On Various Abstract Understandings of Abstract Interpretation Patrick Cousot

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September 12-14, 2015 - Nanjing, China

Formal methods

Reasonings on programs are

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•Reasonings on properties of their semantics (i.e. execution behaviors)

•Always involve some form of abstraction

Abstract interpretation

2

Motivation

A theory establishing a correspondance between

•Concrete semantic properties

 \uparrow what you want to prove on the semantics

Abstract properties

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 \uparrow how to prove it in the abstract

Objective: formalize

- formal methods
- algorithms for reasoning on programs

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Fundamental motivations

Scientific research

in Mathematics/Physics:

trend towards unification and synthesis through universal principles

in Computer science:

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trend towards dispersion and parcelization through a collection of local techniques for specific applications

An exponential process, will stop!

Example: reasoning on computational structures

5

WCET Operational Security protocole Systems biology semantics Axiomatic verification analysis semantics Abstraction Model Dataflow Database refinement Confidentiality analysis checking query analysis Туре Partial Obfuscation Dependence inference Program evaluation analysis synthesis Separation Denotational Effect CEGAR logic Grammar semantics systems Termination analysis Program Theories Trace proof Statistical combination transformation semantics Code Interpolants Abstract model-checking Shape analysis Invariance model Symbolic contracts Integrity proof checking Malware execution analysis Probabilistic detection Quantum entanglement Bisimulation Code verification detection SMT solvers Parsing Type theory Steganography Tautology testers refactoring

Example: reasoning on computational structures

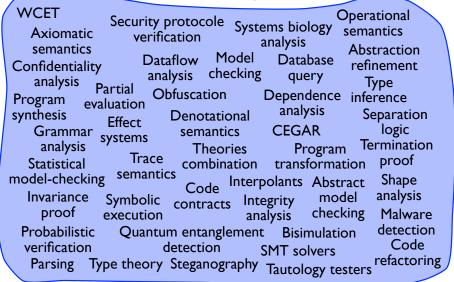
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WCET Operational Security protocole Systems biology semantics Axiomatic verification analysis semantics Abstraction Model Dataflow Database refinement Confidentiality analysis checking query analysis Туре Partial Obfuscation Dependence inference Program evaluation analysis synthesis Separation Denotational Effect CEGAR logic Grammar semantics systems Termination analysis Program Theories Trace proof Statistical combination transformation semantics model-checking Shape Interpolants Abstract Code analysis Invariance model Symbolic contracts Integrity proof checking Malware execution analysis detection Probabilistic Quantum entanglement Bisimulation Code verification detection SMT solvers Parsing Type theory Steganography Tautology testers refactoring

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Example: reasoning on computational structures

Abstract interpretation



Practical motivations

All computer scientists have experienced bugs

9



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(unit error)

Ariane 5.01 failure (overflow)

Patriot failure Mars orbiter loss (float rounding)

Heartbleed (buffer overrun)

Checking the presence of bugs by debugging is great Proving their absence by static analysis is even better!

Undecidability and complexity is the challenge for automation

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10

Boeing 787 Dreamliners contain a potentially catastrophic software bug

Beware of integer overflow-like bug in aircraft's electrical system, FAA warns

by Dan Goodin - May 1, 2015 7:55pm CEST

A software vulnerability in Boeing's new 787 Dreamliner jet has the potential to cause pilots to lose control of the aircraft, possibly in mid-flight, Federal Aviation Administration officials warned airlines recently.

The bug—which is either a classic integer overflow or one very much resembling it—resides in one or the electrical systems responsible for generating power, according to memo the FAA issued last week The vulnerability, which Boeing reported to the FAA, is triggered when a generator has been running continuously for a little more than eight months. As a result, EAA officials have adopted a new airworthiness directive (AD) that airlines will be required to follow, at least until the underlying flaw is fixed

"This AD was prompted by the determination that a Model 787 airplane that has been powered continuously for 248 days can lose all alternating current (AC) electrical power due to the generator control units (GCUs) simultaneously going into failsafe mode," the memo stated. "This condition is caused by a software counter internal to the GCUs that will overflow after 248 days of continuous power. We are issuing this AD to prevent loss of all AC electrical power, which could result in loss of

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TASE 2015, September 12-14 control of the airplane."

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Informal examples of abstraction

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/www.petapixel.com/2011/06/23/how-much-pixelation-is-needed-before-a-photo-becomes-transformed/ Image credit: Photograph by Jay Maisel

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Abstractions of Dora Maar by Picasso



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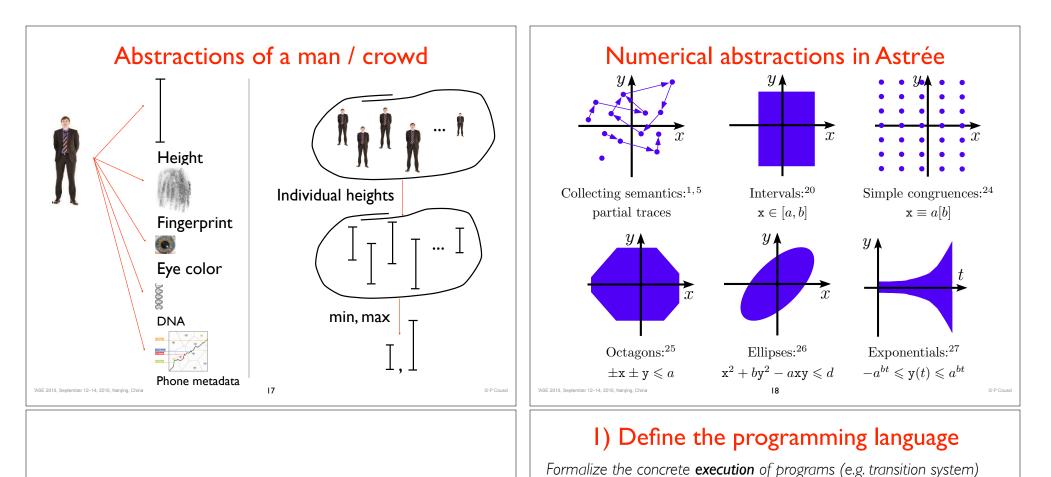
An old idea...

14

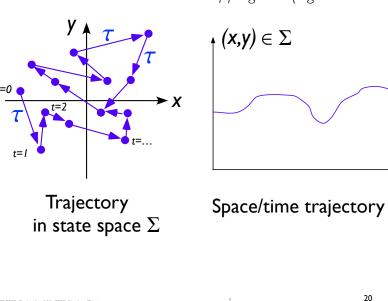
20 000 years old picture in a spanish cave:



(the concrete is unknown)



An informal introduction to abstract interpretation



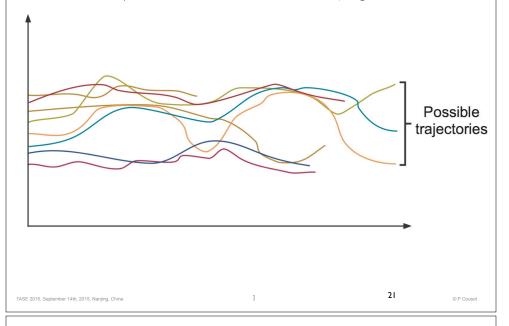
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P. Cousot & R. Cousot A genite introduction to formal verification of computer systems by abstract interpretation. In Logics and Languages for Reliability and Security, J. Esparza, O. Grumberg, & M. Broy (Eds), NATO Science Series III: Computer and Systems Sciences, © IOS Press, 2010, Pages 1–29.

