

Security Proofs using the Game-based Methodology

David Pointcheval

Ecole normale supérieure, CNRS & INRIA



Scuola Superiore di Catania
Catania – Italy
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Outline

- 1 **Cryptography**
 - Introduction
 - Provable Security
- 2 **Game-based Methodology**
 - Game-based Approach
 - Transition Hops
- 3 **Assumptions**
- 4 **Short Signatures**
 - Description of BLS
 - Security Proof
- 5 **Identity-Based Encryption**
 - Definition
 - Description of BF
 - Security Proof
- 6 **Conclusion**

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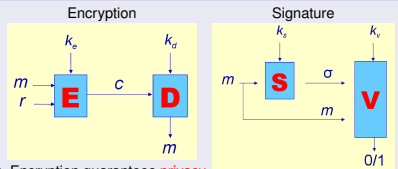
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Introduction

Public-Key Cryptography

Asymmetric cryptography



- Encryption guarantees **privacy**
- Signature guarantees **authentication**, and even **non-repudiation** by the sender

Strong Security Notions

Signature

Existential Unforgeability under Chosen-Message Attacks

An adversary, allowed to ask for signature on any message of its choice, cannot generate a new valid message-signature pair

Encryption

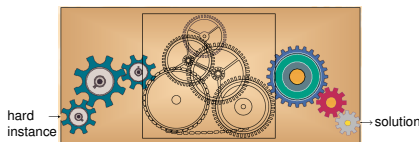
Semantic Security against Chosen-Ciphertext Attacks

An adversary that chooses 2 messages, and receives the encryption of one of them, is not able to guess which message has been encrypted, even if it is able to ask for decryption of any ciphertext of its choice (except the challenge ciphertext)

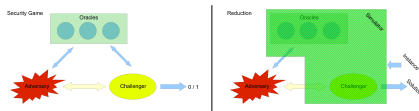
Provable Security

One can prove that:

- if an adversary is able to break the cryptographic scheme
- then one can break the underlying problem (integer factoring, discrete logarithm, 3-SAT, etc)



Direct Reduction



Unfortunately

- Security may rely on several assumptions
- Proving that the view of the adversary, generated by the simulator, in the reduction is the same as in the real attack game is not easy to do in such a one big step

Game-based Methodology

Illustration: OAEP

[Bellare-Rogaway EC '94]

- Reduction proven indistinguishable for an IND-CCA adversary (actually IND-CCA1, and not IND-CCA2) but widely believed for IND-CCA2, without any further analysis of the reduction
- The direct-reduction methodology**

-

[Shoup - Crypto '01]

Shoup showed the gap for IND-CCA2, under the OWP

Granted his new game-based methodology

-

[Fujisaki-Okamoto-Pointcheval-Stern - Crypto '01]

FOPS proved the security for IND-CCA2, under the PD-OWP

Using the game-based methodology

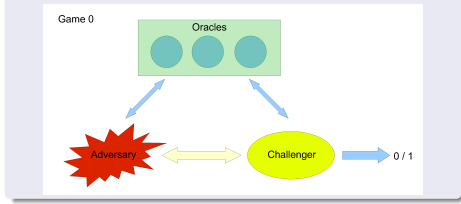
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Sequence of Games

Real Attack Game

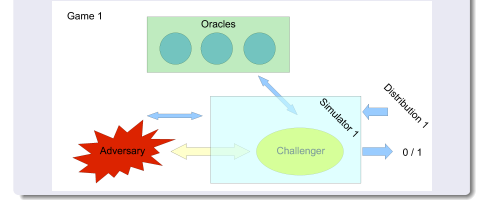
The adversary plays a game, against a challenger (security notion)



Sequence of Games

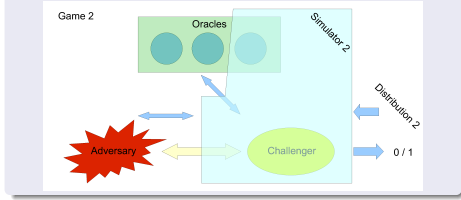
Simulation

The adversary plays a game, against a sequence of simulators



Simulation

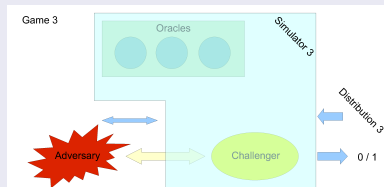
The adversary plays a game, against a sequence of simulators



