: continuous vs discrete modeling, causality in physics, in biology, alpha-numeric coding, elaboration, transmission of information, randomness in biology, Somatic Mutation Theory, Tissue Organization Field Theory.

1. Introduction

The computational virtuality is heavily affecting common and scientific knowledge. The new symbolic forms of interaction on electronic digital networks provide extraordinary new tools for mankind, from everyday worldwide exchanges to scientific modeling. Yet, they also suggest an image of the world rich of a peculiar bias. It is in biology that the reference to informational, alphanumerical data structures has had the greatest impact throughout the second half of the twentieth century, by making DNA an “information carrier” or even a “computer program” for

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ontogenesis. As a consequence, development has been interpreted as the deployment of a program and organisms as “avatars” of genetic information². We begin with an analysis of the peculiar interplay discrete vs continua in the understanding (or by-passing) causality, a crucial notion in natural sciences. We will then mention some of the strong consequences of the weak conceptual frame based on a vague, common sense reference to computational notions³, with particular emphasis on cancer research.

It should be clear that Information Sciences as such do not imply, per se, the fuzzy applications of their proper concepts to other domains. Yet, they contain the grounds for a reading of the world through the digital or “discrete” grid of numerical databases and computations, as soon as those fantastic tools for digital computing are transformed in “models” or *true images* of physical or biological phenomena. In other words, we claim that the intelligibility of the world proposed by discrete mathematical structures is far from neutral; in particular, it yields a peculiar approach to causality. Our claim is that the often implicit, but pervasive, reference to discrete mathematics, such as the main theories of elaboration and transmission of information, biased causal analyses in biology, such as the etiology of cancer.

2. Causality in physics and in computing

A comparative analysis between different theoretical frames will guide our critique of the information theoretic approach still framing research, in molecular biology in particular. This critique stresses the linguistic/computational nature of the theoretical frame, which shaped research, as in the case of cancer we discuss below. In our view, that perspective is not even “reductionist”, if by reduction one refers to “reduction to existing physical theories”, as major physical properties of macro-molecular interactions have been ignored. In order to prove this, we need a close presentation of some major concepts in physics.

2.1 The mathematics of natural phenomena: causality in continuous vs. discrete manifolds

By “discrete” here we refer to the only good mathematical sense one can give to this notion: the set of elements of a *discrete manifold* can be “naturally” given the discrete topology, that is, they may be all isolated (for each element there exists a neighborhood which contains only that element). Thus, we can only count them, as they are all separated by a metrics intrinsic to the manifold, each in its own neighborhood⁴. B. Riemann (1854) beautifully expressed this in his thesis that opened the way to differential Geometry and, then, Relativity Theory: « In the case of discrete magnitudes, the comparison with regard to quantity is accomplished by counting, in the case of continuous magnitudes by measuring » (p.3, Clifford's translation, 1873). « In a discrete manifold, the ground of its metric relations is given in the notion of it, while in a continuous manifold, this ground must come from outside. Therefore, either the reality which underlies space must form a discrete manifold, or we must seek the ground of its metric relations outside it, in binding forces

2 **On Avatars.** From (Gouyon et al., 2002; pp. 154-5), a well-known text book on neo-Darwinian Evolution: “To denote that which transmits genetic information or its physical carrier, we use the term avatar borrowed from the Hindu religion; it alludes to the physical forms adopted by the god Vishnu on his visits to Earth ... The avatar, as noted by J. Damuth, interacts with the environment which provides for its needs and exerts an influence upon it but, above all, the avatar is produced by genetic information to ensure that this information is passed on. *Individual organisms easily meet this definition.* They interact with the environment, are produced by genetic information, and copy the information Selection targets only genetic information, *avatars are mere vehicles.*” [Italics added].

3 A. Danchin (2003; 2009) is one of the few biologists who tried to search rigorously for compilers and operating systems in DNA, while exploring even a possible genetic meaning of Gödel's theorem (see the appendix on “gödelitis” at the end).

4 For example, the “natural” (integer) numbers are naturally isolated. Instead, on the continuum of the real number line, the discrete topology is surely not “natural”: all maps are continuous on it and no relevant mathematics can be done with this. The so called “natural topology” on the real line is usually considered the “interval topology” (or metrics); it is “natural” as it is derived from classical measurement in physics, which is always an interval (classical, and relativistic, measurement is approximated, it is given as a continuous interval, by principle – no jumps, no holes). “Naturality” can also be defined in general Category Theoretic terms, see (Asperti, Longo, 1991).

which act upon it.» (p. 12). In other words, in a discrete, complete manifold, the metric relations are intrinsic, as each point is “naturally” isolated, and one can just count them⁵. In a continuous one, instead, one has to set a metrics, a scale for measurement - and may also count the number of measurements, of course. Moreover, Riemann dares to conjecture that the metrics (and, thus, the curvature of space that he had correlated to the metrics by one of his fundamental results) must be grounded on the “forces acting upon it”. Einstein will understand gravity, as a *cause* of falling bodies, by identifying it to inertia in curving Riemannian spaces, whose metrics (and curvature) depend on the energy-momentum tensor. This greatly contributed in starting a new trend in the understanding of causality in physics, a far from shallow issue, which not enough analyzed in biology, in this author’s opinion.

Interlude: On Continuous Symmetries and Causality

By the unification of inertia and gravity, in Relativity Theory one may say that a body falls for “symmetry reasons”, since inertia is a conservation property (of momentum) and, thus, it may be viewed as a continuous symmetry in the equations, by Noether's Theorems, (Kosmann-Schwarzbach, 2010) - momentum is invariant as for space translation symmetries and energy as for time translation symmetries. Then, following Einstein's idea, enriched by Noether's and H. Weyl's work, XXth century physics largely replaced causality by “symmetry properties”, as extensively discussed in (Bailly, Longo, 2011). In short, physics gave meaning to causality in a broad theoretical frame and could even drop the references to “causes”, far away from common sense, by treating them as an aspect of conservation properties. These are understood as *continuous* symmetries and their groups (more conservation laws and symmetries governing physics could be mentioned: from TCP to the “supersymmetries”, see (Brading, Castellani, 2003) and below for the quantum “discrete” case). It should be clear that there is no ontological nor absolute commitment here: we just discuss how we understand (or, better, organize) natural phenomena by different mathematical tools, either discrete or continua. Their naïve use contributed, in particular, to ... misleading research directions in cancer biology, as we will claim.

Note that, so far, in biology it may be wiser to preserve a “causal” terminology, possibly embedded in a broader theoretical context, beyond the common sense reference to causality. A tentative step in this direction has been made in (Longo et al., 2012), by insisting on the notion of “enablement”, and more generally by the principal frame proposed in (Soto, Longo, Noble, 2016). Typically, it may be still fair and useful to claim that “staphylococcus aureus *caused* pneumonia”, but a good doctor should also analyze what *enabled* the bacterium to reproduce (with variation, its “default state”, see (Soto, Longo, Noble, 2016)), leading to a “pathological” state (all delicate notions). This enabling context may be due to an inflammatory state of the lungs, an immunodeficiency, a stress condition

As for the analysis of the discrete vs. continuous mathematics in understanding causality, one has to distinguish, as we do here, the epistemological issue (the analysis of causality) and the modeling problem, i.e. the use of continuous mathematics vs discrete computational tools in modeling - see (Lesne, 2007) for a broad insight into the *mathematical modeling* of physical dynamics by continuous vs discrete mathematics. Of course, the two issues are related, as soon as one addresses an epistemological analysis of modeling techniques, by a critique, say, of the ontological assumptions often implicit in philosophically naive mathematical modeling (i.e. the view that the model is “objective” or it is intrinsic to or it coincides with “reality”). As observed in (Lesne, 2007), “discrete objects are not really more “objective” than an arbitrary chosen partition of the space in cells”. At most, a relative objectivity may be given in terms of pertinent continuous vs discrete *or* scale symmetries (Longo, Montévil, 2016), whose “naturalness” may be

5 Typically, there are no accumulation points, that is no actual limits points for a converging series, or operations converging to the limit make no sense.

suggested by the fixed physical scale of measurement. As a further, but dual, link to causality, in t(Longo, Montévil, 2016) we show that, in all existing physical theories, each random event corresponds to a (continuous or discrete) symmetry breaking and to time irreversibility.