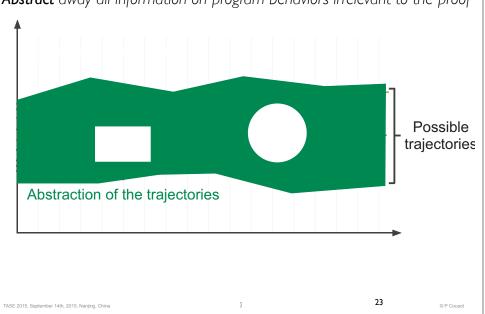
t

II) Define the program properties of interest

Formalize what you are interested to **know** about program behaviors



IV) Choose the appropriate abstraction



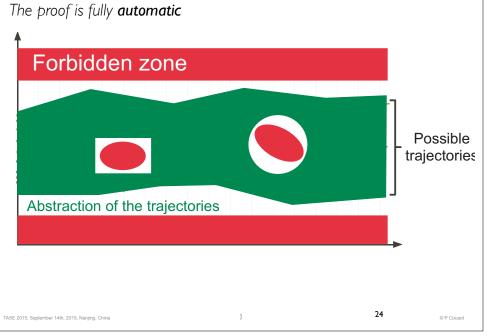
Abstract away all information on program behaviors irrelevant to the proof

III) Define which specification must be checked

Formalize what you are interested to **prove** about program behaviors

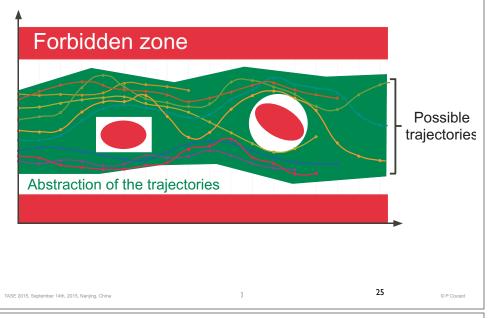


V) Mechanically verify in the abstract



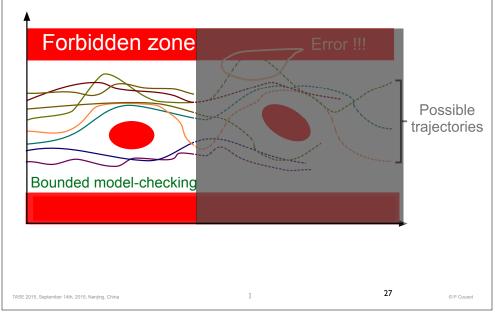
Soundness of the abstract verification

Never forget any possible case so the *abstract proof is correct in the concrete*



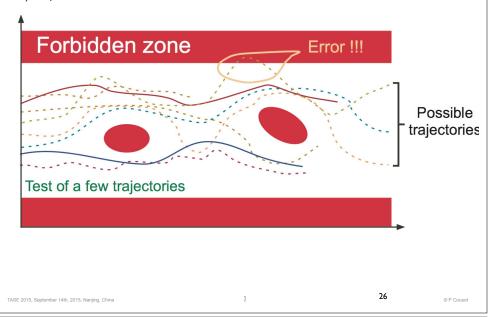
Unsound validation: bounded model-checking

Simulate the beginning of all executions



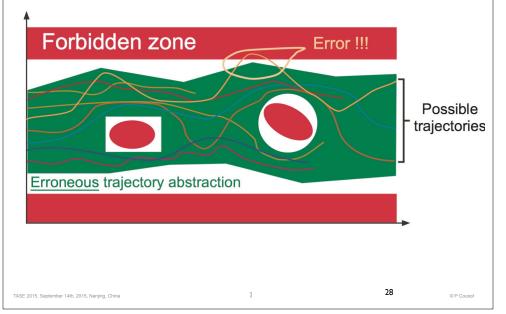
Unsound validation: testing

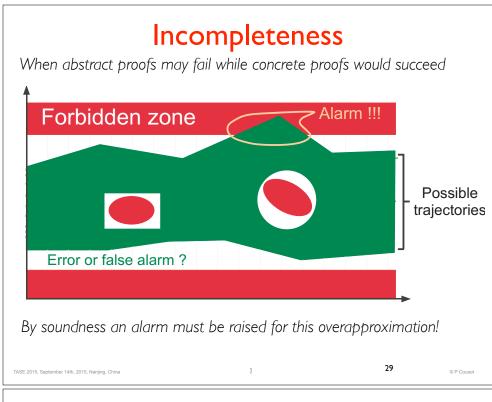
Try a few cases



Unsound validation: static analysis

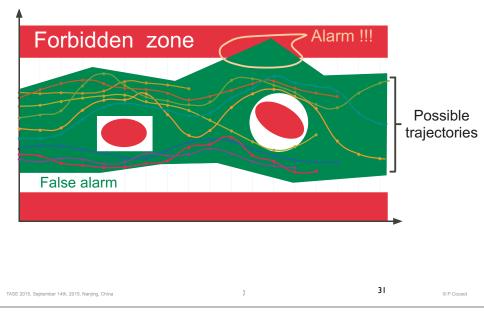
Many static analysis tools are **unsound** (e.g. Coverity, etc.) so inconclusive

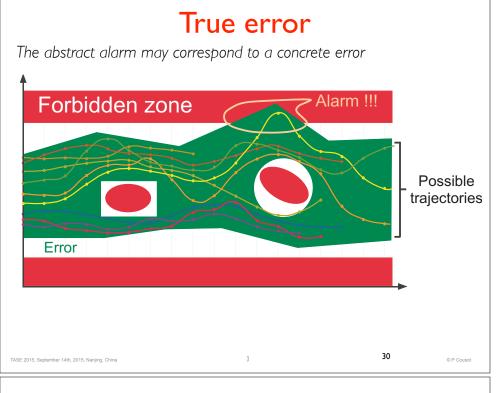




False alarm

The abstract alarm may correspond to no concrete error (false negative)





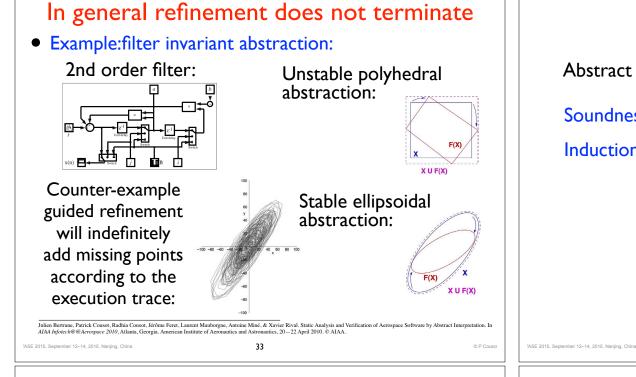
What to do about false alarms?

- Consider special cases: finite (small) models (modelchecking), decidable cases (SMT solvers), human interaction (theorem provers, proof verifiers), ...
- Automatic refinement: inefficient and may not terminate (Gödel, see next slide)
- Domain-specific abstraction:

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- Adapt the abstraction to the programming paradigms typically used in given *domain-specific applications*
- e.g. synchronous control/command: no recursion, simple memory allocation, maximum execution time, etc.

32



Abstract Interpretation

34

Properties and their

Abstractions

Abstract interpretation is all about:

Soundness

Induction

A very short more formal introduction to abstract interpretation

Patrick Cousot & Radhia Cousot. Vérification statique de la cohérence dynamique des programmes. In Rapport du contrat IRIA SESORI No 75-035, Laboratoire IMAG, University of Grenoble France. 125 pages. 23 September 1975.