Sequence of Games

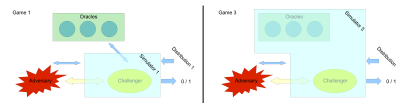
Simulation

The adversary plays a game, against a sequence of simulators



Output

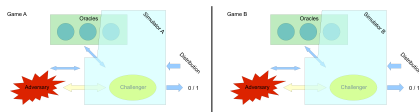
- The output of the simulator in Game 1 is related to the output of the challenger in Game 0 (adversary's winning probability)
- The output of the simulator in Game 3 is easy to evaluate (e.g. always zero, probability of one-half)
- The gaps (Game 1 \leftrightarrow Game 2, Game 2 \leftrightarrow Game 3, etc) are clearly identified with specific events



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Two Simulators



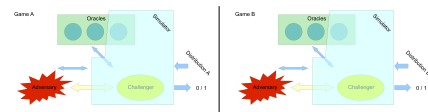
- perfectly identical behaviors
- different behaviors, only if event **Ev** happens
 - **Ev** is negligible
 - **Ev** is non-negligible and independent of the output in **Game_A**
 - Simulator B terminates in case of event **Ev**

[Hop-S-Perfect]

[Hop-S-Neg]

[Hop-S-Non-Neg]

Two Distributions



- perfectly identical input distributions
- different distributions
 - statistically close
 - computationally close

[Hop-D-Perfect]

[Hop-D-Stat]

[Hop-D-Comp]

Two Simulations

- Identical behaviors: $\Pr[\text{Game}_A] - \Pr[\text{Game}_B] = 0$
- The behaviors differ only if **Ev** happens:
 - **Ev** is negligible, one can ignore it
Shoup's Lemma: $\Pr[\text{Game}_A] - \Pr[\text{Game}_B] \leq \Pr[\text{Ev}]$

$$\begin{aligned}
 & |\Pr[\text{Game}_A] - \Pr[\text{Game}_B]| \\
 &= \left| \Pr[\text{Game}_A|\text{Ev}] \Pr[\text{Ev}] + \Pr[\text{Game}_A|\neg\text{Ev}] \Pr[\neg\text{Ev}] - \Pr[\text{Game}_B|\text{Ev}] \Pr[\text{Ev}] - \Pr[\text{Game}_B|\neg\text{Ev}] \Pr[\neg\text{Ev}] \right| \\
 &= \left| (\Pr[\text{Game}_A|\text{Ev}] - \Pr[\text{Game}_B|\text{Ev}]) \times \Pr[\text{Ev}] + (\Pr[\text{Game}_A|\neg\text{Ev}] - \Pr[\text{Game}_B|\neg\text{Ev}]) \times \Pr[\neg\text{Ev}] \right| \\
 &\leq |1 \times \Pr[\text{Ev}] + 0 \times \Pr[\neg\text{Ev}]| \leq \Pr[\text{Ev}]
 \end{aligned}$$

- **Ev** is non-negligible and independent of the output in Game_A , Simulator B terminates, in case of event **Ev**

- Identical behaviors: $\Pr[\text{Game}_A] - \Pr[\text{Game}_B] = 0$
 - The behaviors differ only if **Ev** happens:
 - **Ev** is negligible, one can ignore it
 - **Ev** is non-negligible and independent of the output in Game_A , Simulator B terminates and outputs 0, in case of event **Ev**:

$$\begin{aligned}
 \Pr[\text{Game}_B] &= \Pr[\text{Game}_B|\text{Ev}] \Pr[\text{Ev}] + \Pr[\text{Game}_B|\neg\text{Ev}] \Pr[\neg\text{Ev}] \\
 &= 0 \times \Pr[\text{Ev}] + \Pr[\text{Game}_A|\neg\text{Ev}] \times \Pr[\neg\text{Ev}] \\
 &= \Pr[\text{Game}_A] \times \Pr[\neg\text{Ev}]
 \end{aligned}$$
- Simulator B terminates and flips a coin, in case of event **Ev**:
- $$\begin{aligned}
 \Pr[\text{Game}_B] &= \Pr[\text{Game}_B|\text{Ev}] \Pr[\text{Ev}] + \Pr[\text{Game}_B|\neg\text{Ev}] \Pr[\neg\text{Ev}] \\
 &= \frac{1}{2} \times \Pr[\text{Ev}] + \Pr[\text{Game}_A|\neg\text{Ev}] \times \Pr[\neg\text{Ev}] \\
 &= \frac{1}{2} + (\Pr[\text{Game}_A] - \frac{1}{2}) \times \Pr[\neg\text{Ev}]
 \end{aligned}$$