In summary, in contemporary physics one may understand causality within (or even replace it by) the broad frame of conservation laws. These are mathematically given as *continuous symmetries* in the intended descriptions, possibly by equations (Lie groups are the mathematical tools for their analysis). Of course, this story begun with Galileo's notion of inertia and the later associated transformations, as a continuous symmetry group preserving the laws of physics under changes of reference system. In modeling and simulation, when discrete phase spaces and computations are involved, symmetries are given and broken differently. In this case, as for conservation laws in equations, everything changes and their understanding, approximation and convergence pose major mathematical and practical challenges, see (Gorria et al, 2013). In short, the analysis of causality is in principle lost and it is very hard to reconstruct it.

James Jeans, a major (quantum) physicist of the early XX century, said it very crudely: “when discontinuity gets in, causality gets out”. A discrete manifold is totally discontinuous or totally disconnected: its scattered points have no topological connection with each other. In this perspective, the technical discussion in the Interlude above may be informally summarized as follows. We seem to understand causal relations either by direct *contiguity* (Aristotle's notion of continuity, thus bumping balls) or in a *field* with a pertinent conservation law (this motivated Einstein and Weyl's work, (Brading, Castellani, 2003)).

Note that Quantum Physics and its indeterminism are presented in space and time *continua*: “discrete” structures appear in the dimension of energy (or in the dimension of Planck's h , an action, i.e. energy \times time). Typically, the energy spectrum of the bound electron is discrete, a true surprise in 1900, while the free electron has a continuous spectrum. As a special case of quantum indeterminism, 0-1 discrete alternatives may also result at measurement, such as the spin-up or spin-down of an electron; then the “standard” interpretation consistently and audaciously claims that this event “has no causes”, it is pure contingency – thus, “causality gets out”. From Einstein to Böhm and De Broglie, some physicists rejected this interpretation and many still search for “hidden variables” or hidden causes varying in an *underlying continuum*. These scientists hoped that hidden causes (hidden variables in continua) could also justify quantum entanglement, that is, probability correlations in measurements of remote events (Jaeger, 2009). Note that entanglement is yet another phenomenon that prevents from attributing to quantum space-time a discrete structure, as well separated small boxes of the size of Planck's length, say. By entanglement, quantum observables cannot be “separated” by measurement (there are instantaneous probability correlations, even at a distance). Thus, we are particularly far from the discrete topology, made of isolated, totally disconnected elements, sitting in well separated neighborhoods.

In other words, discrete structures or discretized events provide an *a-causal* image of the world, far from physics (and not justified by Quantum Physics). In a “naturally” discrete manifold, the key issue of measurement, as the only form of access we have to phenomena, is set aside: both classical approximated measurement (an interval in continua) and the challenges of quantum measurement are forgotten (non-commutativity, indetermination, entanglement). Digital databases are accessed exactly, a non-trivial technological achievement in actual computers, and the causal relations are replaced by discrete dynamics of “information” encoded by digits; these dynamics follow formal rules or instructions on how changes of digits have to take place, that is it obeys a “program”. These replacement or re-writing rules (replace a 0 by a 1, or vice versa) physically function according to hidden flows that act on discrete structures, that is, by varying on underlying continua. But, then, how does a digital computer actually work?

2.2 Computational dynamics

Modern computers are based on a fundamental idea by Turing (1936): namely, the split between software and hardware, as for the *elaboration* of information. The autonomous science of software or of programming was then born from Logic, thanks to Turing, Gödel, Church and a few others, jointly to some fantastic areas of great mathematical rigor and achievements (Computability Theory, Proof Theory, Type Theory, by which the author of these lines earned most of his living). The core idea is that programming and its science is independent from the hardware⁶. Similar conclusions can be drawn from Shannon's theory of *transmission* of information (1948): its analysis is independent from the material structure for the transmission (cables, waves, drums ...).

Thus, programming may be identified with a general form of “term (re-)writing: programs are an alpha-numeric writing of instructions on how to transform or re-write alphanumeric strings into new alphanumeric strings (Bezem et al., 2003), a space and time discrete dynamics. In computer networks, distributed in *space-time continua*, this presents some peculiar difficulties adequately dealt by the difficult mathematics of concurrent and network programming. This is based, when needed, on continuous dynamics of complex structures (Baccelli, 2016a; 2016b); yet, computers' network are still grounded and implemented in discrete data bases by term re-writing, as the nodes are digital computers (Aceto et al., 2003). Moreover, if one looks closely into today's computer's hardware, the instructions that modify a discrete (possibly digital) data type actually work by variations of electric tension's levels *in continuous fields* and/or by driving electric currents *in continua* into two stable states, throughout discrete thresholds. That is, in silico, continuous dynamics undergo “critical transitions” and through various sorts of switches, that stabilize current or no current states in a material component of the hardware (the 0 and 1 at the base of digital computing). So, physical causes still refer to continua, yet the physical structure of computers displays only a discrete *interface*, as “bits” or “pixels”, where causality is hidden and only the writing and re-writing system appears (the changing 0 and 1's). This is an amazing technological achievement: by a fine engineering, one may forget the underlying physical hardware and its continuous flows and just consider, and work at, the discrete software processes.

I would dare to say that this discrete visible creation of ours, a programmed dynamic on a computer screen, is as important and as far from the world as the invention of the alphabet, some 5.000 years ago in Mesopotamia (Herrenschmidt 2007). At that time, as paleo-anthropologists claim, humans first discretized the continuous flow of language, originally a song, by strings of meaningless signs. Indeed, modern digital computers are the latest advancement of that atomistic invention of ours, which cuts the flow of language into a discrete notation: this is their “linguistic” origin. Yet, today, the alphabetic writing, once static, *moves* on a screen: it is not only written, but it is automatically *re-written* according to written instructions. Causality gets out from the image of the world that is proposed on the screen of digital re-writing machines, as it is hidden by a cascade of major technological inventions, separating software from hardware. We see only pixels, re-written from other pixel, 0s transformed in 1s and vice versa, following exactly-defined instructions in a discrete structure, with no idea for the biologist nor relevance for the computer scientist of how this is physically obtained. This is a fantastic accomplishment for the science of software (Theory of Programming), which has been broadly developed, independently of the hardware support and its causal dynamics. However, the analysis of a causal structure may be relevant in the natural sciences (e.g. one searches for the “causes” of cancer), possibly even to exclude causes, as standard quantum physics dares to do (the a-causal nature of the spin-up or down of a quanton mentioned above).

And here is another fundamental feature of discrete computations and information technologies: any set of isolated points can be (isomorphically) encoded just in one dimension - a *sequence* of 0 and 1's suffices, that is discrete data and computations are insensitive to dimensional coding. This is

6 Note that a major difficulty in realizing, concretely, Quantum Computing is due to the constraints that the physical theory (thus, the hardware) imposes to programming and to the unavoidable blend of hardware and software: e.g. measurement, which co-constructs the quantum state, and entanglement have key programming (software) consequences. And these are major challenges well beyond current information theories and technologies.

essential in order to write Turing's Universal Machines and, thus, today's operating systems and compilers: they are encoded like programs and data, all in the same, unique dimension, the "Type" (or dimension) of integer numbers. The expressiveness of computing is based on the self-referential power of recursion and compiling, all encodable in the one-dimensional Type of integer numbers, an invention by Gödel, Church, Kleene and Turing, in the '30s, and a key tool also in generalizing recursion theory to all countable types, (Kreisel, 1982). This feat has been obtained by computing's insensitivity to dimensions (and to codings, modulo some minor, linear, coding costs).