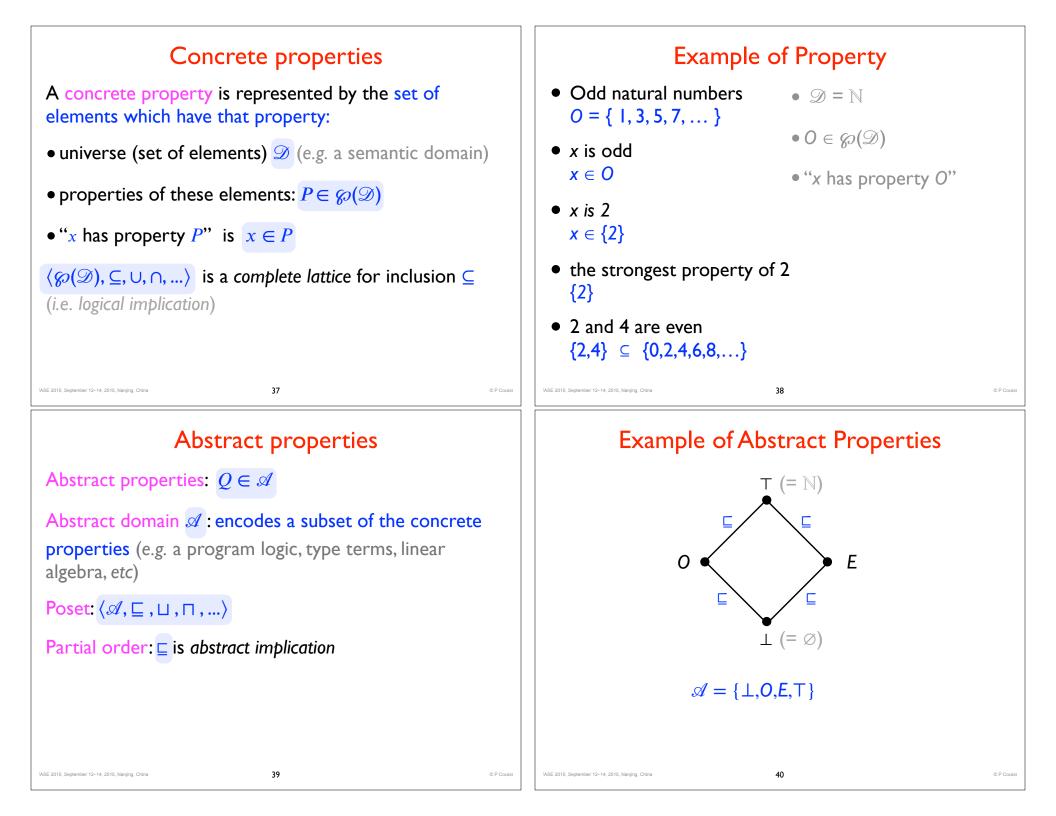
Patrick Cousot & Radhia Cousot. Static Determination of Dynamic Properties of Programs. In B. Robinet, editor, Proceedings of the second international symposium on Programming, Paris, France, pages 106-130, April 13-15 1976, Dunod, Paris

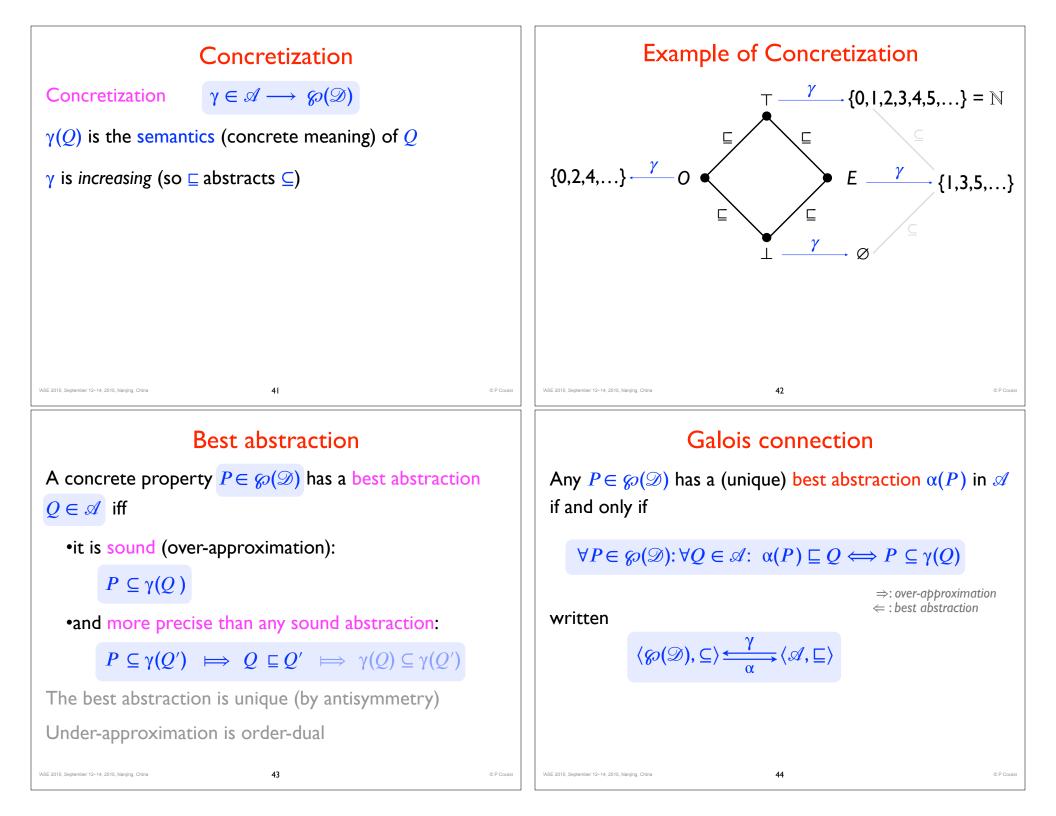
Patrick Cousot, Radhia Cousot: Abstract Interpretation: A Unified Lattice Model for Static Analysis of Programs by Construction or Approximation of Fixpoints. POPL 1977: 238-252 Patrick Cousot, Radhia Cousot: Systematic Design of Program Analysis Frameworks. POPL 1979: 269-282

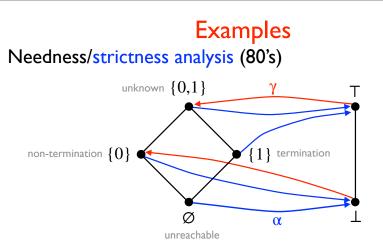
Patrick Cousot. Méthodes itératives de construction et d'approximation de points fixes d'opérateurs monotones sur un treillis, analyse sémantique des programmes. Thèse És Sciences Mathématiques, Université Joseph Fourier, Grenoble, France, 21 March 1978

Patrick Cousot. Semantic foundations of program analysis. In S.S. Muchnick & N.D. Jones, editors, Program Flow Analysis: Theory and Applications, Ch. 10, pages 303-342, Prentice Hall, Inc., Englewood Cliffs, New Jersey, U.S.A., 1981. IASE 2015. September 12-14, 2015. Naniing, China 35

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Similar abstraction $(\gamma(T) \triangleq \{\text{true, false}\})$ for scalable hardware symbolic trajectory evaluation STE (90)

Alan Mycroft: The Theory and Practice of Transforming Call-by-need into Call-by-value. Symposium on Programming 1980: 269-281

Carl-Johan H. Seger, Randal E. Bryant: Formal Verification by Symbolic Evaluation of Partially-Ordered Trajectories. Formal Methods in System Design 6(2): 147-189 (1995)

In absence of best abstraction?