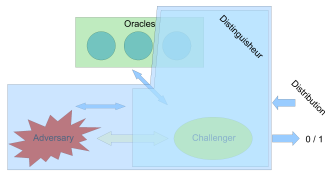
Two Simulations

- Identical behaviors: $\Pr[\text{Game}_A] - \Pr[\text{Game}_B] = 0$
- The behaviors differ only if **Ev** happens:
 - **Ev** is negligible, one can ignore it
 - **Ev** is non-negligible and independent of the output in Game_A , Simulator B terminates in case of event **Ev**

Event Ev

- Either **Ev** is negligible, or the output is independent of **Ev**
- For being able to terminate simulation B in case of event **Ev**, this event must be *efficiently detectable*
- For evaluating $\Pr[\text{Ev}]$, one re-iterates the above process, with an initial game that outputs 1 when event **Ev** happens

Two Distributions



$$\Pr[\text{Game}_A] - \Pr[\text{Game}_B] \leq \text{Adv}(\mathcal{D}^{\text{Oracles}})$$

Two Distributions

$$\Pr[\text{Game}_A] - \Pr[\text{Game}_B] \leq \text{Adv}(\mathcal{D}^{\text{oracles}})$$

- For identical/statistically close distributions, for any oracle:

$$\Pr[\text{Game}_A] - \Pr[\text{Game}_B] = \text{Dist}(\text{Distrib}_A, \text{Distrib}_B) = \text{negl}()$$

- For computationally close distributions, in general, we need to exclude additional oracle access:

$$\Pr[\text{Game}_A] - \Pr[\text{Game}_B] \leq \text{Adv}^{\text{Distrib}}(t)$$

where t is the computational time of the distinguisher

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Gap Groups

Definition (Pairing Setting)

- Let \mathbb{G}_1 and \mathbb{G}_2 be two cyclic groups of prime order p
- Let g_1 and g_2 be generators of \mathbb{G}_1 and \mathbb{G}_2 respectively
- Let $e : \mathbb{G}_1 \times \mathbb{G}_2 \rightarrow \mathbb{G}^T$, be a bilinear map

Definition (Admissible Bilinear Map)

Let $(p, \mathbb{G}_1, g_1, \mathbb{G}_2, g_2, \mathbb{G}^T, e)$ be a pairing setting, with $e : \mathbb{G}_1 \times \mathbb{G}_2 \rightarrow \mathbb{G}^T$ a non-degenerated bilinear map

- Bilinear: for any $g \in \mathbb{G}_1, h \in \mathbb{G}_2$ and $u, v \in \mathbb{Z}$,

$$e(g^u, h^v) = e(g, h)^{uv}$$

- Non-degenerated: $e(g_1, g_2) \neq 1$

Bilinear Maps

Bilinear Diffie-Hellman Problems

We focus on the symmetric case: $\mathbb{G}_1 = \mathbb{G}_2 = \mathbb{G}$

Diffie-Hellman Problems

- CDH** in \mathbb{G} : Given $g, g^a, g^b \in \mathbb{G}$, compute g^{ab}
- DDH** in \mathbb{G} : Given $g, g^a, g^b, g^c \in \mathbb{G}$, decide whether $c = ab$ or not

CDH can be hard to solve, but DDH is easy in gap-groups

Bilinear Diffie-Hellman Problems

- CBDH** in \mathbb{G} : Given $g, g^a, g^b, g^c \in \mathbb{G}$, compute $e(g, g)^{abc}$
- DBDH** in \mathbb{G} : Given $g, g^a, g^b, g^c \in \mathbb{G}$ and $h \in \mathbb{G}^T$, decide whether $h \stackrel{?}{=} e(g, g)^{abc}$

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Signature in Gap Groups

[Boneh-Lynn-Shacham - Asiacryp '01]

Let G be a cyclic group of prime order p , with a generator g
 Assumption: G **gap-group** (DDH easy, whereas CDH intractable)

Signature Scheme

- Key generation: choose $x \in \mathbb{Z}_p$, and set $y = g^x$;
- Signature of $M \in G$: $\sigma = M^x$;
- Verification of (M, σ) : check **DDH**(g, y, M, σ)