Once again, these are very effective tools, but may yield a totally distorted image of the physical and biological world⁷. Typically, everything changes in physics and, a fortiori, in biology as well when changing dimensions: from the dimensionality of energy vs. force, say, to the description of waves' propagation, heat for example, dimensional differences are crucial, in physics; in biology, if one forgets dimensionality then misses the bodily material structure of organisms, which necessarily has three space dimensions⁸.

In conclusion, the informational/computational approach diverted for too long the attention from the rich networks of causal and enablement relations, within an organism and an ecosystem, in favor of an instructional *a-causal* perspective. A change in a phenotype *must* derive from a change in the instructions that are encoded in discrete data types which may totally bypass the physico-chemical causal structure or even force a wrong one (see below). Moreover, by the loss of relevance of the dimensional analysis and the split software/hardware, this approach misses the *proper dimensionality* as well as the *radical materiality* of biological entities. These are made of their specific matter: the bases of DNA, the molecular components of membranes have no physico-chemical alternatives, in a space that we strictly understand in three-dimensions. There is no way to transfer the biological "information" in DNA on Lego, like in the toy Turing Machine constructed in homage to Turing in Manchester in 2012, and have it work for ontogenesis. Synthetic biology extracts and re-combines fragments of DNA, or their exact chemical replica, and places them in cellular membranes with their proper physico-chemical and dimensional structure. The dualistic perspectives, software vs. hardware, or soul vs. body, a fantastic invention for the purposes of computing with machines, or a strong religious commitment, respectively, constitute a major distortion of knowledge when imported into the natural sciences. They set on fuzzy grounds, for instance, the analysis of the causes of cancer, as we will point out.

3. Strong Consequences of Weak Hypotheses

Once focusing on term re-writing as the programming structure of selfish genes, (physical) causality gets out and the search for coded "instructions" or "recipes" (Maynard-Smith, 1999) guide the analyses of biological phylogenetic and ontogenetic dynamics. So, François Jacob explicitly identified genes with alphabetic writing⁹, while W. Gilbert (1992) claimed that, once fully decoded the human DNA, we were going to be able to encode it in a CD-rom and say: "Here is a human being, this is me". In the same dualistic/mystical vein, Francis Collins, director of the National

7 Wolfram and his followers claim that the Universe may be seen as a (big) Turing Machine (Wolfram, 2013). From this perspective, an apple would fall because it is programmed to fall, like a falling apple on a computer screen. The modern physics of symmetries (see the interlude on Symmetries, in sect. 2.1) is not much affected by these claims. But, for lack of a theory of organisms, the myth that an embryo develops *because* it is programmed to do so has been unfortunately more successful than the unneeded computational explanation of falling bodies.

8 Through "mean field theory", in physics, we know that more than three space dimensions force a mean field and forbid singularities, such as borders, membranes ... an impossible world for organisms. In two dimensions, it is hard to have ducts and their crossing. We thus seem to be fit just for three space dimensions, no more, no less. One dimensional discrete encodings miss or bypass this fundamental aspect of the topological/geometric structures. As a matter of fact, one may claim that "everything "geometric" or spatial is *sensitive* to coding and to dimensions.

9 "La surprise, c'est que la spécificité génétique soit écrite, non avec des idéogrammes comme en chinois, mais avec un alphabet" F. Jacob, Leçon inaugurale, Coll. France, 7 mai 1965.

Human Genome Institute, publicly asserted in 2000: “We have grasped the traces of our own instruction manual, previously known to God alone.”

3.1 Exact Codings

The informational approach to biology transforms into ontologies the images of programming on discrete data types as drawn from common sense understanding – with which science is supposed always to break (Bachelard, 1940), as we did when science moved away from the common sense idea of the sun rising on an immobile Earth or when proposing Relativity Theory and Quantum Mechanics. As a matter of fact, the reference to “information” and “programming” is not scientific, as it does not scientifically apply the fundamental invariance properties of these robust scientific disciplines, such as the computationally very effective split software/hardware and the one-dimensional encoding nor other mathematical invariants proper to information and programming nor the ensuing theorems. Instead, it uses a vague, common sense “transfer” and “weak” meanings¹⁰. Nor it is metaphorical, as metaphors are rich of meaning transfer; that is, they add knowledge by referring to (other) meaningful contexts. The crude, naive dualism and immateriality of these vague references to discrete coding and software is sufficient though to erase the spatiality, materiality, singularity and historicity of the living, which can be always surmised as *this living thing here*, in *this* three-dimensional space, with *this* material body and *this* history.

This specificity of organisms is also hard to be described by the ideal invariance of general mathematics, by the a-historic and generic nature of mathematical objects; this is also shown by the absence of the invention of new mathematical concepts and structures inspired by biology, when compared with the fantastic role of physics in producing new mathematics. And in no way it can be scientifically reduced to the uni-dimensional and immaterial invariance of computer software and its arithmetic coding: these are provably incomplete even as for proving relevant results of arithmetic (Longo, 2011).

In summary, is information used in Shannon-Brillouin sense? Does information refer to Turing-Kolmogorof Algorithmic information theory? Is it always to be viewed as software on discrete data types? In spite of the lack of a scientific specification of what information means exactly, the informational approach was justified by and/or implied several important consequences. First, the molecular structures became the obvious discrete data types and codes for programs and the ultimate information storage for organisms and for all biological dynamics. Then the functional specificity of nucleic acids was supposed to be entirely due to sequences of its bases, as complete codes for the sequences of the amino acids of proteins. Moreover, exact macromolecular specificity, e.g. the *key-lock* paradigm, was *derived* from the analysis of how to elaborate and transmit information: “Necessarily stereospecific molecular interactions explain the structure of the code ... a boolean algebra, like in computers” (Monod, 1970). Chemical and stereo-specificity allow the “oriented transmission of information”, as assumed by Crick's 1958 Central Dogma of molecular biology, (Monod, 1970).

Here are the shared views that still now follow from the information theoretic frame, as summarized in the Stanford's “Biological Information” chapter¹¹:

- i. The description of whole-organism phenotypic traits (including complex behavioral traits) as

10 In a rare attempt to turn these “metaphors” into precise notions, Maynard-Smith (1999), in an extensively quoted paper, explicitly mentions Turing-Kolmogorof (Elaboration or Algorithmic Information Theory) and Shannon-Brillouin (Transmission or Communication of Information), but confuses these approaches in their dual relation to complexity and entropy, see (Longo et al., 2012; Perret, Longo, 2016) for a critique.

11 Philosophy of Biology: <http://plato.stanford.edu/archives/fall2008/entries/information-biological/>

- specified or coded by information contained in the genes,
- ii. The treatment of many causal processes within cells, and perhaps of the whole-organism developmental sequence, in terms of the execution of a *program* stored in the genes,
 - iii. Treating the transmission of genes (and sometimes other inherited structures) as a flow of information from the parental generation to the offspring generation.

As unambiguously synthesized in (Griffiths, 2001, pp. 395–96) “Genes are instructions—they provide information—whilst other causal factors are merely material.... A gay gene is an instruction to be gay even when [because of other factors] the person is straight.”

Under this computational perspective, the informational cascade from DNA to phenotypes is centered on molecular exact (“stereospecific”) interactions, that turns out to be the only way (“it is necessary”) to transmit and elaborate information, as in a re-writing system. The boolean, key-lock model refers to a formal chemistry that may be analyzed in terms of computational re-writing processes: these transform sequences of letters into sequences of letters, following the instructions, in a deterministic and predictable way, plus some unavoidable noise, (Monod, 1970)¹².

3.2 Stochasticity and Novelty Creation

It should be clear that the founding fathers of molecular biology discovered fundamental physico-chemical structures and mechanisms at the core of cellular activity. Yet, their amazing experimental insights and observations, such as highlighting the double helix structure or the allosteric and lac operon mechanisms by J. Monod, F. Jacob and J.-P. Changeux (1961 – 1962), were later embedded into the theoretical frame we criticize here.