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Best abstraction of a disk by a rectangular parallelogram (intervals)



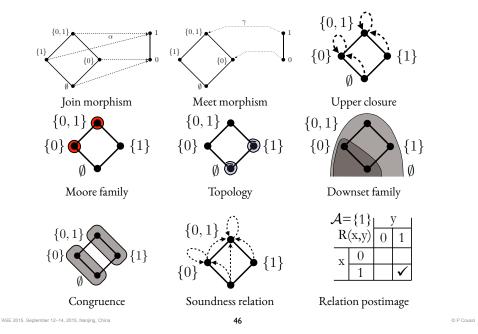
No best abstraction of a disk by a polyhedron (Euclid)



use only abstraction or concretization or widening (*)

(*) Patrick Cousot, Radhia Cousot: Abstract Interpretation Frameworks. J. Log. Comput. 2(4): 511-547 (1992)
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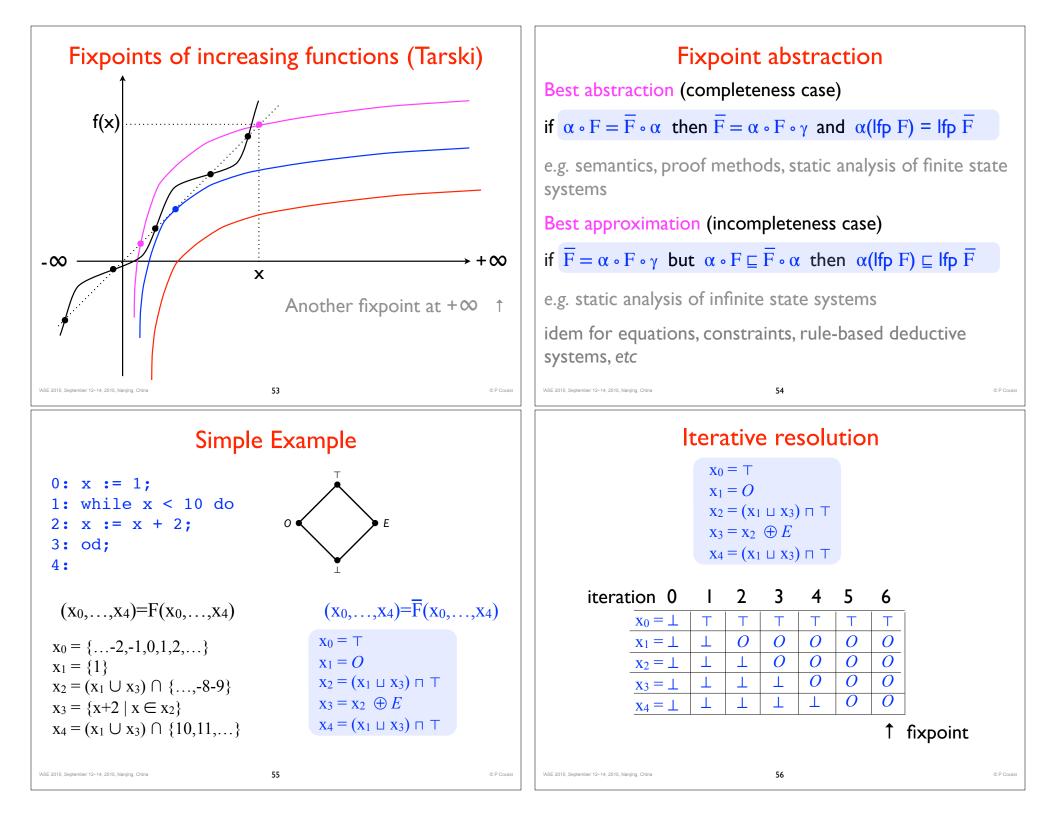
Equivalent mathematical structures