Full-Domain Hash

$$\mathcal{H} : \{0, 1\}^* \rightarrow G$$

- In order to sign m , one first computes $M = \mathcal{H}(m) \in G$
- then $\sigma = M^x = \text{CDH}(g, y, \mathcal{H}(m))$

EUF-CMA Security

EUF-CMA

Existential Unforgeability under Chosen-Message Attacks

An adversary, allowed to ask for signature on any message of its choice, cannot generate a new valid message-signature pair

Theorem

The BLS signature achieves EUF-CMA security, under the **CDH** assumption in G , in the Random Oracle Model:

$$\text{Adv}^{\text{euf-cma}}(t) \leq q_H \times \text{Adv}^{\text{cdh}}(t + q_H \tau_e)$$

Assumptions:

- any signing query has been first asked to \mathcal{H}
- the forgery has been asked to \mathcal{H}

Real Attack Game



Random Oracle

$$\mathcal{H}(m) : M \xleftarrow{R} G, \text{ output } M$$

Key Generation Oracle

$$\mathcal{K}(): sk \xleftarrow{R} \mathbb{Z}_p, pk = g^{sk}$$

Signing Oracle

$$\mathcal{S}(m) : M = \mathcal{H}(m), \text{ output } \sigma = M^{sk}$$

Simulations

- **Game₀**: use of the oracles \mathcal{K} , \mathcal{S} and \mathcal{H}
- **Game₁**: use of the *simulation of the Random Oracle*

Simulation of \mathcal{H}

$\mathcal{H}(m)$: $\mu \xleftarrow{R} \mathbb{Z}_p$, output $M = g^\mu$

⇒ **Hop-D-Perfect**: $\Pr[\text{Game}_1] = \Pr[\text{Game}_0]$

- **Game₂**: use of the *simulation of the Signing Oracle*

Simulation of \mathcal{S}

$\mathcal{S}(m)$: find μ such that $M = \mathcal{H}(m) = g^\mu$, output $\sigma = \text{pk}^\mu$

⇒ **Hop-S-Perfect**: $\Pr[\text{Game}_2] = \Pr[\text{Game}_1]$

CDH Instance

- **Game₄**: **CDH** instance $(g, A = g^a, B = g^b)$
Use of the *simulation of the Key Generation Oracle*

Simulation of \mathcal{K}

$\mathcal{K}()$: set $\text{pk} \leftarrow A$

Modification of the *simulation of the Random Oracle*

Simulation of \mathcal{H}

If this is the t -th query, $\mathcal{H}(m)$: $M \leftarrow B$, output M

The unique difference is for the t -th simulation of the random oracle, for which we cannot compute a signature.

But since it corresponds to the forgery output, it cannot be queried to the signing oracle:

⇒ **Hop-S-Perfect**: $\Pr[\text{Game}_4] = \Pr[\text{Game}_3]$

 \mathcal{H} -Query Selection

- **Game₃**: random index $t \xleftarrow{R} \{1, \dots, q_H\}$

Event **Ev**

If the t -th query to \mathcal{H} is not the output forgery

We terminate the game and output 1 if **Ev** happens

⇒ **Hop-S-Non-Negl**

Then, clearly

$$\Pr[\text{Game}_3] = \Pr[\text{Game}_2] \times \Pr[\neg \text{Ev}] \quad \Pr[\text{Ev}] = 1 - 1/q_H$$

$$\Pr[\text{Game}_3] = \Pr[\text{Game}_2] \times \frac{1}{q_H}$$

Conclusion

In **Game₄**, when the output is 1, $\sigma = \text{CDH}(g, A = g^a, B = g^b)$ and the simulator computes one exponentiation per hashing:

$$\Pr[\text{Game}_4] \leq \text{Adv}^{\text{cdh}}(t + q_H \tau_e)$$

$$\Pr[\text{Game}_4] = \Pr[\text{Game}_3]$$

$$\Pr[\text{Game}_3] = \Pr[\text{Game}_2] \times \frac{1}{q_H}$$

$$\Pr[\text{Game}_2] = \Pr[\text{Game}_1]$$

$$\Pr[\text{Game}_1] = \Pr[\text{Game}_0]$$

$$\Pr[\text{Game}_0] = \text{Adv}^{\text{euf-cma}}(A)$$

$$\text{Adv}^{\text{euf-cma}}(A) \leq q_H \times \text{Adv}^{\text{cdh}}(t + q_H \tau_e)$$