The computational approach typically excludes physical stochasticity from being an essential component of gene expression, and, more generally, stochastic and low-affinity macromolecular interactions, whose probabilities depend on the context. This exclusion is contrary to evidence on these chemical phenomena, which dates back to the late '50s – as for the role of Brownian motion in a cell and stochastic gene expression, see (Kupiec, 1983; Elowitz et al., 2002; Paldi, 2003; Raj et al., 2006 and 2008; Fromion et al., 2013; Marinov et al., 2014) for references and contributions. Moreover, since long, chemistry deals with macromolecular interactions in stochastic terms (Gillepsie, 1977). Macromolecules have large enthalpic quasi-chaotic oscillations, they are “very sticky” and low affinities are relevant: they are thus treated in probabilistic terms - see the references above and (Creager, Gaudillière, 1996; Kupiec, 1996) for more on the origin of this debate. In short, the chemical analyses are based on the *global stochastic* behaviour of ensembles of macromolecules and not the individual behaviour of each of these molecules, which remains submitted to the perturbing influence of thermal agitation and other “random” dynamics such as affinities with low probabilities. However, this stochasticity has a different nature from the one dealt with in statistical physics: many molecular types, in a cell, contain “small” numbers of molecules and their behaviour is highly constrained by chemical affinities, membranes, compartments ... and by the biology and the “Physics of Epigenetics”, see below. On these grounds, a recent research track, derived from chemistry, radically departs from the “information-programming” approach, where each gene would act like a Laplacian demon “instructing” molecules, individually, but differs also from purely statistical approaches. The aim is to find a right

12 “Biological specificity ... is entirely ... in complementary combining regions on the interacting molecules” (Pauling, 1987). “The orderly patterns of metabolic and developmental reactions giving rise to the unique characteristics of the individual and of its species ... the shapes of individual molecules allow them to selectively recognize and bind to one another. The main principle which guides this recognition is termed complementarity. Just as a hand fits perfectly into a glove, molecules which are complementary have mirror- image shapes that allow them to selectively bind to each other” (McGraw-Hill Dictionary of Scientific & Technical Terms, 6E, 2003).

coarse graining description for understanding the “regulated” stochasticity of macromolecular interactions in a cell, including gene expression. This is based on a mesoscopic level of analysis, of networks in particular, whose dynamics cannot be derived by the knowledge of the constituting elements and which display “canalized” stochastic behaviors, (Giuliani, 2010). This perspective extends to the macromolecular level Boltzmann's approach by microstates in statistical physics, (Kuznetsov, 2002).

The informational language, instead, constructs an autonomous conceptual universe independent from the underlying physical processes and their causal structure: that is, causes are replaced by information flows, signals, control, ... programs, whose necessary physical support is the assumed exact complementarity of keys and locks, hands and gloves. Of course, some randomness cannot be excluded. Yet, in view of the predictable determinisms of boolean re-writing systems, it is described as “noise” affecting, in particular, evolution: “Evolution originates in noise, imperfections ...” (Monod, 1970). Also in this respect then, the information theoretic terminology is not neutral. In particular, it sets a bias on the understanding of biological variability, adaptivity, diversity: they are (or are derived from) unavoidable noise, usually eliminated from information processing or, whenever possible, averaged out in biology, thus treated by “central limit” theorems like in the more recent approaches in Noise Biology - see (Bravi, Longo, 2015) for a critique. In the programming frame, on top of noise, some have been looking for biological novelty, thus diversity creation, also in Gödel's formal combinatorics of signs (see at the end for a mathematical appendix on Gödelitis, a rather common infectious disease). This is not an idea conceived by extremists, but by a few coherent molecular biologists who consistently search for arithmetic recursion and *logical negation* in DNA coding (they are both needed to encode Gödel's theorem); it is a tentative, more rigorous “DNA as a program” approach that, at least, goes beyond the usual vague, common sense use of “information” and “programming” in biology. It is thus possible to criticize it more precisely.

Thus, concerning biological randomness, which is unpredictability and a component of the production of novelty, information-oriented frames do not need to refer to the complex blend of physical, classical and quantum randomness in a cell: either it is noise in information-elaboration channels or it is ... “pseudo-Gödelian”. Even the Brownian motion is seen as disturbing noise in exact, Turing-machine like, genetic expression. Brownian motion instead, jointly to the enthalpic oscillations of macromolecules, dominates the physical dynamics and the energetic landscape and has a constructive role in both prokaryote and eukaryote cells (see the references above as for stochastic gene expression, an approach harshly marginalized for decades by the informational mainstream; (Richard et al., 2016) presents further experimental evidence). Thus, the stochastic approach highlights a fundamental causal component of bio-chemical interactions in continuous physical dynamics, while “stochastic” transmission and elaboration of digital information would make little sense. Moreover, different forms of randomness, at all levels of organization, may causally contribute to phenotypic changes and to biological stability by adaptivity and diversity (see (Buiatti, Longo, 2013) for the further notion of “bio-resonance” and (Calude, Longo, 2016a) for a survey).

As mentioned above, a close analysis of the physical structure and environment of the cell (the “Physics of Epigenetics”) may provide an understanding of some of the key physical constraints that canalize molecular dynamics. In particular, movements, torsions and compressions of the chromatin fiber structure enhance and control “DNA transactions by an epigenetic tuning of its mechanical and topological constraints”, as stressed in the seminal work by (Lesne, Victor, 2006). More precisely, “steric hindrance, conformational changes at various scales, topological constraints (on DNA and the fiber), elastic properties (of DNA and the fiber), electrostatics” ... crucially contribute to chemical interactions, as those authors observe. In (Cortini et al., 2016) a broad survey of “the physics that governs the three-dimensional organization of the genome in cell nuclei” is presented. The authors also stress that even the terminology of “histone code” is inadequate and it is

so, in our opinion, because of the material and dimensional invariance of the notions of information and code that contradicts these analyses of the physical dynamics in cells. Note also that torsions and elastic deformations are not used to elaborate information in computers (please, do not try with yours) nor, more generally, in the implementation of alphanumeric re-writing systems.

The informational perspectives bypasses or is incompatible with additional physical phenomena in cells, such as the possibly very relevant role of the “super-coherence” of water. This is a Quantum Electrodynamics effect in highly partitioned structures containing water, such as in an organism made of 10^{13} cells; it organizes water molecules by co-oriented spins and accelerates by this the Brownian motion of non-water molecules at constant temperature (Del Giudice, 1983, 1986; Arani, 1995). This enhances the rate of (stochastic) biochemical activity.

In conclusion, the needed physical analysis of macromolecular dynamics requires a complex blend of discrete and continua. Quantum Physics, in a completely different realm (though playing a role also in biology) faces a similar challenge. In biology, the role of molecules, beginning with a fundamental physico-chemical trace of evolution, the DNA, and of their discrete structure is evident. In particular, as a *discrete* template for proteins, the DNA constitute a relatively stable constraint to molecular random movement and formation; it resists thermal fluctuations (Sarpeshkar, 1998), while it uses molecules’ Brownian motion and is “opened” to interactions also by pressures and torsions, all notions that we better understand in continua.

In sect. 7, we will refer to a properly biological investigation of constraints and of unpredictable changes, which uses but goes beyond purely physical notions of constraints and randomness, as for the analysis of both biological stability and novelty creation.

3.3 The Software of Life and reductionism, both away from Physics

In summary, in Theory of Programming, a robust science on its own, but also in the information/programming approach to biology, the underlying hardware has no interest for the program analyst, provided that it works correctly, in spite of some noise. In Computer Science, the needs of Programming set the standard of “correct” working for the physical, material structure, which followed by more than 10 years Turing's mathematical distinction between software and hardware. It is the engineers' job to have the hardware work according to the programmer's needs and, thus, realize an interface appearing as a (Turing-vonNeuman) discrete state architecture, with whatever material structure they have. And they can have it work correctly, which is just fantastic: in modern computers, we implemented the strongest form of Cartesian soul/body split, by radically subordinating matter (hardware) to an independent soul (software). Similarly, the material cell must follow the genetic instructions; it is an Avatar (see the footnote above on Avatars). Yet, the genome may escape from them and generate novelty internally, independently from physics, from the organism and from the ecosystem, by noise in information processing or by implementing Gödel's self-referential encoding of the formal metatheory, a set of instructions on how to diagonalize, by using negation, on alpha-numeric signs (see the appendix on Gödelitis).