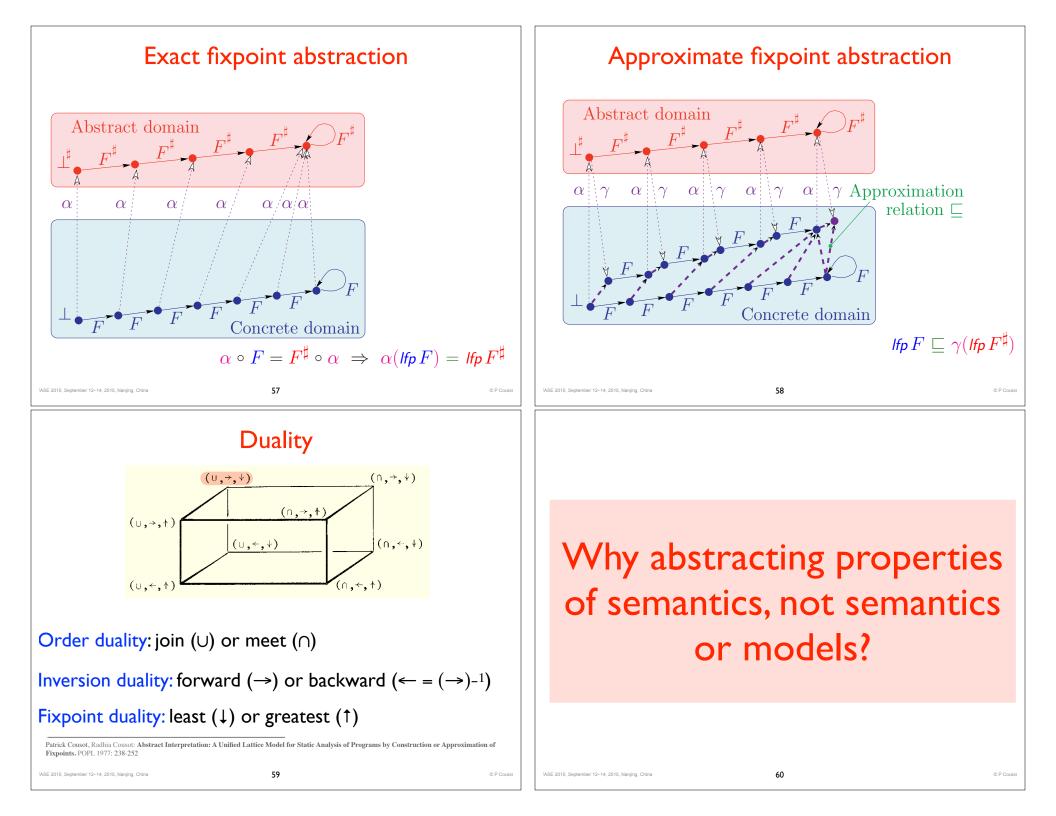


Sound semantics abstraction

program	P ∈ L pro	ogramming language
standard semantics	$S[\![\mathtt{P}]\!]\in\mathscr{D}$	semantic domain
collecting semantics	$\{S[\![P]\!]\}\in \wp(\mathscr{D})$	semantic property
abstract semantics	$\bar{S}[\![P]\!] \in \mathscr{A}$	abstract domain
concretization	$\gamma \in \mathscr{A} \longrightarrow \mathscr{D}(\mathcal{A})$	Ø)
soundness	$S[P] \subseteq \gamma(\overline{S}[P])$	·]])
<i>i.e.</i> $S[P] \in \gamma(\overline{S}[P])$, P has abstro	ict property S [[P]]
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Calculational design of the abstract semantics **Best abstract semantics** If $\langle \mathscr{D}(\mathscr{D}), \subseteq \rangle \xrightarrow{\gamma} \langle \mathscr{A}, \sqsubseteq \rangle$ then the best abstract The (standard hence collecting) semantics are defined by semantics is the abstraction of the collecting semantics composition of mathematical structures (such as set unions, products, functions, fixpoints, etc) $S[\overline{P}] \triangleq \alpha(\{S[P]\})$ If you know best abstractions of properties, you also know best abstractions of these mathematical structures Proof: •It is sound: $S[P] \triangleq \alpha(\{S[P]\}) \sqsubseteq S[P] \Longrightarrow \{S[P]\} \subseteq$ So, by composition, you also know the best abstraction of $\gamma(\mathsf{S}[\![\mathsf{P}]\!]) \longrightarrow \mathsf{S}[\![\mathsf{P}]\!] \in \gamma(\mathsf{S}[\![\mathsf{P}]\!])$ abstract semantics •It is the most precise: $S[P] \in \gamma(S[P]) \Longrightarrow \{S[P]\} \subseteq \gamma(S[P])$ Orthogonally, there are many styles of $\implies \mathsf{S}[\![\overline{\mathsf{P}}\!]\!] \triangleq \alpha(\{\mathsf{S}[\![\overline{\mathsf{P}}]\!]\}) \sqsubseteq \mathsf{S}[\![\mathsf{P}]\!]$ • semantics (traces, relations, transformers,...) • *induction* (transitional, structural, segmentation [POPL 2012]) • presentations (fixpoints, equations, constraints, rules [CAV 1995]) ASE 2015, September 12–14, 2015, Nanjing, China 50 49 E 2015, September 12-14, 2015, Naniing, Chin Example: functional connector Simple example If $g = \langle \mathscr{C}, \subseteq \rangle \stackrel{\gamma}{\longleftrightarrow} \langle \mathscr{A}, \sqsubseteq \rangle$ then $F(x_2) = \{x+2 \mid x \in x_2\}$ $\alpha \circ F \circ \gamma(\perp)$ $= \alpha(\{x+2 \mid x \in \emptyset\})$ $g \longmapsto g = \langle \mathscr{C} \xrightarrow{\checkmark} \mathscr{C}, \subseteq \rangle \xrightarrow{\lambda \overline{F}. \gamma \circ \overline{F} \circ \alpha} \langle \mathscr{A} \xrightarrow{\checkmark} \mathscr{A}, \sqsubseteq \rangle$ $= \alpha(\emptyset)$ = | $\alpha \circ \mathbf{F} \circ \gamma(O)$ $F(x_2)$ 0 Eα $= \alpha(\{x+2 \mid x \in \gamma(O)\}\)$ g $= \alpha(\{x+2 \mid x \in \{1,3,5,...\}\})$ F E0 $= \alpha(\{3,5,7,\ldots\})$ 0 E= O $(\mapsto$ is a called a *Galois connector*) Т 52 51 © P Couso © P Couso





Understandings of Abstract Interpretation

- *I*. Abstract interpretation = a non-standard semantics (computations on values in the standard semantics are replaced by computations on abstract values) \implies extremely limited
- 2. Abstract interpretation = an abstraction of the standard semantics \implies limited
- 3. Abstract interpretation = an abstraction of <u>properties</u> of the standard semantics \implies more

i.e. (1) is an abstraction of (2), (2) is an abstraction of (3)

How to abstract the standard semantics?

61

The join abstraction:

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 $\langle \wp(\wp(\Pi)), \subseteq \rangle \xrightarrow{\gamma_{\cup}} \langle \wp(\Pi), \subseteq \rangle$ $\alpha_{\cup}(X) \triangleq \bigcup X$ $\gamma_{\cup}(Y) \triangleq \wp(Y)$

Join abstraction of the collecting semantics:

 $\alpha_{\cup}(C[[\mathbf{P}]]) \triangleq \bigcup \{S[[\mathbf{P}]]\} \triangleq S[[\mathbf{P}]]$

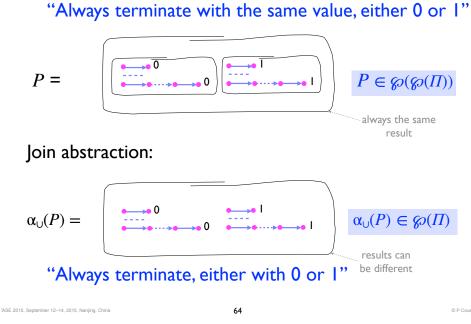
(i.e. the semantics is the join abstraction of its strongest property)

Example: trace semantics properties

Domain of [in]finite traces on states: Π "Standard" trace semantics domain: $\mathcal{D} = \mathcal{D}(\Pi)$ "Standard" trace semantics $S[P] \in \mathcal{D} = \wp(\Pi)$ Domain of semantics properties is $\wp(\mathcal{D}) = \wp(\wp(\Pi))$ Collecting semantics $C[P] \triangleq \{S[P]\} \in \wp(\mathcal{D}) = \wp(\wp(\Pi))$

Loss of information

62



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Limitations of the union abstraction

Complete iff any property of the semantics S[P] is also valid for any subset $\gamma(S[P]) = \wp(S[P])$:

- Examples: safety, liveness
- Counter-example: security (e.g. authentication using a random cryptographic nonce)



Exact abstractions

65

The concrete properties of the standard semantics S[P] that you want to prove can always be proved in the abstract (which is simpler):

 $\forall Q \in \mathscr{A} \colon S[\![\mathsf{P}]\!] \in \gamma(Q) \iff S[\![\overline{\mathsf{P}}]\!] \sqsubseteq Q$

where

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 $S[[\overline{\mathbf{P}}]] \triangleq \alpha \circ S[[\mathbf{P}]] \circ \gamma$

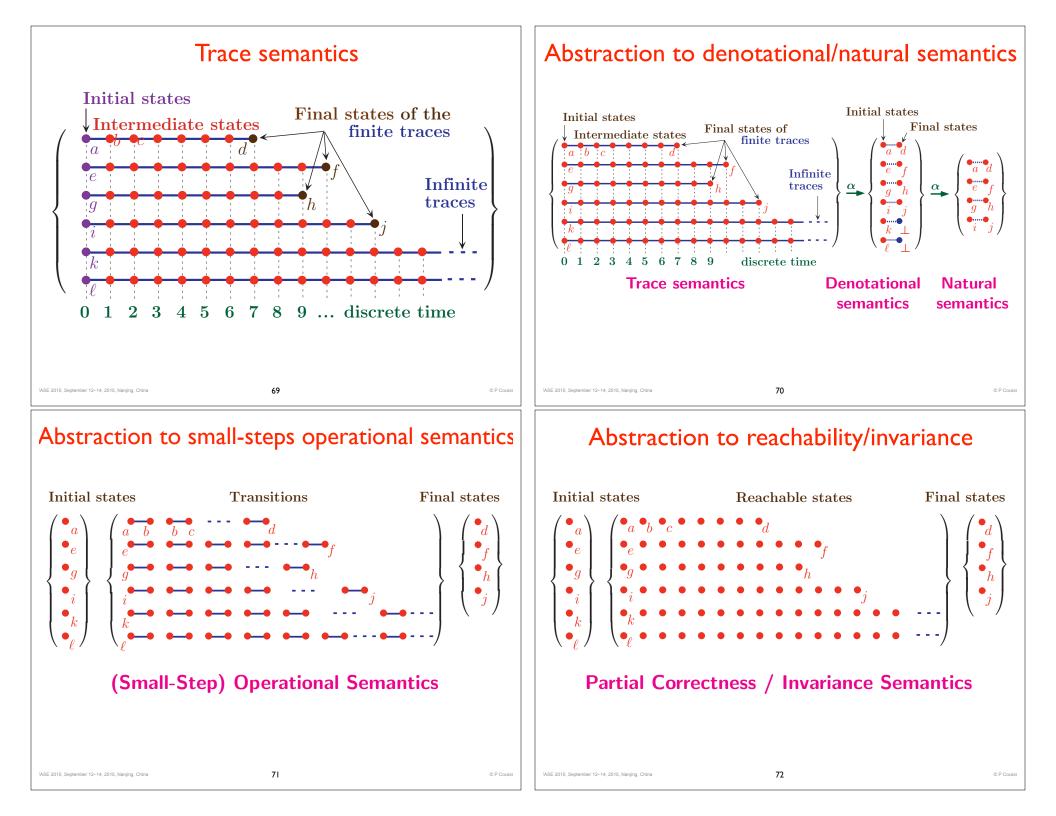
Example III of exact abstractions: semantics