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Identity-Based Cryptography

[Shamir – Crypto '84]

Public-Key Cryptography

Each user ID owns

- a public key pk
- a certificate that guarantees the link between ID and pk
- a private key sk , related to pk

One has to access a dictionary in order to get pk , the public key of ID , together with the certificate, in order to encrypt a message to ID

Identity-Based Cryptography

Each user ID owns

- a private key sk , related to ID
- the public key pk is indeed ID itself

Identity-Based Encryption

Setup

The authority generates a master secret key msk , and publishes the public parameters, PK

Extraction

Given an identity ID , the authority computes the private key sk granted the master secret key msk

Encryption

Any one can encrypt a message m to a user ID using only m , ID and the public parameters PK

Decryption

Given a ciphertext, user ID can recover the plaintext, with sk

Definition (IND – ID – CCA Security)

- \mathcal{A} receives the global parameters
- \mathcal{A} asks any extraction-query, and any decryption-query
- \mathcal{A} outputs a target identity ID^* and two messages (m_0, m_1)

The challenger flips a bit b , and encrypts m_b for ID^* into c^*

- \mathcal{A} asks any extraction-query, and any decryption-query
- \mathcal{A} outputs its guess b' for b

Restriction: ID^* never asked to the extraction oracle, and (ID^*, c^*) never asked to the decryption oracle.

CPA: no decryption-oracle access

$$\text{Adv}^{\text{ind-id-cca}} = 2 \times \Pr[b' = b] - 1$$

BF IB-Encryption (Cont'd)

Setup

- The authority sets up a gap-group framework: a group \mathbb{G} of prime order p , with a generator g , equipped with an admissible bilinear map

$$e: \mathbb{G} \times \mathbb{G} \rightarrow \mathbb{G}^T$$
- It selects a master secret key $\text{msk} = s \in \mathbb{Z}_p$
- It publishes the public parameters: $\text{PK} = (p, \mathbb{G}, e, g, P = g^s)$

Extraction

Given an identity ID , the authority computes the private key $\text{sk} = \mathcal{H}(ID)^s$

Note that sk is a BLS signature of ID : $e(\text{sk}, g) = e(\mathcal{H}(ID), P)$

Encryption

- In order to encrypt a message m to a user ID
- one chooses a random $r \in \mathbb{Z}_p$
 - computes $A = g^r$ and $K = e(P, \mathcal{H}(ID)^r)$
 - sends $(A, B = K \times m)$
- $$K = e(P, \mathcal{H}(ID)^r) = e(g^s, \mathcal{H}(ID)^r)$$
- $$= e(g^r, \mathcal{H}(ID)^s) = e(A, \text{sk})$$

Decryption

- Upon reception of (A, B) , user ID
- computes $K = e(A, \text{sk})$
 - gets $m = B/K$

BF IB Security Analysis

Theorem

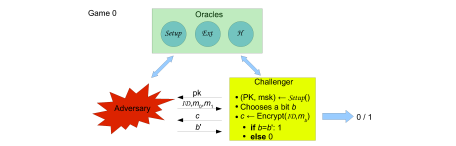
The BF IB-Encryption is IND-ID-CPA secure under the DBDH problem, in the random oracle model

By masking m with $H(K)$: $B = m \oplus H(K)$, the BF IB-Encryption is IND-ID-CPA secure under the CBDH problem, in the random oracle model

Theorem

The BLS signature achieves EUF-CMA security, under the CDH assumption in \mathbb{G} , in the Random Oracle Model

Real Attack Game



Random Oracle

$\mathcal{H}(ID): M \xrightarrow{R} \mathbb{G}$, output M

Setup Oracle

$\text{Setup}(): \text{msk} \xrightarrow{R} \mathbb{Z}_p, P = g^{\text{msk}}$

Extraction Oracle

$\text{Ext}(ID): M = \mathcal{H}(ID)$, output $\text{sk} = M^{\text{msk}}$

Simulations H-Query Selection

- **Game₀**: use of the oracles *Setup*, *Ext*, and \mathcal{H}
- **Game₁**: use of the *simulation of the Random Oracle*

Simulation of \mathcal{H}

$\mathcal{H}(ID): \mu \xleftarrow{R} \mathbb{Z}_p$, output $M = g^\mu$

- ⇒ **Hop-D-Perfect**: $\Pr[\text{Game}_1] = \Pr[\text{Game}_0]$
- **Game₂**: use of the *simulation of the Extraction Oracle*