When developmental biology follows this extreme Cartesian dualism, it is reduced to purely formal laws of a derived symbolic chemistry, a virtual interface handled in terms of information and programming theory, with a reference to physics in occasional reductionist claims¹³. But, if the causal structure of this presumed formal bio-chemistry of information in macromolecules is absent, doubtful or incomplete, which laws of physics are actually refereed to, in reductionists perspectives in biology?

Physics, from Galileo to Quanta, has never ceased to construct and modify its laws by confronting unprecedented phenomena or by novel insights into known phenomena or just by ... changing the scale of observation. There is *no reduction within physics*, as it proceeds by “unification”, from Newton and Boltzmann to current attempts to unify Quantum and Classical/Relativistic physics or chemistry or hydrodynamics, see (Chibbaro et al., 2015) and (Longo, 2016) for a review. For example, hydrodynamics, as a science of incompressible fluids in continua, is not understood in terms of quanta; physicists try instead to invent a new theoretical frame that could unify these theories (note that there is a lot of water in an organism ... thus, which “physics” are reductionists in biology referring to?). Moreover, classical and quantum random phenomena, which are far from unified, are both present and interact in cells and may have phenotypic effects (Buiatti, Longo, 2013). In physics, all existing *unifications* were based on very strong theoretical hypotheses, grounded on revolutionary ideas. For instance, Newton equations and infinitesimal calculus, which unified Galileo's falling stones and celestial bodies; Boltzmann asymptotic construction of Statistical Physics, which unified particles' dynamics and Thermodynamics on the grounds of the ergodic hypothesis, an incredibly strong and precise statement; String Theory or Non-Commutative Geometry, as for today's attempts to unify quantum and relativistic fields by incredibly strong, revolutionary assumptions and concepts, surely not derived from common sense. And none of these is a “reduction” to a “lower” level. Moreover, as it is in the two latter cases above, unification, in science, should always be provisional and “local,” not dogmatic and a priori reductionist, but constructed as a new theoretical frame. It may be a long way to work at unifying frames of biological analyses and of relevant physical theories, since even the analysis of molecular dynamics requires original physical treatments, as those hinted in the previous (sub-)sections, as for stochasticity, for example.

The deduction of strong consequences from weak, fuzzy, a-scientific, vaguely metaphorical or “common sense” hypotheses, such as the “information” or “programming” assumptions in biology, is unacceptable as a scientific praxis. Note finally that, the pre-scientific reference is only made to a Theory of Information on discrete data types, elaborated, transmitted and encoded by programs, written as alpha-numeric instructions. No reference is ever made, that I know, to the well-established discipline of Geometry of Information, where symmetry changes in possibly continuous symmetry groups propose a radically different conceptual frame (Barbaresco, Djafari, 2015).

In addition to the few listed above, we will see some specific strong consequences of the weak hypotheses transferred from common sense notions of “information” to biology and how these still affect cancer research. This domain has been for too long dominated by the myth of the computer program, centralized in the DNA (the Central Dogma of Molecular Biology): the focus on information-program-signal, as drivers of development, supports the idea that ontogenesis as well as its pathological developments should be always or first studied as a DNA centered, programming issue. In this context, cancer has been consistently analyzed as the result of DNA *de-programming* either inherited or *provoked by a carcinogen* disrupting the DNA *encoded instructions* (the mutagenic effect of carcinogens). Let's briefly summarize some steps of this still prevailing view of the etiology of this life-threatening disease, a view that recently received further support from the software industry, in spite of massive negative evidence.

4. An announced debacle

“... you cannot prove a vague theory wrong”
Richard Feynman (1964)

We will follow the story of a wrong path as courageously acknowledged by one of the founding fathers and major actor of the dominating theory, in biology of cancer, R. A. Weinberg, in his

2014's paper (see references). The so called Somatic Mutation Theory (SMT) postulates that cancer originates as a one-cell disease, it is then clonal, and is due to one or more (*driver*) mutations. These would allegedly be either induced by a carcinogen or inherited - see (Nowel, 1976, Cairns, 1981; Strauss, 1981) for classical surveys of this century-old theory originally proposed, in a different language, by (Boveri, 1914).

Since 1971, generously funded projects have heralded the final victory against cancer thanks to genetic therapies able to “reprogram” the “deprogrammed DNA”, within a few years. In particular, this approach was at the core of President Nixon's War on Cancer (see below for more quotations on this). The common sense notion of “program” was indeed understandable also by Nixon; a major advantage of using an everyday, a-scientific language, as it facilitates the understanding of the message by everybody. Moreover, programs can be debugged, thus the promise of genetic therapies as DNA debugging, iterated till now (see below): an easy to understand, short path to therapies. In spite of providing neither therapeutic solutions nor plausible explanations of the carcinogenic process, since 1971, a major technological achievement, by the year 2000, i.e., the complete decoding of human genome, was seen as a further tool to solve the cancer puzzle and generate, once again, genetic therapies. These had to be expected at latest within 10 or 15 years, while sound diagnosis and prognosis were promised much sooner, on the grounds of newly uncovered fundamental “hallmarks” of cancer. Genetic analysis of cancer cells should have provided diagnosis of malignant vs. benign forms of this disease, primary vs. metastatic cancers etc. These optimistic papers are too many to be listed; it may be enough to quote (Collins,1999), by the head of the Genome Project, (Hanahan, Weinberg, 2000) (over 20,000 quotations in a few years), (van Eschenbach, 2003), all major personalities in the field. In (van Eschenbach, 2003), cancer is viewed both as “a genetic disease and a cell signaling failure. Genes that control orderly replication become damaged”; on the grounds of this causal analysis, the paper promises, by 2015, genetic therapies for “eliminating suffering and death due to cancer”. Incidentally, this claim was supported by the American Association for Cancer Research in 2005.

Thanks to the full knowledge of DNA sequences in normal and cancer cells, these proposed upcoming therapies were supposed to be based “on scientific laws as robust as those of chemistry and physics” (Hanahan, Weinberg, 2000). The proximity of metaphors of “programming” to common sense, as always, promoted these promises among funding agencies and the general public. The enormous financial efforts and the ruthless exclusion of alternative hypotheses have both been motivated for decades by the idea that any phenotype, including “pathological” ones, is determined by the genes, or their mutations. However, a half-century of genetic research has produced no plausible gene-based cancer therapy, see (Baker, 2014; Huang, 2014) - two elegant syntheses and highly recommendable reading to the non-biologist (but so worrying!). As Weinberg (2014) himself acknowledges “We were, after all, reductionists, who would parse cancer cells down to their smallest molecular details and develop useful, universally applicable lessons about the mechanisms of cancer development ... Half a century of cancer research had generated an enormous body of observations about the behavior of the disease, but there were essentially no insights into how the disease begins and progresses to its life-threatening conclusions”. So, Weinberg (2014) observes, against the extensively quoted (Hanahan, Weinberg, 2000), that “a particularly jaundiced cancer researcher” commented to him that “one should never, ever confuse cancer research with science!”.

How could DNA be de-programmed according to the early research projects? At the beginning of the 1971 War on Cancer, retroviruses were considered as DNA de-programming agents. “Few seemed deterred by the well-established observation that most types of human cancer did not represent communicable diseases” (Weinberg, 2014). Ramazzini, anatomist and physician in Bologna had already made this observation in early XVIIIth century.

Weinberg continues his auto-critique (pp. 267-9) by summarizing further spurious key steps in the

SMT approach to cancer. Since 1973 the search focused on “chemical species correlated directly with mutagenic activity”. He then recalls the progressive move, between 1982 and 1999: from “just one mutation” to “a specific sequence of mutations”. “Only later was it clear that most human carcinogens are actually not mutagenic ... but fortunately I and others were not derailed by discrepant facts” (sic).