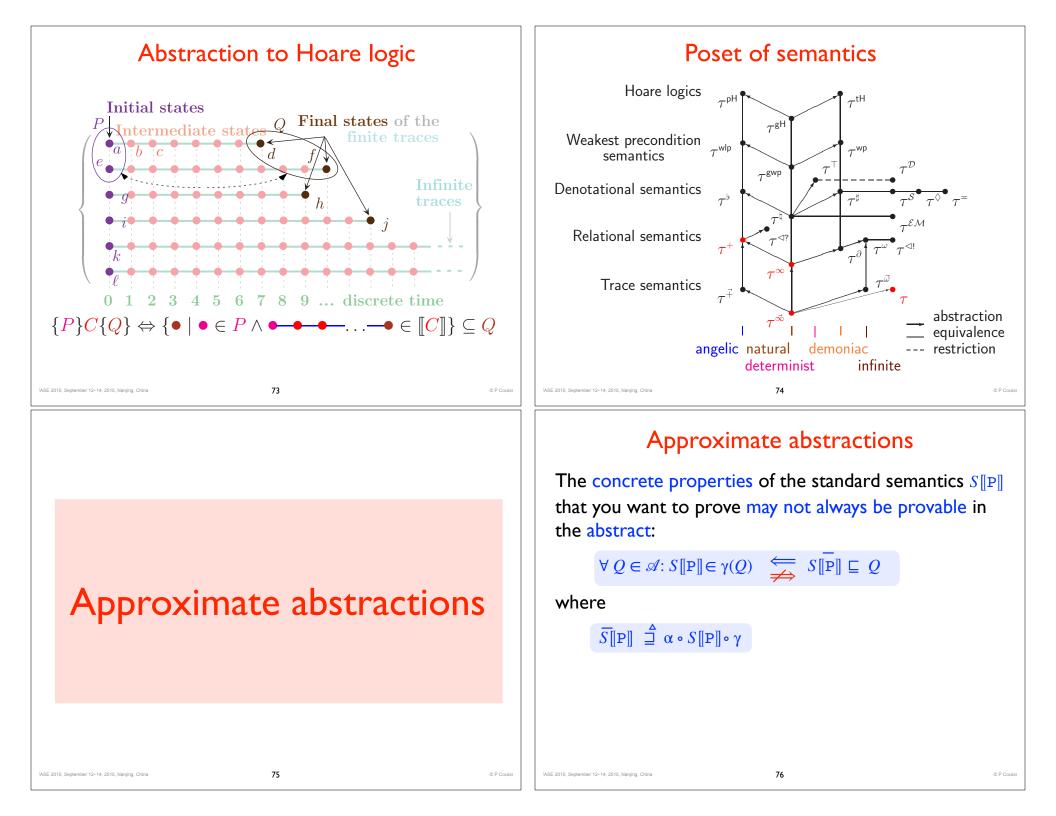
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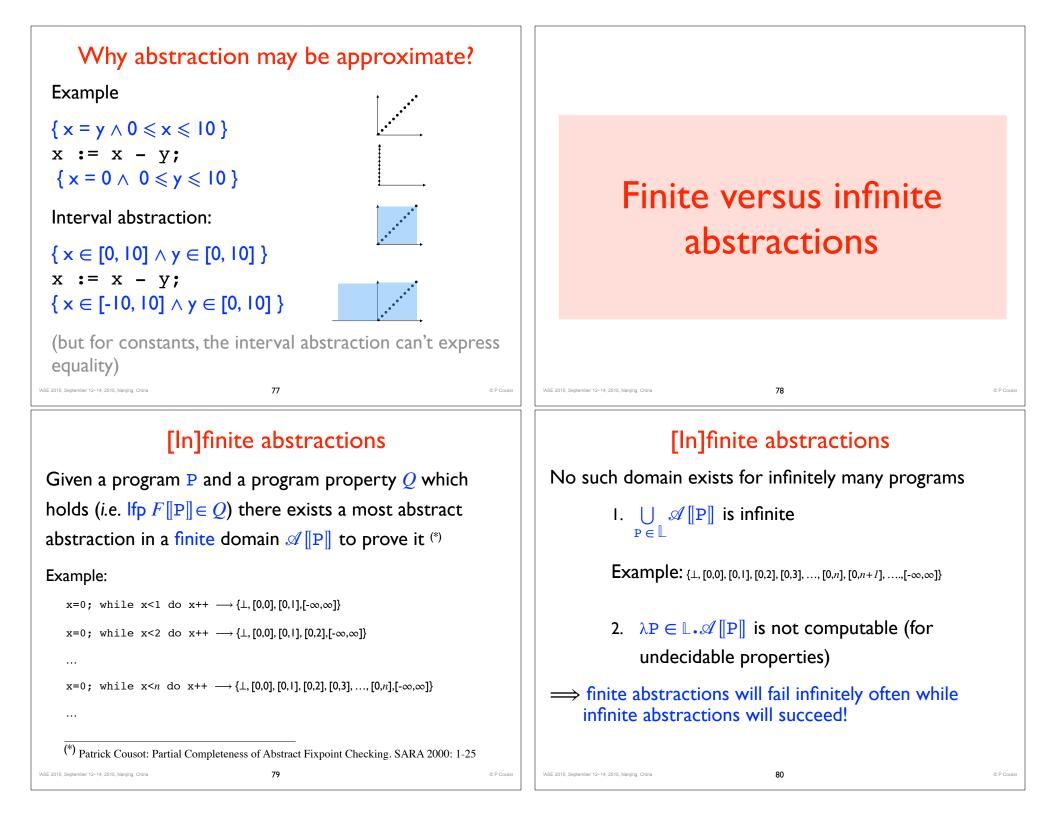
Patrick Cousot: Constructive design of a hierarchy of semantics of a transition system by abstract interpretation. Theor. Comput. Sci. 277(1-2): 47-103 (2002)

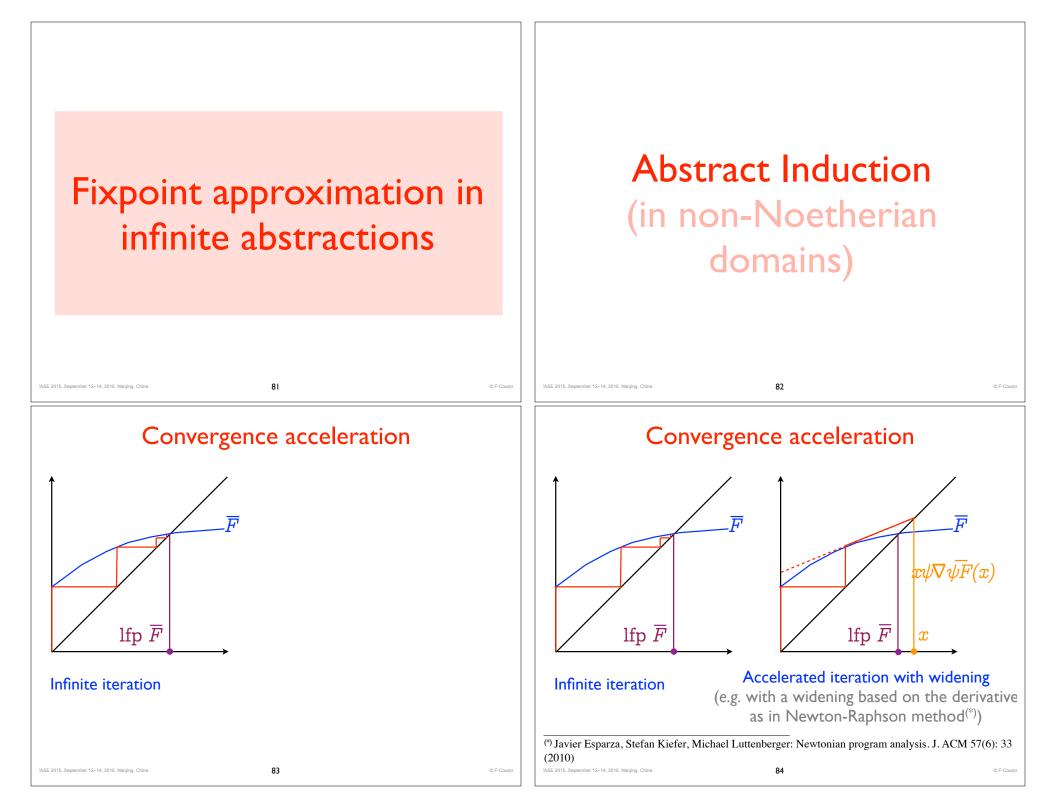
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Problem with infinite abstractions