Simulation of *Ext*

Ext(*ID*): find μ such that $M = \mathcal{H}(ID) = g^\mu$, output $\text{sk} = P^\mu$

⇒ **Hop-S-Perfect**: $\Pr[\text{Game}_2] = \Pr[\text{Game}_1]$

- **Game₃**: random index $t \xleftarrow{R} \{1, \dots, q_H\}$

Event *Ev*

If the t -th query to \mathcal{H} is not the challenge *ID*

We terminate the game and flip a coin if **Ev** happens
 ⇒ **Hop-S-Non-Negl**

$$\Pr[\text{Game}_3] = \frac{1}{2} + \left(\Pr[\text{Game}_2] - \frac{1}{2} \right) \times \Pr[\neg \text{Ev}] \quad \Pr[\text{Ev}] = 1 - 1/q_H$$

$$\Pr[\text{Game}_3] = \frac{1}{2} + \left(\Pr[\text{Game}_2] - \frac{1}{2} \right) \times \frac{1}{q_H}$$

Challenge *ID* Challenge Ciphertext

- **Game₄**: True **DBDH** instance $(g, g^\alpha, g^\beta, g^\gamma)$ with $h = e(g, g)^{\alpha\beta\gamma}$
 Use of the *simulation of the Setup Oracle*

Simulation of *Setup*

Setup(\cdot): set $P \leftarrow g^\alpha$

Modification of the *simulation of the Random Oracle*

Simulation of \mathcal{H}

If this is the t -th query, $\mathcal{H}(ID): M \leftarrow g^\beta$, output M

Difference for the t -th simulation of the random oracle: we cannot extract the secret key. Since this is the challenge *ID*, it cannot be queried to the extraction oracle:
 ⇒ **Hop-D-Perfect**: $\Pr[\text{Game}_4] = \Pr[\text{Game}_3]$

- **Game₅**: True **DBDH** instance $(g, g^\alpha, g^\beta, g^\gamma)$ with $h = e(g, g)^{\alpha\beta\gamma}$
 We have set $P \leftarrow g^\alpha$, and for the t -th query to \mathcal{H} : $M = g^\beta$

Ciphertext

Set $A \leftarrow g^\gamma$ and $K \leftarrow h$ to generate the encryption of m_b under *ID*

⇒ **Hop-D-Perfect**: $\Pr[\text{Game}_5] = \Pr[\text{Game}_4]$

- **Game₆**: Random **DBDH** instance $(g, g^\alpha, g^\beta, g^\gamma)$ with $h \xleftarrow{R} \mathbb{G}_T$
 ⇒ **Hop-D-Comp**:

$$|\Pr[\text{Game}_6] - \Pr[\text{Game}_5]| \leq \text{Adv}^{\text{dbdh}}(t + q_{HT_e})$$

Conclusion

In this last **Game₆**, it is clear that $\Pr[\mathbf{Game}_6] = \frac{1}{2}$

$$|\Pr[\mathbf{Game}_6] - \Pr[\mathbf{Game}_5]| \leq \text{Adv}^{\text{dbdh}}(t + q_H \tau_e)$$

$$\Pr[\mathbf{Game}_5] = \Pr[\mathbf{Game}_4]$$

$$\Pr[\mathbf{Game}_4] = \Pr[\mathbf{Game}_3]$$

$$\Pr[\mathbf{Game}_3] = \frac{1}{2} + (\Pr[\mathbf{Game}_2] - \frac{1}{2}) \times \frac{1}{q_H}$$

$$\Pr[\mathbf{Game}_2] = \Pr[\mathbf{Game}_1]$$

$$\Pr[\mathbf{Game}_1] = \Pr[\mathbf{Game}_0]$$

$$\Pr[\mathbf{Game}_0] = \frac{1}{2} + \text{Adv}^{\text{ind-id-cpa}}(\mathcal{A})$$

$$\text{Adv}^{\text{ind-id-cpa}}(\mathcal{A}) \leq q_H \times \text{Adv}^{\text{dbdh}}(t + q_H \tau_e)$$

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Conclusion

- The game-based methodology uses a sequence of games
- The transition hops
 - are simple
 - easy to check

It leads to easy-to-read and easy-to-verify security proofs:

- Some mistakes have been found granted this methodology [Analysis of OAEP]
- Some security analyses became possible to handle [Analysis of EKE]

This approach can be automatized [CryptoVerif]