This is a crucial remark. As a matter of fact, there is increasing evidence that many (most?) carcinogens interfere on tissue organization, not by sending (chemical) signals that de-program DNA. For example, Maltoni (1980) observed the disruptive role of asbestos micro-filaments on the tissue matrix, on cell connections and membranes, but could not point to any direct mutagenic effect. This observation was in contrast with the claims of the dominating SMT and, hence, received little consideration. As a matter of fact, when asbestos is made into powder, it ceases to generate cancer: “fiber dimension is one of the important determinant factors of asbestos carcinogenicity” (Huang et al. 2011). Also, by subcutaneously inserting diverse inert objects (plastics, metals, etc) it has been shown that their carcinogenic effects depended not on their chemical make up but on their peculiar physical structure (e.g. the carcinogenic effect may depend on the presence and size of micropores in plastic membranes, a fact known since (Karp et al., 1973)). Of course, mutations will massively follow as consequences (passenger mutations) not causes (driver mutations) of cancer, as we will recall soon.

Other commentators of note have expressed their views on carcinogenesis for the record. In a very interesting interview, Venter (2010), whose team first decoded the human genome in 2000, acknowledged that “We Have Learned Nothing from the Genome”. Wrong expectations were due to “the ill-founded belief that those who know the DNA sequence also know every aspect of life ... That is nonsense”. However, cancer biologists did learn something from the Genome Decoding. The extensive decoding of the DNA of cells in cancerous tissues showed that, in the same tissue, cells may have very different mutations and chromosomal changes: “Genome sequencing also came of age and documented myriad mutations afflicting individual cancer cell genomes” (Weinberg, 2014). More precisely, “63 to 69% of all somatic mutations [are] not detectable across every tumor region ... Gene-expression signatures of good and poor prognosis were detected in different regions of the same tumor” (Gerlinger et al., 2012), see also (Kato et al., 2016). No much help came from genomics in the analysis of metastasis either, as acknowledged also by proponents of SMT: “Despite intensive effort, however, consistent genetic alterations that distinguish cancers that metastasize from cancers that have not yet metastasized remain to be identified ... The idea that growth at metastatic sites is not dependent on additional genetic alterations is also supported by recent results showing that even normal cells, when placed in suitable environments such as lymph nodes, can grow into organoids, complete with a functioning vasculature” (Vogelstein et al., 2013). In the interpretation hinted in the next section, normal cells in a context that cannot control and canalize their “normal” reproduction with variation may yield a “pathological” situation. Moreover, no driver mutations specific to metastasis have yet to be documented (Zhang et al., 2013; Alshaya et al., 2014; Versteeg, 2015).

Finally, it is remarkable that cells in healthy tissues may have the genetic hallmarks of cancer: “aged sun-exposed skin is a patchwork of thousands of evolving clones with over a quarter of cells carrying cancer-causing mutations while maintaining the physiological functions of epidermis” (Martincorena et al., 2015). Equally noteworthy is that cell aneuploidy and polyploidy, that used to be considered as another chromosomal signature of cancer are present in 50% or more normal liver cells and are considered to be beneficial by assuring resilience to toxic shocks and for liver regeneration (Duncan, 2013).

Following the quotations referred above, a few relevant facts have become clear from the massive DNA decoding of cells in cancer tissues. They are:

1 - Gene-expression signatures for benign and malignant cancer may coexist in the same tumor.

- 2 - Genetic analyses do not allow to discriminate between a tumor that (has or) will metastasize(d) from another that (has or) will not.
- 3 – DNA sequencing does not help in distinguishing a primary from a metastatic cancer.

Note that 90% of lethal cancers are metastatic (Sporn, 1999; Cook, 2011). This stresses the relevance of the last two points. Of course, the etiology of cancer remains open, that is, the origin of primary cancers. Yet, proponents of SMT acknowledge that 99.9% of mutations found in cells of all cancer tissues are passenger not driver mutations of cancer, see (Vogelstein et al., 2013) and the next section¹⁴. So, in a more than vast majority of cases, many seem to acknowledge that the “primary and immobile motor” of ontogenesis (and thus of cancer as of any phenotype), DNA as a program, becomes a passive recipient of orders (resulting in passenger mutations). Of course, the messy situation of cells' chromosomes in a cancer (not just mutations, but massive polyploidy, aneuploidy, etc) may negatively retro-act on tissues' healthy dynamics: their deregulating effects may even further disrupt the cells' dialogue, hormonal control of reproduction etc. see the next section and (Sonnenschein, Soto, 1999, 2011; Baker, 2014, 2015; Huang, 2014) for surveys.

In view of the remarkable empirical knowledge that DNA decoding has provided, are we approaching the end of a (de-)programming DNA centered view of cancer and of ontogenesis in general? Hopefully, empirical negative results in the natural sciences should have the same role as “negative results” in mathematics or mathematical physics: in principle, they should modify scientific thinking and scientists may become more open to or invent new theories, new scientific paradigms (Longo, 2010). To the contrary, the genocentric informational/programming views cannot be falsified by experience, because they are not scientific: those views are based on common sense notions of information and program and on the “homunculus” ancient myth, modernized by encoding it in chromosomes. Thus, the massive presence of mutations and chromosomal alterations in cancer tissues continues to be perceived as *the cause* of the disease, since according to that theory any phenotype must have an antecedent in the genotype and the genotype is supposed to completely control the organism-avatar. We know from human history that when common sense and myths combine, they are invincible or any change requires a true revolution.

Following the trend, Microsoft proposes to help in solving the cancer puzzle by its technical (or commercial?) skill in software production: Microsoft's “computing cancer project” (Microsoft, 2016) claims that one has to understand how the cell's programs work, then “If you can figure out how to build these programs, and then you can debug them, it's a solved problem”. Their motto is “Our approach to solving cancer: debug the system”. Is this just surplus money that goes to cancer research? Not necessarily, because joint ventures in this enterprise are meant to apply for funds to research institutions. And, more importantly, Microsoft's talent for commercials and publicity, which are the actual aim of these announcements in spite of the sufferings they refer to, may confirm *common sense* by reaching the general public, politicians and managers who decide about funding; in short, it sets a reference¹⁵. IBM also offers DNA decoding services for cancer diagnosis and prognosis, in spite of the evidence mentioned above. And Big Data enter massively in the game. In view of the very heterogeneous and unexpected genetic situation of cancer cells, of the “myriad mutations afflicting individual cancer cell genomes” thus of “cancer's infinite complexity” (Weinberg, 2014), and of the failure to turn cancer biology into a science, many researchers follow

14 In reference to the percentages mentioned in the last few lines, it may be fair to claim that most publications in biology of cancer (90% ?), in the last few decades, focus on geno-centric approaches and that the vast majority of research funding (90% ?) has been allocated to those analyses. These two aspects of research trends are also the result of the amplifying effects of bibliometrics, that reinforces main stream, fashionable areas (Longo, 2014), and thus enhances positive unstoppable retro-actions between publications and funding.

15 S. Knapton, “Microsoft will 'solve' cancer within 10 years by 'reprogramming' diseased cells”, The Telegraph, 20/9/2016. As a former user, now a Linux fan, I think that Microsoft should better and first debug its own software, see (Di Cosmo, 1998).

(Anderson, 2008) philosophy. Namely, collect all “-omics” available data (genomics, proteomics, metabolomics ...), then “... throw the numbers into the biggest computing clusters the world has ever seen and let statistical algorithms find patterns where science cannot ... Correlation supersedes causation, and science can advance even without coherent models, unified theories ... No semantic or causal analysis is required”. Of course, the larger is the database, the best for prediction and action with no need for understanding.