For non-Noetherian iterations, we need

- finitary abstract induction, and
- finitary passage to the limit

X ⁰ =⊥,, >	$x^{n+1} = \mathfrak{T}(X)$	$^{0},, \mathbf{X}^{n}, F(X^{0}),,$	$F(X^n)), \dots, lim_{n \to \infty} X^n$	
		iteration converging		
	J	above the limit	below the limit	
lteration starting from	below the limit	widening \bigtriangledown	dual narrowing $\widetilde{\bigtriangleup}$	
	above the limit	narrowing $ riangle$	dual widening $\widetilde{\bigtriangledown}$	
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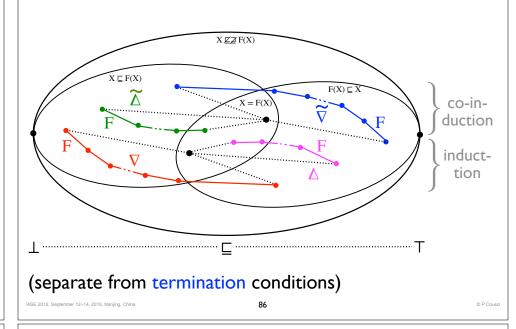
Examples of widening/narrowing

Abstract induction for intervals:

•a widening ^[1,2]

$\begin{array}{l} (x \ \bar{\bar{v}} \ y) = \underbrace{\operatorname{cas} \ x \ \bar{v} \ a, \ y \ e \ v_a}_{a}, \ y \ e \ v_a \ \underline{dans}}_{a \ \overline{v_a}, \ y \ e \ v_a} \\ + \ \frac{1}{2} \left[\begin{array}{c} 0, \ 2 = > \ y \ ; \\ + \ 2, \ \Box = > \ x \ ; \\ - \ [n_1, m_1], [n_2, m_2] = > \\ & \left[\begin{array}{c} \underline{(si} \ n_2 < n_1 \ \underline{alors} \ -\infty \ \underline{sinon} \ n_1 \ \underline{fsi} \ ; \\ \underline{sincas} \ \underline{sinon} \ m_1 \ \underline{fsi} \ ; \end{array} \right]; \end{array}$	$[a_1, b_1] \overline{\nabla} [a_2, b_2] =$ $[\underline{if} a_2 < a_1 \underline{then} -\infty \underline{else} a_1 \underline{fi},$ $\underline{if} b_2 > b_1 \underline{then} +\infty \underline{else} b_1 \underline{fi}]$			
•a narrowing ^[2]				
[a ₁ ,b ₁] Ā [a ₂ ,b ₂] =				
[if a ₁ = -∞ then a ₂ else MIN (a ₁ ,a ₂),				
$\frac{\text{if } b_1^{= +\infty} \text{ then } b_2 \text{ else MAX } (b_1, b_2)]}{(b_1, b_2)}$				
 Patrick Cousot, Radhia Cousot: Vérification statique de la cohérence dynamique des programmes, Rapport du contrat IRIA-SESORI No 75-032, 23 septembre 1975. Patrick Cousot, Radhia Cousot: Abstract Interpretation: A Unified Lattice Model for Static Analysis of Programs by Construction or Approximation of Fixpoints. POPL 1977: 238-252 				
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[Semi-]dual abstract induction methods



On widening/narrowing/and their duals

Because the abstract domain is non-Noetherian, *any* widening/narrowing/duals can be *strictly* improved infinitely many times (*i.e.* no best widening)

E.g. widening with thresholds [1]

```
 \begin{array}{l} \forall x \in \bar{L}_{2}, \perp \nabla_{2}(j) \ x = x \nabla_{2}(j) \ \perp = x \\ [l_{1}, u_{1}] \nabla_{2}(j) \ [l_{2}, u_{2}] \\ &= [if \ 0 \le l_{2} < l_{1} \ then \ 0 \ elsif \ l_{2} < l_{1} \ then \ -b \ -1 \ else \ l_{1} \ fi, \\ & if \ u_{1} < u_{2} \le 0 \ then \ 0 \ elsif \ u_{1} < u_{2} \ then \ b \ else \ u_{1} \ fi] \end{array} 
Any terminating widening is <u>not</u> increasing (in its first parameter)
```

Any abstraction done with Galois connections can be done with widenings (i.e. a widening calculus)

[1] Patrick Cousot, Semantic foundations of program analysis, Ch. 10 of Program flow analysis: theory and practice, N. Jones & S. Muchnich (eds), Prentice Hall, 1981. IASE 2015, September 12–14, 2015, Manjing, China © P

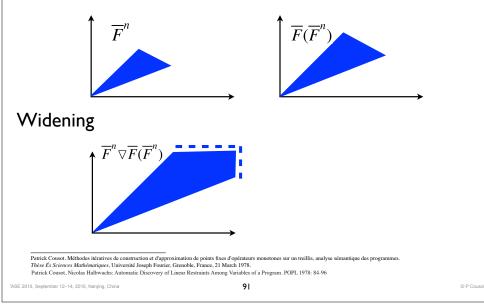
Infinitary static analysis with abstract induction

Example: (simple) widening for polyhedra

89

Iterates

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Widening

 $\langle \mathscr{A}, \sqsubseteq \rangle$ poset

 $\nabla \in \mathscr{A} \times \mathscr{A} \longrightarrow \mathscr{A}$

Sound widening (upper bound):

 $\forall x, y \in \mathscr{A}: x \sqsubseteq x \bigtriangledown y \land y \sqsubseteq x \bigtriangledown y$ Terminating widening: for any $\langle x^n \in \mathscr{A}, n \in \mathbb{N} \rangle$, the sequence $y^0 \triangleq x^0, \dots, y^{n+1} \triangleq y^n \bigtriangledown x^n, \dots$ is ultimately stationary $(\exists \varepsilon \in \mathbb{N}: \forall n \ge \varepsilon: y^n = y^\varepsilon)$

(Note: sound and terminating are independent properties)

Patrick Cousot, Radhia Cousot: Abstract Interpretation: A Unified Lattice Model for Static Analysis of Programs by Construction or Approximation of Fixpoints. POPL 1977: 238-252

Iteration with widening for static analysis

Problem: compute *I* such that $Ifp \subseteq F \subseteq I \subseteq Q$

Compute I as the limit of the iterates:

X⁰ ≜ ⊥,

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- $X^{n+1} \triangleq X^n$ when $F(X^n) \sqsubseteq X^n$ so $I = X^n$
- $X^{n+1} \triangleq (X^n \bigtriangledown F(X^n)) \bigtriangleup Q$

otherwise



Check that $F(I) \sqsubseteq Q$

Example: Astrée

Patrick Cousot, Radhia Cousot: Abstract Interpretation: A Unified Lattice Model for Static Analysis of Programs by Construction or Approximation of Fixpoints. POPL 1977: 238-252

Dual narrowing

 $\langle \mathscr{A}, \sqsubseteq \rangle$ poset

 $\widetilde{\wedge} \in \mathscr{A} \times \mathscr{A} \longrightarrow \mathscr{A}$

Sound dual narrowing (interpolation):

 $\forall x, y \in \mathscr{A} \colon x \sqsubseteq y \implies x \sqsubseteq x \widetilde{\bigtriangleup} y \sqsubseteq y$ Terminating dual narrowing: for any $\langle x^n \in \mathcal{A}, n \in \mathbb{N} \rangle$, the sequence $y^0 \triangleq x^0, ..., y^{n+1} \triangleq y^n \bigwedge x^n, ...$ is ultimately stationary ($\exists \varepsilon \in \mathbb{N}: \forall n \geq \varepsilon: y^n = y^\varepsilon$)

(Note: sound and terminating are independent properties)

Cousot, P. Méthodes itératives de construction et d'approximation de points fixes d'opérateurs monotones sur un treillis, analyse sémantique de programmes (in French). Thèse d'État ès sciences mathématiques, Université scientifique et médicale de Grenoble, France 1978.

Iteration with dual narrowing for static checking

Problem: find I such that $|\mathsf{Ip} \vdash F \vdash I \vdash Q$

Compute *I* as the limit of the iterates:

•
$$X^0 \triangleq \bot$$
,
• $X^{n+1} \triangleq X^n$ when $F(X^n) \sqsubseteq X^n$ so $I = X^n$
• $X^{n+1} \triangleq F(X^n) \overleftrightarrow{\Omega} Q$, otherwise

Check that $F(I) \sqsubseteq Q$

Example: First-order logic + Graig interpolation (with

some choice of one of the solutions, control of

combinatorial explosion, and convergence enforcement)

Kenneth L. McMillan: Applications of Craig Interpolants in Model Checking. TACAS 2005: 1-12 ASE 2015, September 12-14, 2015, Nanjing, China

Industrialization

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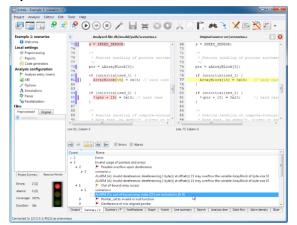
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Stephan Thesing, Jean Souvris, Reinhold Heckmann, Famantanantsoa Randimbivololona, Marc Langenbach, Reinhard Wilhelm, Christian Ferdinand: An Abstract Interpretation-Based Timins Validation of Hard Real-Time Avionics Software. DSN 2003: 625-632

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Effectively used in production to qualify truly large and complex software in transportation, communications, medicine, etc

Bruno Blanchet, Patrick Cousot, Radhia Cousot, Jérôme Feret, Laurent Mauborgne, Antoine Miné, David Monniaux, Xavier Rival: A static analyzer for large safety-critical software. PLDI 2003: 196-207 96

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Example of domain-specific abstraction: ellipses

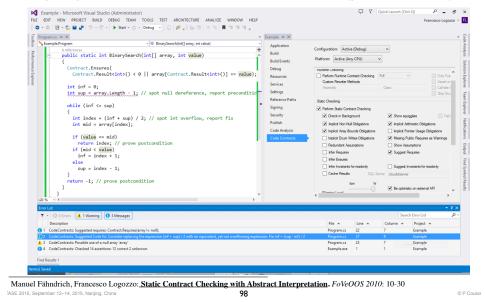
```
typedef enum {FALSE = 0, TRUE = 1} BOOLEAN;
 BOOLEAN INIT; float P, X;
 void filter () {
    static float E[2], S[2];
    if (INIT) { S[0] = X; P = X; E[0] = X; }
    else { P = (((((0.5 * X) - (E[0] * 0.7)) + (E[1] * 0.4))
                + (S[0] * 1.5)) - (S[1] * 0.7)); \}
   E[1] = E[0]; E[0] = X; S[1] = S[0]; S[0] = P;
    /* S[0], S[1] in [-1327.02698354, 1327.02698354] */
 }
 void main () { X = 0.2 * X + 5; INIT = TRUE;
    while (1) {
      X = 0.9 * X + 35; /* simulated filter input */
      filter (); INIT = FALSE; }
                                97
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```

Comments on screenshot (courtesy Francesco Logozzo)

- I. A screenshot from Clousot/cccheck on the classic binary search.
- 2. The screenshot shows from left to right and top to bottom
 - C# code + CodeContracts with a buggy BinarySearch
 - 2. cccheck integration in VS (right pane with all the options integrated in the VS project system)
 - 3. cccheck messages in the VS error list
- 3. The features of cccheck that it shows are:
 - I. basic abstract interpretation:
 - the loop invariant to prove the array access correct and that the arithmetic operation may overflow is inferred fully automatically
 - 2. different from deductive methods as e.g. ESC/Java or Boogie where the loop invariant must be provided by the end-user
 - 2. inference of necessary preconditions:
 - I. Clousot finds that array may be null (message 3)
 - 2. Clousot suggests and propagates a necessary precondition invariant (message 1)
 - 3. array analysis (+ disjunctive reasoning):
 - 1. to prove the postcondition should infer property of the content of the array
 - 2. please note that the postcondition is true even if there is no precondition requiring the array to be sorted.
 - 4. verified code repairs:
 - from the inferred loop invariant does not follow that index computation does not overflow

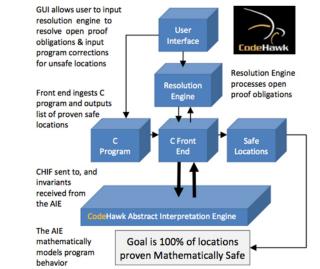
Code Contract Static Checker (cccheck)

https://github.com/Microsoft/CodeContracts (public domain)



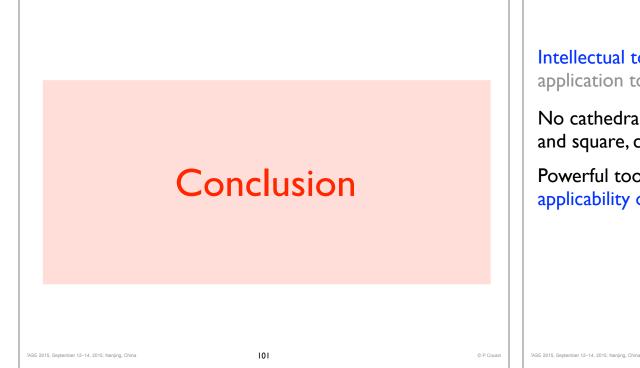
Example III: CodeHawk

• http://www.kestreltechnology.com



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Abstract interpretation

Intellectual tool (not to be confused with its specific application to iterative static analysis with $\bigtriangledown \& \bigtriangleup$)

No cathedral would have been built without plumb-line and square, certainly not enough for skyscrapers:

Powerful tools are needed for progress and applicability of formal methods

Abstract interpretation

Varieties of researchers in formal methods:

- (i) explicitly use abstract interpretation, and are happy to extend its scope and broaden its applicability
- (ii) implicitly use abstract interpretation, and hide it
- (iii) pretend to use abstract interpretation, but misuse it
- (iv) don't know that they use abstract interpretation, but would benefit from it

Never too late to upgrade

The End

102