We are coming full circle back to the more than 100 years old remarks by Riemann, Jeans and others quoted above: if you have only discrete manifolds, give up causality. Thus, consistently claim the purest Data Miners, just look for correlations without explanations – science is no more needed. Note first that these provably wrong claims against theorizing allow to neglect measurement as well: classical, relativistic and quantum challenges as for physical measurement are forgotten – a digital database is exact, the metrics is intrinsic. The pre-given discrete structure of the databases may thus help to forget *how* these data have been collected in complex biological systems. The (often implicit) a priori's in the choice of observables and of their metrics do not need to be discussed, as this would be “theorizing”: in our view, instead, Data are “Compressed Theories” (and not viceversa), as their “collecting” supposes a theoretical perspective (the choice of observables, measurement theory and tools ..., see (Longo, 2016)).

Moreover, as formally shown in (Calude, Longo, 2016), sufficiently large sets of numbers, even when produced by a random process, necessarily contain correlations, which are then spurious. More precisely, a nice and non-obvious combinatorial theory of numbers, Ramsey Theory, proves the following:

(Informal) Set the criteria for a correlation in a database: its n-arity (you want to correlate n variables), the length p of the correlation (you want it to be long enough, e.g. n data must correlate every minute, for a year, say), the number c of parts you divide your database (you give the same “color”, say, out of c colors, to numbers that you consider correlated: they are close or happen simultaneously or whatever). Then, for *any* n, p and c, one can compute a number, d say, such that *for any* set A with d or more elements and *for any* partition of the n-uples in A in c colors, there exists a subset B of A that contains p elements and is monochromatic, i.e. it is entirely contained in one partition – thus B realizes the correlation given by n, p and c.

The number d above is truly “huge”, but isn't the larger the best? Then the data miner may happily exclaim: “we have got a correlation!”, even when ... the data set A has been produced by a random generator. That is, in any immense numeric databases one has a deluge of spurious correlations, in a very strong sense, as the set A and the partition of A above are *arbitrary*. Thus, A may have been obtained by ... throwing dices, flipping coins, quantum measurements ... and by arbitrary choices of observables and measurements. It is hard to predict and act on these grounds. Moreover, when you are dealing with very large sets of numbers, most of them are “random”, in a precise sense (Calude, Longo, 2016). It may be wiser, then, to try some scientific theorizing.

5. Towards TOFT

Following a different research path, an approach proposed by cancer biologists Sonnenschein and Soto (TOFT, Tissue Organization Field Theory, see the references by these authors) is based on Darwinian principles that we further extended to a tentative theory of organisms (see the next section). The TOFT approach to cancer refers to early intuitions by C. Waddington, J. Needham and a few others (1930s), later forgotten by the subsequent genocentric perspective (see (Sonnenschein,

Soto, 2011) for references). The novelty and the suitable “paradigm instability” brought in by TOFT vs. SMT is analyzed in (Baker, 2014; 2015) and (Smythies, 2015).

TOFT key principle is that all cells, including somatic cells, tend a priori to reproduce: in (Sonnenschein, Soto, 1999) terminology, *cell proliferation* and *motility* is the “default state”. We extended this default state to the idea that all organisms as well as the cells in multicellular organisms, tend to reproduce *with variations* and to move, as more closely spelled out in the next section. This is an extension to cells within an organism of Darwin's principle of heredity in evolution as *descent with modification*, which occupies three out of the first six chapters of the Origin of Species (see Longo et al, 2015; Montévil et al., 2016) . This revolutionary principle is essential to Darwin's second principle, *selection*. It is a “limit-state” analogous to Galilean inertia, but specific to life forms. Note that inertial movement is a *limit* principle, as it is always constrained and modified by gravitation and frictions. Analogously, somatic cells, and also organisms in an ecosystem, are constrained/controlled by the organism or the environment in their free reproduction and movement. As Darwin observes, an unconstrained organism would quickly cover the entire Earth, by reproduction. Galileo's inertia, Darwin's principles and the default state of reproduction with variation and motility are all derived from observation and posed as principles of intelligibility at the core of their theoretical approach. By positing inertia, asymptotically (no physical body moves like a point on an Euclidian straight line at constant speed), Galileo could analyze what affects it, gravitation and frictions. On the grounds of his first principle, Darwin could propose selection as acting on organisms. TOFT central idea then is to analyze what controls cell reproduction with variation and motility in an organism (see (Longo et al., 2015; Soto et al., 2016) for more on Darwin and the conceptual analogy with Galileo's principle of inertia). Under this perspective, cancer is a tissue-based, organismal problem, akin to the process of morphogenesis during development: “cancer is development gone awry” (Sonnenschein, Soto, 2011).

In summary, within an organism, when effective control by intercellular exchanges, tissues matrix, hormones, etc. is disrupted by a carcinogen, cells reproduce and change at a speed that may even reach that of embryogenesis. This less constrained reproduction, in turn, modifies the micro-environment, it actually *complexifies* it in a precise histological sense, while *reducing* tissue (organ) functionality, an hallmark of cancer as observed in (Longo et al., 2015). Note that, in contrast to the claim by the SMT that “once a cancer cell, always a cancer cell”, cells from a mammary carcinoma (an epithelial cancer), when placed into a normal mammary stroma (the normal micro-environment of the mammary epithelium) revert to normalcy (Maffini et al. 2005). The idea is that cancer does not depend on a “triggering signal” at the molecular level, which would deprogram the DNA of an *a priori* quiescent cell by inducing a driver mutation and enhancing reproduction. Instead, cancer can be considered as the failure of the regulatory relations between and of cells in a tissue and of the tissue in an organism. Passenger mutations massively follow (also for SMT supporters, they are 99.9% of mutations in cell in cancerous tissues, see above), as mutations are one of the main ways to generate variation at the cellular level.

These hypotheses, and their therapeutic consequences redirect the attention of researchers toward prevention and modifications of environmental conditions. At the ecosystemic level, the focus is on endocrine disruptors and other causes of cancer (Soto, Sonnenchein, 2010). At the organismal one, the reconstruction of the cells' micro-environment may be crucial, (Cook et al., 2011; Bizzarri, Cucina, 2014). In the latter case, like in the recombination experiments in (Maffini et al, 2005), cells inside a cancer can be normalized. The reader should consult (Bizzarri, 2013; Baker, 2014; Smithies, 2015; Pisco, Huang, 2015) for surveys. Moreover, “Thinking in terms of TOFT can spur new lines of research” (Baker, 2015), as many if not most cancer “conundra” are made

understandable along these new lines of thought, (Kato et al., 2016)¹⁶.

6. From TOFT to Working Hypothesis in Biology of Organisms

In our approach, we take on board the rich methodology of knowledge construction proper to physics (such as: set strong principles, starting from but well beyond observations, see below), but not necessarily the tools and theories from physics. Yet, we may locally take on board physical analysis at the molecular level, without excluding them as done for too long by the computational approach (see sect. 3.2). In two books (Bailly, Longo, 2011; Longo, Montévil, 2014) and in several papers, we tried to articulate physical and mathematical knowledge (methods and concepts) with phenomena that are specific to life and worked on some specific “perspectives” on organisms (rhythms, biological time, criticality ...). We then joined the efforts of our colleagues, Sonnenschein and Soto towards the proposal of a “theory of organisms”, introduced in (Longo et al 2015) and summarized in the volume (Soto, Longo, Noble, 2016), in particular in both (Soto et al, 2016) papers. In that perspective, DNA is considered as a fundamental, internal “constraint” to cellular and biological activity, where we used constraints in the sense described in (Montévil, Mossio, 2015; Mossio et al., 2016). That is, DNA is a physico-chemical trace of an entire history (Longo, 2017), continually used by the cell dynamics, and thus constraining it to certain proteomics, according to the context. It sets boundaries to the proteome's Brownian motion, under the physical constraints and active canalization mentioned in sect. 3.2, possibly enhanced also by the quantum effects we quoted. In this theoretical frame, (Montévil et al, 2016b) modeled mammary gland morphogenesis by the dynamics of constraints that, generated by the cell agency, organize the surrounding tissue matrix, which in turn, constrains the proliferation and motility of the cells. Mathematical modeling in biology should *follow* a sound theoretical approach and not be based on the passive transfer of tools from mathematical physics. This is how physics produced new mathematics, from Newton to A. Connes, in recent years, as it never happened in mathematical biology.

Our perspective goes back to Darwin, whose greatness is to have formulated autonomous and strong theoretical principles of intelligibility for phylogenesis, on the principal model, but not by the techniques, of the major creators in physics. As mentioned above, the two Darwinian principles of evolutionary heredity are *descent with modifications* and *selection*. The ongoing challenge is thus to articulate these principles with the analysis of the organism, in the long-term attempt to unify ontogenesis and phylogenesis.

The role of strong, explicit principles in mathematics and physics is crucial. Their role also in biology may be explained by two fundamental principles in mathematics and physics; they happen to be also “limit” principles, a status proper also to the Darwinian “default state” of organisms (reproduction with variation and motility (Soto, Longo, Noble, 2016)).

In (Longo, 2015), from which this section is partly borrowed, Euclid's “line with no thickness” (a definitional principle made explicit in definition β , book I) and Galileo's principle of inertia are extensively discussed. They are limits, that is they are the infinite limit of decreasing thickness and a limit movement, respectively, as well as founding principles for knowledge construction, far away from *common sense*. Our quest for principles in biology follows these examples and Darwin's, while acknowledging that the principles specific to physics—grounded on invariance, conservation properties as symmetries, and optimal trajectories—are necessary but not sufficient for the analysis

¹⁶ Darwinian principles in the analysis of cancer have been extensively used in the literature, see for example (Gatenby et al., 2010; Shiffman et al. 2013). While sharing the principles, we differ as we consider cancer as a tissue based problem, not a cell based one. That is, TOFT stresses the failure in the control of cell reproduction with variation by the triangular relation tissue-organism-ecosystem. In our view, this is more consistent with the role of closure of constraints in biology and to an ecosystemic approach to evolution: genes are more followers than promoters of changes (West-Eberhard, 2003), both in evolution and cancer (see the largely prevailing “passengers” mutations over “drivers” mutations mentioned above).

of the proper observables of living beings, organisms and phenotypes. Living systems are in a permanent state of *critical transition*: their symmetries are continually breaking and being reconstituted, at least at each cell reproduction (Bailly, Longo, 2011; Longo, Montévil, 2014; Longo, Soto, Longo, 2016). In our perspective, Darwin's principle of *reproduction-with-variation* may be seen as a principle of *non-conservation*, opposed to and symmetric with the principles of conservation and invariance in mathematics and physics, but at the level of the appropriate biological observables, that is, of organisms. The adequate theorization of the biological field therefore demands extensions and sums of various physical theories— such as the ones due to the coexistence of both classical and quantum random phenomena in the cell (Buiatti, Longo, 2013), of far from equilibrium dynamics (Nicolis, Prigogine, 1977), of extended criticality (Bailly, Longo, 2011; Longo, Montévil, 2014). These operations rely on physical theories and extend their methods, while remaining irreducible to their mathematical techniques. They propose proper biological principles as well as “points of view,” and “perspectives” on the organism, whose unity furnishes the guiding thread through these different theoretical aspects. The intelligibility of the biological field is only possible through intersections and partial integrations that aim to construct objects-of-knowledge in dialectical relation with the constraints of experience. In biology, experiences plays a singular role, beginning with the difference *in vitro* vs. *in vivo*, unknown to physics, and the peculiar role of historical knowledge and, thus, of diachronic measurement in theory building (Longo, 2017). Unity with physical theories (classical, quantum?) may be a long-term goal, surely not a reduction, as hinted at the end of sect. 3.3.

Thanks to mathematization, theorizing in physics extracts generic objects and properties, out of intentional observations and measurement, as conceptual and mathematical invariants. Their objectivity as invariance depends entirely on the theoretical framework. In biology, instead, objects are always historic singularities, which are grasped by conceptual models that are qualitative, provisional, and over-determined by history and cultural perspectives. The centrality of each singular organism, with its own historicity, implies the primacy of variation and symmetry breaking that overthrow the current mathematical primacy of invariance. This primacy has had very powerful knowledge effects, but it may prove an obstacle to understanding life, especially when it is disfigured in the genocentric approach to DNA and the myth of the “program”, an informational invariant. For example, the radical materiality of organisms that we mentioned, its historical thickness, and the density of its internal and external relations, rule out any dualism between “software” and “hardware” and the associated one-dimensionality of digital information, discussed above. Finally, one of the very conditions of possibility for physical knowledge, the space of phases (the observables and the parameters), is overthrown in biology. In physics, the (phase) space is fixed a priori, a proper one for each physical theory: in classical, quantum, hydrodynamics, thermodynamics ... first pre-define their spaces of analysis, as the Kantian condition of possibility and immanent norm of physical “trajectories”, in the broadest sense. In biological processes, by contrast, the phylogenetic trajectories constitute and constantly reorganize the space of possibles (of phases), the ecosystem. The observables (phenotypes and organisms) are the *results* of the processes. The historicity of life is grounded on these changes of observables and parameters along evolution (phenotypes and pertinent parameters change), and on the key role of *rare events*, a peculiarity of historical processes, (Longo, 2017).

If our analysis of living dynamics is pertinent, it poses the problem of how to test the limits of traditional scientific objectivities, of which physics and mathematics represent the paradigms, when facing biological theorization. Overcoming very powerful theoretical practices that are rooted in old, deep metaphysical and *theological* ideas, (Longo, 2011b), is a radical challenge, but some attempts are seeing the light of day, ours is one of them.

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Mathematical Appendix on Gödelitis. In an attempt to bypass Monod's mechanistic-formal approach, enriched by some noise, Danchin (2003) and (2009) tried to bring Gödel's theorem into the picture. Beyond formalism, Gödel's incompleteness would prove the unpredictable “creativity” of biology within the programming approach. A remarkable attempt for a leading biologist, as these issues in Logic are far from common sense (see (Smorinski, 1978), (Longo, 2010), (Longo, 2011a) for technical references). Indeed, (Rogers, 1967), a classic in Computability Theory, calls “creative” the set of (encoded) theorems of arithmetic, i.e. the formal-mechanical consequences of its axioms. By Gödel's first theorem, this set is not computable (and, to the biologist, the word may recall Bergson's Creative Evolution). Yet, this set is *semi-computable*, meaning that it may be effectively generated and, as such, is far from “unpredictable”, since an algorithm produces all and exactly all its infinite elements. Moreover, the recursive generation of Gödel's undecidable formula is effective as well: it is an incredibly smart recursive and diagonal construction (it uses logico-formal negation), which allows to *construct* a formula not derivable from the axioms. This procedure may be indefinitely and effectively iterated. In short, Gödelian undecidability is effectively produced by an encoding of the metatheory into the formal theory, it does *not finitely “create”* generally unpredictable information as the diagonal formula may be constructed, even though it is not derivable from the axioms (as it also uses the coding of their metatheory). Thus, formal derivability is not decidability, as the “information” in the axioms does not allow to decide all formulae, for example Gödel's diagonal one, yet it is still *semi-computability* or *semi-decidability*. Moreover, it allows to effectively construct that formula and to show that ... it cannot be decided by the axioms. That is, the construction of the sentence that escapes the given axioms is also effective (semi-computable). Theoretical unpredictability, the least property one expects for “creativity” in nature, is at least (algorithmic) randomness (Calude, 2002) and this is far from semi-computability. It is the “opposite” (e.g. a random set of numbers and its complement cannot contain *any infinite semi-computable* subset) and it may be soundly compared to unpredictability in physics (e.g. it mathematically relates to classical ergodicity and to Quantum randomness, asymptotically (see Calude, Longo, 2016a, for a survey)). If creativity, thus unpredictability, were just Gödelian semi-computability and its recursively produced undecidable formula, I would love to have a program generating a semi-computable subset of an unpredictable process, such as future phenotypes or, better, future lottery drawings: this would make me immensely rich. The merit of Danchin's remarks, though, is that they are based on precise mathematical notions, thus they may be proved to be wrong.

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